



UDC 622

ISSN 2334-8836 (Štampano izdanje)  
ISSN 2406-1395 (Online)

# Mining and Metallurgy Engineering Bor

2/2015



Published by: Mining and Metallurgy Institute Bor

---

---

MINING AND METALLURGY INSTITUTE BOR

---

**MINING AND METALLURGY ENGINEERING**  
BOR is a journal based on the rich tradition of expert and scientific work from the field of mining, underground and open-pit mining, mineral processing, geology, mineralogy, petrology, geomechanics, metallurgy, materials, technology, as well as related fields of science. Since 2001, is published twice a year, and since 2011 four times year.

**Editor-in-chief**

Academic Ph.D. Milenko Ljubojev, Principal Research Fellow, Associate member of ESC Mining and Metallurgy Institute Bor  
E-mail: [milenko.ljubojev@irmbor.co.rs](mailto:milenko.ljubojev@irmbor.co.rs)  
Phone: +38130/454-109, 435-164

**Editor**

Vesna Marjanović, B.Eng.

**English Translation**

Nevenka Vukašinović

**Technical Editor**

Suzana Cvetković

**Preprinting**

Vesna Simić

**Printed in:** Grafomedtrade Bor

**Circulation:** 200 copies

**Web site**

[www.irmbor.co.rs](http://www.irmbor.co.rs)

**Journal is financially supported by**

The Ministry of Education, Science and Technological Development of the Republic Serbia  
Mining and Metallurgy Institute Bor

**ISSN 2334-8836 (Štampano izdanje)**

**ISSN 2406-1395 (Online)**

*Journal indexing in SCIndex and ISI.  
All rights reserved.*

**Published by**

Mining and Metallurgy Institute Bor  
19210 Bor, Zeleni bulevar 35  
E-mail: [milenko.ljubojev@irmbor.co.rs](mailto:milenko.ljubojev@irmbor.co.rs)  
Phone: +38130/454-110

**Scientific – Technical Cooperation with  
the Engineering Academy of Serbia**

**Editorial Board**

Prof.Ph.D. Tajduš Antoni  
*The Stanislaw University of Mining and Metallurgy, Krakow, Poland*

Prof.Ph.D. Mevludin Avdić  
*MGCF-University of Tuzla, B&H*

Prof.Ph.D. Vladimi Bodarenko  
*National Mining University, Department of Deposit Mining, Ukraine*

Ph.D. Mile Bugarin, Principal Research Fellow  
*Mining and Metallurgy Institute Bor*

Prof.Ph.D. Ruža Čeliković  
*MGCF-University of Tuzla, B&H*

Ph.D. Miroslav R.Ignatović, Senior Research Associate  
*Chamber of Commerce and Industry Serbia*

Prof.Ph.D. Vencislav Ivanov  
*Mining Faculty, University of Mining and Geology "St. Ivan Rilski" Sofia Bulgaria*

Academic Prof.Ph.D. Jerzy Kicki  
*Gospodarki Surowcami Mineralnymi i Energia, Krakow, Poland*

Ph. D., PEng. Dragan Komljenović  
*Hydro-Quebec Research Institute Canada*

Ph. D. Ana Kostov, Principal Research Fellow  
*Mining and Metallurgy Institute Bor*

Prof. Ph. D. Nikola Lilić  
*Faculty of Mining and Geology Belgrade*

Ph.D. Dragan Milanović, Research Associate  
*Mining and Metallurgy Institute Bor*

Prof.Ph.D. Vitomir Milić  
*Technical Faculty Bor*

Ph.D. Aleksandra Milosavljević, Research Associate  
*Mining and Metallurgy Institute Bor*

Ph.D. Dragoslav Rakić  
*Faculty of Mining and Geology Belgrade*

Prof.Ph.D. Rodoljub Stanojlović  
*Technical Faculty Bor*

Academ Prof.Ph.D. Mladen Stjepanović  
*Engineering Academy of Serbia*

Ph.D. Biserka Trumić, Senior Research Associate  
*Mining and Metallurgy Institute Bor*

Prof.Ph.D. Neboja Vidanović  
*Faculty of Mining and Geology Belgrade*

Prof.Ph.D. Milivoj Vulić  
*University of Ljubljana, Slovenia*

Prof.Ph.D. Nenad Vušović  
*Technical Faculty Bor*

---

JOURNAL OF INTERNATIONAL IMPORTANCE, VERIFIED BY A SPECIAL DECISION  
ON THE MINISTRY OF EDUCATION, SCIENCE AND TECHNOLOGICAL DEVELOPMENT  
OF THE REPUBLIC SERBIA - M24

---

---

---

INSTITUT ZA RUDARSTVO I METALURGIJU BOR

---

MINING AND METALLURGY ENGINEERING  
BOR je časopis baziran na bogatoj tradiciji stručnog i naučnog rada u oblasti rudarstva, podzemne i površinske eksploatacije, pripreme mineralnih sirovina, geologije, mineralogije, petrologije, geomehanike, metalurgije, materijala, tehnologije i povezanih srodnih oblasti. Izlazi dva puta godišnje od 2001. godine, a od 2011. godine četiri puta godišnje.

**Glavni i odgovorni urednik**

Akademik dr Milenko Ljubojev, naučni savetnik  
Institut za rudarstvo i metalurgiju Bor  
E-mail: [milenko.ljubojev@irmbor.co.rs](mailto:milenko.ljubojev@irmbor.co.rs)  
Tel. 030/454-109, 435-164

**Urednik**

Vesna Marjanović, dipl.inž.

**Prevodilac**

Nevenka Vukašinović, prof.

**Tehnički urednik**

Suzana Cvetković, teh.

**Priprema za štampu**

Vesna Simić, teh.

**Štamparija:** Grafomedtrade Bor

**Tiraž:** 200 primeraka

**Internet adresa**

[www.irmbor.co.rs](http://www.irmbor.co.rs)

**Izdavanje časopisa finansijski podržavaju**

Ministarstvo za prosvetu, nauku i tehnološki razvoj  
Republike Srbije  
Institut za rudarstvo i metalurgiju Bor

**ISSN 2334-8836 (Štampano izdanje)**

**ISSN 2406-1395 (Online)**

*Indeksiranje časopisa u SCIndeksu i u ISI.*

*Sva prava zadržana.*

**Izdavač**

Institut za rudarstvo i metalurgiju Bor  
19210 Bor, Zeleni bulevar 35  
E-mail: [milenko.ljubojev@irmbor.co.rs](mailto:milenko.ljubojev@irmbor.co.rs)  
Tel. 030/454-110

**Naučno - tehnička saradnja sa  
Inženjerskom Akademijom Srbije**

**Uredivački odbor**

Prof. dr Tajduš Antoni  
*Stanislavov univerzitet za rudarstvo i metalurgiju,  
Krakow, Poljska*

Prof. dr Mevludin Avdić  
*RGGF-Univerzitet u Tuzli, BiH*

Prof. dr Vladimir Bodarenko  
*Nacionalni rudarski univerzitet,  
Odeljenje za podzemno rudarstvo, Ukrajina*

Dr Mile Bugarin, naučni savetnik  
*Institut za rudarstvo i metalurgiju Bor*

Prof. dr Ruža Čeliković  
*RGGF-Univerzitet u Tuzli, BiH*

Dr Miroslav R. Ignjatović, viši naučni saradnik  
*Privredna komora Srbije*

Prof. dr Vencislav Ivanov  
*Rudarski fakultet Univerziteta za rudarstvo i geologiju  
"St. Ivan Rilski" Sofija Bugarska*

Prof. dr Jerzy Kicki  
*Državni institut za mineralne sirovine i energiju,  
Krakow, Poljska*

Dr Dragan Komljenović  
*Istraživački institut Hidro-Quebec, Kanada*

Dr Ana Kostov, naučni savetnik  
*Institut za rudarstvo i metalurgiju Bor*

Prof. Dr Nikola Lilić  
*Rudarsko geološki fakultet Beograd*

Dr Dragan Milanović, naučni saradnik  
*Institut za rudarstvo i metalurgiju Bor*

Prof. dr Vitomir Milić  
*Tehnički fakultet Bor*

Dr Aleksandra Milosavljević, naučni saradnik  
*Institut za rudarstvo i metalurgiju Bor*

Dr Dragoslav Rakić, docent  
*Rudarsko geološki fakultet Beograd*

Prof. dr Rodoljub Stanojlović  
*Tehnički fakultet Bor*

Akademik Prof. dr Mladen Stjepanović  
*Inženjerska akademija Srbije*

Dr Biserka Trumić, viši naučni saradnik  
*Institut za rudarstvo i metalurgiju Bor*

Prof. dr Nebojša Vidanović  
*Rudarsko geološki fakultet Beograd*

Prof. dr Milivoj Vulić  
*Univerzitet u Ljubljani, Slovenija*

Prof. dr Nenad Vušović  
*Tehnički fakultet Bor*

---

**ČASOPIS MEĐUNARODNOG ZNAČAJA VERIFIKOVAN POSEBНОM ODLUKOM  
MINISTARSTVA ZA PROSVETU, NAUKU I TEHNOLOŠKI RAZVOJ  
REPUBLIKE SRBIJE - M24**

---

**CONTENS**  
**SADRŽAJ**

---

*Vesna Ljubojev, Vesna Marjanović, Dragan Milanović, Suzana Stanković*

MINERALOGICAL CHARACTERISTICS OF SLAG (FROM THE FLOTATION PLANT OF RTB BOR) GRANULATED IN THE LABORATORY CONDITIONS .....	1
MINERALOŠKE OSOBINE ŠLIJAKE (IZ POGONA „FLOTACIJE“ RTB BOR) GRANULISANE U LABORATORIJSKIM USLOVIMA .....	7

*Zoran Vaduvesković, Daniel Kržanović, Nenad Vušović*

CONVERSION OF FLOTATION PROCESSING USING THE HEAP LEACHING METHOD IN THE MINE CEMENTACIJA – KRAKU BUGARESKU IN THE COPPER MINE BOR .....	13
KONVERZIJA FLOTACIJSKE PRERADE POSTUPKOM LUŽENJA NA GOMILI NA RUDNIKU CEMENTACIJA – KRAKU BUGARESKU U RUDNIKU BAKRA BOR .....	21

*Dragan Zlatanović, Vladimir Milisavljević, Milenko Ljubojev, Dragan Ignjatović*

FORECAST THE BEHAVIOUR OF ROCK MASS BEFORE TAKING UP THE EXCAVATION AT DEEPER LAYERS OF THE ORE BODY BORSKA REKA .....	29
PROGNOZA PONAŠANJA STENSKOG MASIVA PRE OTKOPAVANJA NA DUBLJIM HORIZONTIMA RUDNOG TELA BORSKA REKA .....	41

*Miodrag Miljković, Rodoljub Stanojlović, Jovica Sokolović*

DETERMINATION THE NECESSARY STRENGHT OF STOPE FILLINGS AT TOTAL LAYER EXCAVATION .....	53
ODREĐIVANJE POTREBNE ČVRSTOCJE ZASIPA PRI POTPUNOM OTKOPAVANJU LEŽIŠTA .....	61

*Daniel Kržanović, Nenad Vušović, Zoran Vaduvesković, Milenko Ljubojev*

ANALYSIS THE LONG-TERM DEVELOPMENT OF THE OPEN PIT NORTH MINING DISTRICT MAJDANPEK FOR THE CAPACITY OF $5 \times 10^6$ TONS OF ORE ANNUALLY .....	69
ANALIZA DUGOROČNOG RAZVOJA POVRŠINSKOG KOPA SEVERNI REVIR MAJDANPEK ZA KAPACITET $5 \times 10^6$ TONA RUDE GODIŠNJE .....	79

*Branislav Rajković, Zoran Ilić, Daniela Urošević*

TAKE UP PULLEY SELECTION OF BELT CONVEYOR FOR THE ORE IN TERMS OF AXLE SIZING .....	89
IZBOR ZATEZNOG BUBNJA TRAKASTOG TRANSPORTERA ZA RUDU SA ASPEKTA DIMENZIONISANJA OSOVINE .....	95

***Milka Vidović, Vojin Gordanić, Ivana Trajković, Sanja Jovanić***

HYDROGEOCHEMICAL INVESTIGATION OF GROUND AND SURFACE WATER IN THE NEOGENE - QUATERNARY SEDIMENTS .....	101
HIDROGEOHEMIJSKA ISPITIVANJA KVALITETA PODZEMNIH POVRŠINSKIH VODA U NEOGENIM – KVARTARNIM SEDIMENTIMA .....	107

***Vojin Gordanić, Milka Vidović, Ivana Trajković, Saša Rogan***

GEOCHEMICAL MAPPING OF RIVERBANK PROFILES IN THE BASIN AREA OF THE RIVER IBAR: ROLE IN ESTABLISHING THE GEOCHEMICAL BASIS FOR THE ASSESSMENT OF ANTHROPOGENIC INFLUENCE ON THE ENVIRONMENT .....	113
GEOHEMIJSKO KARTIRANJE OBALSKIH PROFILA U SLIVNOM PODRUČJU REKE IBAR: ULOGA U USPOSTAVLJANJU GEOHEMIJSKE OSNOVE ZA PROCENU ANTROPOGENOG UTICAJA NA ŽIVOTNU SREDINU .....	121

***Biserka Trumić, Aleksandra Ivanović, Vojka Gardić***

SEGREGATION OF IMPURITIES IN PLATINUM AND PLATINUM-BASED ALLOYS .....	129
SEGREGACIJA NEĆISTOĆA U PLATINI I LEGURAMA NA BAZI PLATINE .....	139

***Bore Jegdić, Maja Stevanović, Aleksandar Jegdić***

CHEMICAL AND ELECTROCHEMICAL DISSOLUTION OF CHROMIUM AT ROOM AND Elevated TEMPERATURES .....	149
HEMIJSKO I ELEKTROHEMIJSKO RASTVARANJE HROMA NA SOBNOJ I NA POVIŠENIM TEMPERATURAMA .....	155

***Ljiljana Savić, Vladimir Radovanović, Ljubinko Savić***

BUSINESS SUCCESS MANAGEMENT .....	161
UPRAVLJANJE POSLOVNIM USPEHOM .....	171

***Slavica Miletić, Dejan Bogdanović, Jane Paunković***

SELECTION OF THE OPTIMAL MODEL OF INTEGRATED S USTAINABLE MANAGEMENT SYSTEM IN THE MINING COMPANIES .....	181
IZBOR OPTIMALNOG MODELA INTEGRISANOG ODRŽIVOG SISTEMA MENADŽMENTA U RUDARSKIM KOMPANIJAMA .....	193

---

Vesna Ljubojev\*, Vesna Marjanović\*, Dragan Milanović\*, Suzana Stanković\*

## MINERALOGICAL CHARACTERISTICS OF SLAG (FROM THE FLOTATION PLANT OF RTB BOR) GRANULATED IN THE LABORATORY CONDITIONS\*\*

### Abstract

A sample of slag from the Flotation Bor, RTB Bor, was mineralogical tested after granulation in the laboratory conditions. Minerals contained in the sample of granulated slag are: fayalite and ferrite that form the basis with rarely sprayed fine particles of magnetite, pyrite, chalcopyrite, bornite, copper matte and elemental - native copper [6, 7]. Granulation of slag was conducted in the laboratory conditions on the device specially designed for this purpose.

**Keywords:** smelter slag, copper minerals, fayalite, mineralogical testing

### INTRODUCTION

The copper smelter slag is produced as a by-product during the pyrometallurgical copper smelting. The composition and concentration of elements in slag depends on the composition of ore concentrate which is processed and technological processing methods. Slag represents the complex systems of a number of components, which occur at high smelting temperature, such as non-metallic inclusions and newlyformed oxides [1].

Many years metallurgical processing of copper concentrate in the industrial complex of RTB Bor has created a dump slag, which is used as the secondary raw material, as it contains significant amounts of valuable metals. Total amount of slag in the "Depot - Slag 1" amounts to about 9,190,940 tons with the medium content of Cu - 0.715%, Au – 0.282 g/t, Ag - 4.5 g/t and Mo 0.0413% [2].

In the Flotation Plant Bor, the section C was originally designed for flotation of ore, and later adapted for flotation of slag [3].

The process of slag comminution in the plant consists of crushing and grinding.

However, the ore is suitable for comminution from the standpoint of consumption the energy, linings and grinding bodies of slag and to explore the possibility of energy saving and reducing the wear of linings and grinding bodies in the process of grinding; heating of slag was carried out in the laboratory conditions to the melting point and its cooling by a jet of water to form the granules of slag. It would consider the possibility of expulsion the process of comminution in the industrial conditions, and enabled the saving of energy and raw material [4].

### SAMPLE AND EXPERIMENTAL METHOD

A sample of smelting slag was taken from the crushing process in the Flotation Plant in Bor [4].

\* Mining and Metallurgy Institute Bor

\*\* This work is the result of the Project TR33023 "Development of Technologies for Flotation Processing the Copper Ore and Precious Metals to Achieve Better Technological Results" funded by the Ministry of Education, Science and Technological Development of the Republic of Serbia

Upon completion the natural drying, sampling was performed according to the standard method of sampling and a repre-

sentative sample was formed that was physically and chemically analyzed. The chemical composition of the sample is given in Table 1.

**Table 1** Chemical content of sample and granulated slag [5]

Content (%) compound – chemical element	Sample	Analytical method
Cu	0.33	ASS
Fe <sub>3</sub> O <sub>4</sub>	3.41	A- Fe <sub>3</sub> O <sub>4</sub>
CaO	19.60	V
S	0.20	G
Fe	27.92	V
SiO <sub>2</sub>	46.72	G
Al <sub>2</sub> O <sub>3</sub>	4.52	ICP-AES

The term granulation involves rapidly cooling the liquid-hot slag under the pressurized cold water and obtaining the slag in the form of irregular granules. The quality of granules depends on the chemical composition of slag, slag temperature before spillage, rate of slag spillage, pressure and the amount of cooling water [4].

Previously dried and analyzed slag was subjected to melting in an induction furnace for smelting, power of 100 kWh, in a pot volume V = 10 h, manufacturer ELING - Loznica. During the experiment, 25 kg of slag was melt at the temperature of spillage of T = 1,250°C [8].

Granulation of slag in the laboratory conditions was performed on a specially designed granulator which is mobile and allows rapidly cooling of slag by jets, which are located on the front side of the tank, just behind a roller of granulator, which has one part immersed in cooling water. Below the roller is a carrying basket with a perforated bottom that accepts the resulting granules and that after discharging the total amount of slag from furnace is removed by a crane after draining, left in a basket for granulated slag [4].

Copper and slag are insoluble in each other and due to this they are separated from each other in the furnace precipitator. Copper matte drops are denser than the slag and under the influence of gravity pass through

the slag and form a separate layer at the bottom of the furnace. Less dense layer of slag floats on a layer of copper matte. In the furnace precipitator, blister and slag layers are formed separately in two separate layers. The basic components of slag during melting of copper concentrate are SiO<sub>2</sub>, FeO, Fe<sub>2</sub>O<sub>3</sub> and MgO, and slag often contains Fe<sub>3</sub>O<sub>4</sub>, Al<sub>2</sub>O<sub>3</sub>, Cu<sub>2</sub>S, and smaller quantities fine droplets of mechanically affected copper. Copper content in the slag of flame furnace should be from 0.15 to 0.25%. However, due to significant presence of mechanically included copper matte in the slag, and due to the chemical bound copper in the form of copper oxide, copper content in the slag is higher [1].

Compound FeO in slag is most commonly found in the form of fayalite, Fe<sub>2</sub>SiO<sub>4</sub>, in which an excess of iron oxide can be dissolved, as it is the case in base slag.

## MINERALOGICAL TESTING OF GRANULATES SLAG

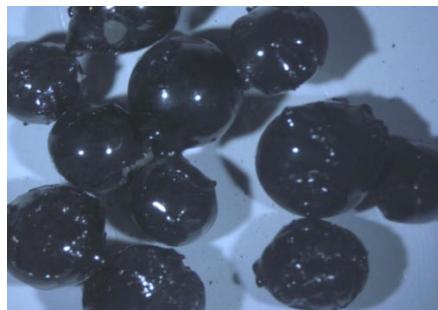
Determination of mineral composition and structural-textural characteristics of minerals was made on a representative sample [6, 7].

The samples poured into acrylic resin are made of the obtained representative sample of granulated slag. Determination of slag

samples was done on a microscope for transmitted and reflected light, the brand AXIOSKOP 40, with the device for microphoto. The chemical analysis on Niton was also carried out.

Qualitative mineralogical analysis was carried out under the polarization microscope for reflected light in the air for the purpose of identification the ore and non-ore minerals. Quantitative mineralogical analysis was carried out by the method of parallel sections, with spacing of 1 mm. The distance between the examined fields and sections were moved by hand. Determination of slag samples was done on the microscope for transmitted and reflected light, the brand AXIOSCOPE 40, with the device for microphoto.

Based on the qualitative mineralogical analyses the following mineral composition of slag was determined: solid sulfide melt (Cu-Fe), chalcocite, pyrite, copper, chalcopyrite, bornite, magnetite and gangue minerals. Gangue minerals were presented with a



**Figure 1** Spherical grains in granulated slag, binocular, magnification 6.5 x

### Microscopic description

Microscopic analysis has showed that the granulated slag is mainly built of fayalite and ferrite that build the basis in which fine particles of magnetite, pyrite, chalcopyrite, chalcocite, bornite, copper matte and elemental (native) copper are rarely sprayed, Figure 3.

Fayalite (iron silicate) is represented in the form of poke crystals, which indicates

glass with occurrence a variety of eutectic dendrites (fayalite and others) that were not particularly determined.

Structural characteristics of samples can be divided into:

1. Simple mesogen present the investigated mineral that is easily adhered to one mineral or only gangue - double mesogens.
2. Complex mesogen presents the investigated mineral that is adhered to more minerals and gangues – multiple mesogens.

### Macroscopic description of granulated slag

Granulated slag has various coarseness with visible larger pieces. The spheroids of different sizes, smooth surfaces can be observed in a sample of granulated slag, Figure 1, as well as large number of very sharp glassy particles of slag, Figure 2. The sample is dark gray to black.



**Figure 2** Grains of granulated slag (sharp edges), binocular, magnification 2.0 x

the product of smelting - slag. Ferrites (various iron oxides), also indicate the product of ore smelting. They are represented in the form of skeletal crystals (dendrites), Figure 9.

Magnetite occurs predominantly independent, in the form of cube and radial radiating aggregates. It rarely occurs in irregular shapes, Figures 7 and 8.

Pyrite is the most common of all sulfide minerals and occurs in the form of hypidiomorphic grains, mostly independent (free grain).

Since copper minerals occur chalcopyrite, chalcocite and bornite, in Figure 6.

Chalcopyrite occurs in irregular, relatively small, fields, rarely adhered to chalcocite,

while some grains are permeated with chalcocite.

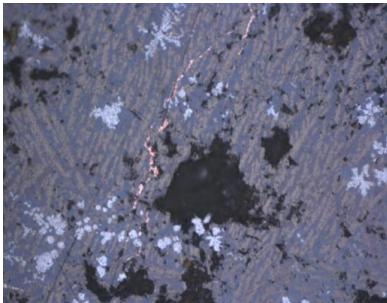
Chalcocite is less frequent in fine grains; it is free or is adhered to chalcopyrite and gangue mineral.

Elemental (native) copper occurs in the form of fine spherical shapes and small veins, Figures 4, 5 and 10.

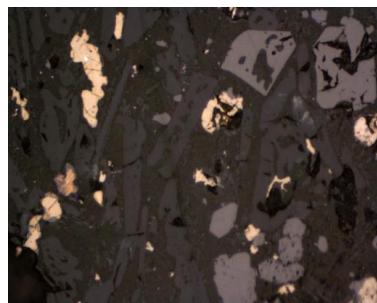
#### Micropotos of slag



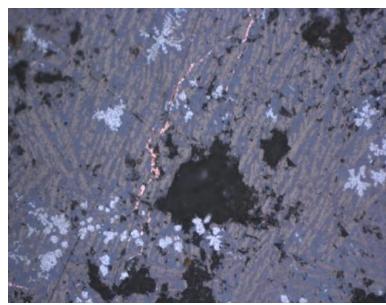
**Figure 3** Copper matte, bornite and chalcopyrite, magnification 500 x II N



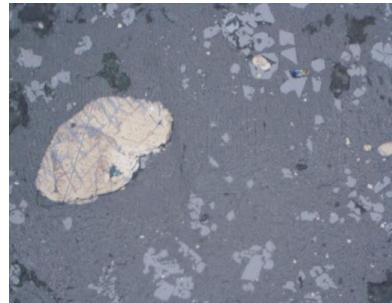
**Figure 5** Veins of elemental copper, magnification 500 x II N



**Figure 7** Magnetite in the form of cube, chalcopyrite, magnification 500 x II N



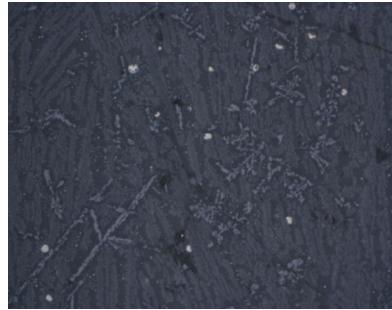
**Figure 4** Veins of elemental copper in fayalite basis, magnification 500 x II N



**Figure 6** Chalcopyrite grains in fayalite basis, permeated with chalcocite, magnification 500 x II N



**Figure 8** Magnetite in various forms, magnification 500 x II N



**Figure 9** Fayalite dendrites,  
magnification 500 x II N



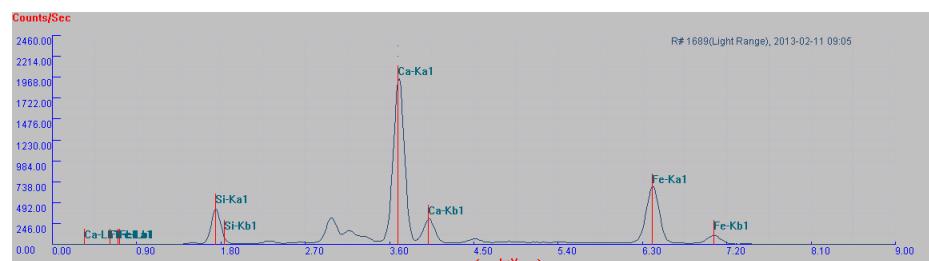
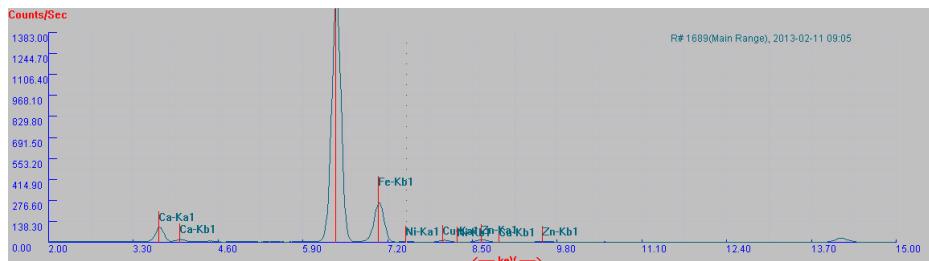
**Figure 10** Veins of elemental copper,  
magnification 500 x II N

Chemical analysis of samples of granulated slag was done on apparatus NITON XL-L3t-900 from which it can be concluded that iron is the most common of 25.791%. This indicates a large content of

iron minerals, which after thermal oxidation treatment transfer into  $\text{Fe}_2\text{O}_3$  and  $\text{Fe}_3\text{O}_4$ . The copper content is 0.156%. The obtained results are shown in Table 2 and Figure 11.

**Table 2** Chemical analysis obtained by recording on X-ray NITON XL-3t-90

Compounds – Chemical elements	Cu	S	Fe	Si	Ca	Al	Zn
Content, %	0.156	1.117	25.791	21.639	11.082	2.588	0.121



**Figure 11** Chemical analysis obtained by recording on X-ray NITON XL-3t-90

## CONCLUSION

Granulated slag from the process of pyrometallurgical smelting of copper is in the form of spherical grains and grains with sharp edges. Slag mainly contains oxide species and several species of sulfide minerals. The main component is the fayalite basis in which copper, chalcopyrite, magnetite and copper matte are permeated. Copper is in the form of copper matte and elemental copper in the form of veins in the fayalite basis. Magnetite is in the form of cube and other various forms.

## REFERENCES

- [1] Morales A., Cruells M., Roca A., Bergo R., Treatment of Copper Flash Smelter Dusts for Copper and Zinc Extraction and Arsenic Stabilization, Hydrometallurgy 105(2010), p. 148-154.
- [2] Mitrović Z., et al., Main Mining Project for Slag Excavation from Technogenic Deposit “Depot Slag 1”, Verification the Technological Process of Concentrate Obtaining and Superelevation of the Flotation Tailing Dump “RTH” in Bor to K +378 for Annual Production of 1,200,000 t Slag; Copper Institute Bor, 2006;
- [3] <http://rtb.rs/rtb-bor-doo/rudnik-bakra-bor/flotacija-bor/>
- [4] Magdalinović S., Milanović D., Čadežnović B., Marjanović V., Technological Method of Slag Granulation to Reduce Grain-size at the Inlet into Flotation, Mining Engineering 3(2011), p. 101-110;
- [5] Čadežnović B., Marjanović V., Ljubojev V., Milanović D., Possibilities of Use the Copper Matte From Smelter Slag in its Direct in its Direct Discharge from Furnace, Mining Engineering, 2(2012), p. 143-148;
- [6] Ljubojev V., Petrović J., Krstić S., Mineralogical Characteristics of Smelting Slag in the Technogenic Deposit “Depot 1” (Bor, Serbia). The Geology in digital Age: Proceedings of the Meeting of the Association of European Geological Societies (MAEGS 17), Belgrade (2011), p. 237-240;
- [7] Ljubojev V., Repost on Microscope Testing of Granulated Slag, MMI Bor, May, 2013.
- [8] Čadjenović B., Drobnjaković B., Milanović D., Magdalinović S., New Laboratory Plant for Granulation Using the Changed Technological Process of Smelter Slag Discharging, R. radovi 4(2011), p. 99-104.
- [9] Požega E., Gomidželović L., Copper Smelters with Reverbatory and ISASMELT Furnace, Bakar 2(2010), p. 25-32.

Vesna Ljubojev\*, Vesna Marjanović\*, Dragan Milanović\*, Suzana Stanković\*

**MINERALOŠKE OSOBINE ŠLJAKE  
(IZ POGONA „FLOTACIJE“ RTB BOR)  
GRANULISANE U LABORATORIJSKIM USLOVIMA\*\***

*Izvod*

*Uzorak šljake iz pogona „Flotacije“ Bor, RTB-a Bor je mineraloški ispitivan posle granulacije u laboratorijskim uslovima. Minerali koji se nalaze u uzorku granulisane šljake su: fajalit i ferit koji čine osnovu, u koju su retko uprskane sitne čestice magnetita, pirita, halkopirita, bornita, bakrenca i elementarnog – samorodnog bakra [6, 7]. Granulisanje šljake je vršeno u laboratorijskim uslovima na uredaju specijalno konstruisanom za tu namenu.*

*Ključne reči:* topionička šljaka, minerali bakra, fajalit, mineraloško ispitivanje

**UVOD**

U topionicama bakra šljaka nastaje kao nus-proizvod u toku pirometalurškog topljenja bakra. Sastav i koncentracija elemenata u šljaci zavisi od sastava koncentrata rude koja je prerađena i tehnoloških postupaka prerade. Šljaka predstavlja složene sisteme većeg broja komponenata, koji nastaju na visokoj temperaturi topljenja, kao što su nemetalični uključci i novonastali oksidi [1].

U industrijskom kompleksu RTB Bor višegodišnja metalurška prerada koncentrata bakra stvorila je deponiju šljake, a koja se koristiti kao sekundarna sirovina, jer sadrži značajne količine korisnih metala. Ukupne količine šljake u „Depo - šljake 1“ iznose oko 9.190.940 t sa srednjim sadržajem Cu - 0,715%, Au - 0,282 g/t, Ag - 4,5 g/t i Mo 0,0413% [2].

U pogonu „Flotacije Bor“, sekcija C je prvo bitno projektovana za flotaciju rude, a

kasnije je prilagođena za flotaciju šljake [3]. Proces usitnjavanja šljake u pogonu se sastoji od drobljenja i mlevenja.

Međutim, ruda je pogodnija za usitnjavanje sa stanovišta potrošnje energije, obloga i meljućih tela od šljake i da bi se istražila mogućnost uštede energije i smanjenje habanja obloga i meljućih tela u procesu usitnjavanja, u laboratorijskim uslovima izvršeno je zagrevanje šljake do tačke topljenja i njeno hlađenje mlazom vode radi formiranja granula šljake. Time bi se razmotrila mogućnost izbacivanja procesa drobljenja u industrijskim uslovima, i omogućila ušteda energije i repro materijala [4].

**UZORAK I EKSPERIMENTALNA PROCEDURA**

Uzorak topioničke šljake uzet je iz procesa drobljenja u pogonu „Flotacije“ u Boru [4].

\* Institut za rudarstvo i metalurgiju Bor

\*\* Ovaj rad je proistekao kao rezultat projekta TR33023 "Razvoj tehnologija flotacijske prerade ruda bakra i plemenitih metala radi postizanja boljih tehnoloških rezultata" finansiranog od strane Ministarstva prosvete, nauke i tehnološkog razvoja Republike Srbije

Po završetku prirodnog sušenja izvršeno je uzorkovanje prema standardnoj metodi i formiran je reprezentativan

uzorak koji je fizički i hemijski analiziran. Hemijski sastav uzorka dat je u tabeli 1.

**Tabela 1.** Hemijski sastav uzorka i granulisane šljake [5]

Sadržaj (%) jedinjenja - hemijskog elementa	Uzorak	Analitička metoda
Cu	0,33	ASS
Fe <sub>3</sub> O <sub>4</sub>	3,41	A- Fe <sub>3</sub> O <sub>4</sub>
CaO	19,60	V
S	0,20	G
Fe	27,92	V
SiO <sub>2</sub>	46,72	G
Al <sub>2</sub> O <sub>3</sub>	4,52	ICP-AES

Pod pojmom granulacije podrazumeva se naglo hlađenje tečne usijane šljake pod pritiskom hladne vode i dobijanje šljake u vidu nepravilnih granula. Kvalitet granula zavisi od hemijskog sastava šljake, temperature šljake pre izlivanja, brzine izlivanja šljake, pritiska i količine rashladne vode [4].

Prethodno osušena i analizirana šljaka je podvrgnuta topljenju u indukcionoj peći za topljenje, snage 100 kWh, u loncu zapremine V=10 L, proizvođača ELING - Loznica. Prilikom eksperimenta istopljeno je 25 kg šljake, temperatura pri kojoj je šljaka izlivena je bila T=1.250°C. [8]

Granuliranje šljake u laboratorijskim uslovima je izvršeno na specijalno konstruisanom granulatoru koji je mobilan i omogućava, da se šljaka naglo hlađi mlaznicama, koje se nalaze na čeonoj prednjoj strani rezervoara, odmah iza valjka granulatora, kome je jedan deo potopljen u rashladnu vodu. Ispod valjka je prihvatri koš sa perforiranim dnom, koji prihvata nastale granule i koji se nakon izlivanja celokupne količine šljake iz peći vadi uz pomoć dizalice i nakon ceđenja, odlaže u korpu za granulisanu šljaku [4].

Bakrenac i šljaka su nerastvorljivi jedan u drugo i zbog toga oni se odvajaju jedno od drugog u pećnom taložniku. Kapljice bakrenca su gušće od šljake i pod uticajem

gravitacije prolaze kroz šljaku i na dnu peći formiraju poseban sloj. Manje gušći sloj šljake pluta na sloju bakrenca. U pećnom taložniku, slojevi blistera i šljake formiraju se odvojeno u dva posebna sloja. Osnovne komponente šljake prilikom topljenja bakarnog koncentrata su SiO<sub>2</sub>, FeO, Fe<sub>2</sub>O<sub>3</sub> i MgO, a šljaka često sadrži i Fe<sub>3</sub>O<sub>4</sub>, Al<sub>2</sub>O<sub>3</sub>, Cu<sub>2</sub>S, i u manim količinama sitne kapljice mehanički zahvaćenog bakrenca. Sadržaj bakra u šljaci plamene peći trebao bi da bude od 0,15 do 0,25 %. Međutim, zbog značajnog prisustva mehanički uključenog bakrenca u šljaci i zbog hemijski vezanog bakra u obliku oksida sadržaj bakra u šljaci je veći [1].

Jedinjenje FeO u šljaci se najčešće nalazi u obliku fajalita, Fe<sub>2</sub>SiO<sub>4</sub>, u kome može biti rastvoren i višak gvožđe-oksida, kao što je slučaj u baznim šljakama.

## MINERALOŠKO ISPITIVANJE GRANULISANE ŠLJAKE

Na reprezentativnom uzorku izvršena je determinacija mineralnog sastava i određivanje strukturno-teksturnih karakteristika minerala [6, 7].

Od dobijenog reprezentativnog uzorka granulisane šljake urađeni su preparati uliveni u akrilnu smolu. Determinacija uzorka šljake rađena je mikroskopom za propuštenu

i odbijenu svetlost, marke AXIOSKOP 40, sa uređajem za mikrofotografiju. Takođe, urađena je hemijska analiza na Nitonu.

Kvalitativna mineraloška analiza rađena je pod polarizacionim mikroskopom za odbijenu svetlost u vazduhu u cilju identifikacije rudnih i nerudnih minerala. Kvanti-tativna mineraloška analiza rađena je metodom paralelnih profila, sa rastojanjem od 1 mm. Rastojanje između ispitivanih polja i profila pomerana su ručno. Determinacija uzoraka šljake rađena je mikroskopom za propuštenu i odbijenu svetlost, marke AXIOSKOP 40, sa uređajem za mikrofotografiju.

Na osnovu kvalitativnih mineraloških analiza utvrđen je sledeći mineralni sastav šljake: čvrsti sulfidni rastop (Cu-Fe), haldozin, pirit, bakar, halkopirit, bornit, magnetit i minerali jalovine. Minerali jalovine predstavljeni su stakлом sa pojmom različitih

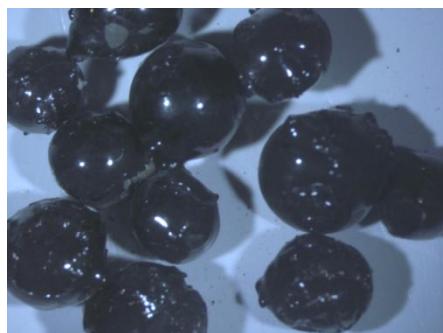
eutektičkih dendrita (fajalit i dr.) koji nisu posebno određivani.

Strukturne karakteristike uzorka možemo podeliti na :

1. Prosti sraslac, predstavlja ispitivani mineral koji je jednostavno srastao sa jednim mineralom ili samo jalovinom - dvojni sraslaci.
2. Složeni sraslac, predstavlja ispitivani mineral koji je srastao sa više minerala i jalovinom višebrojni sraslaci.

#### Makroskopski opis granulisane šljake:

Granulisana šljaka je različite krupnoće sa vidljivim većim komadima. U uzorku granulisane šljake mogu se zapaziti sferični oblici različite veličine, glatkih površina, slika 1., kao i veliki broj veoma oštih staklastih čestica šljake, slika 2. Uzorak je tamnosive do crne boje.



Sl. 1. Sferična zrna u granulisanoj šljaci, binokular, uvećanje 6,5 x



Sl. 2. Zrna granulisane šljake (oštih ivica), binokular, uvećanje 2,0 x

#### Mikroskopski opis

Mikroskopskim ispitivanjem utvrđeno je da je granulisana šljaka pretežno izgrađena od fajalita i ferita koji grade osnovu u koju su retko uprskane sitne čestice magnetita, pirita, halkopirita, haldozina, bornita, bakrena i elementarnog (samorodnog) bakra, slika 3.

Fajalit (silikati gvožđa) su zastupljeni u vidu pritkastih kristalića, što ukazuje na proizvod topljenja rude – šljaka. Feriti (razni

oksidi gvožđa), takođe ukazuju na proizvod topljenja rude. Zastupljeni su u vidu skeletnih kristala (dendrita), slika 9.

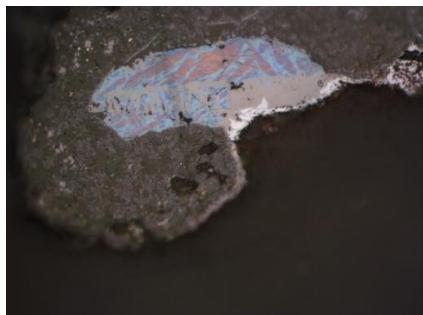
Magnetit se javlja pretežno samostalan, u formi kocke i radialno zrakastih agregata. Ređe se javlja u nepravilnim oblicima, slika 7 i 8.

Od svih sulfidnih minerala pirit je najzastupljeniji i javlja se u vidu hipidiomorfnih zrna, uglavnom samostalan (slobodna zrna).

Od minerala bakra javljaju se halkopirit, halkozin i bornit, slika 6.

Halkopirit se javlja u nepravilnim, relativno sitnim, poljima, retko srastao sa halkozinom, dok su pojedina zrna prožeta halkozinom.

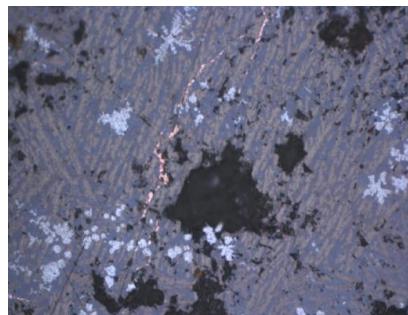
#### Mikrofotografije šljake



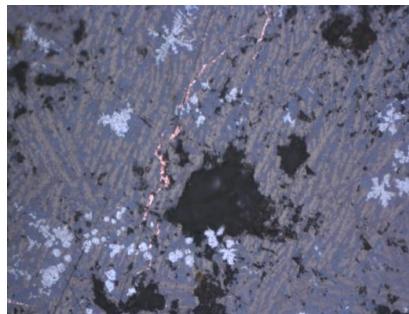
Sl. 3. Bakrenac, bornit i halkopirit, uvećanje 500 x II N

Halkozin se ređe javlja u sitnim zrnima slobodan ili je srastao za halkopirit i jaloninu.

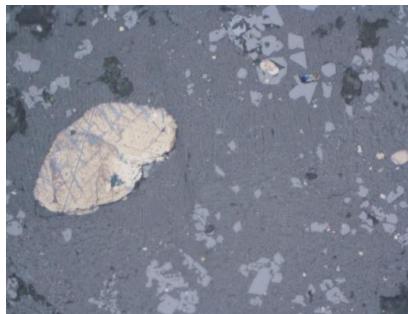
Elementarni (samorodni) bakar se javlja u vidu sitnih sferičnih oblika kao i sitnih žilica, slike 4, 5 i 10.



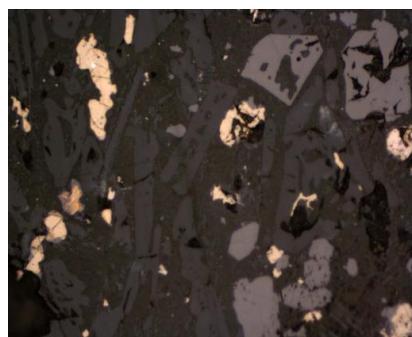
Sl. 4. Žilice elementarnog bakra u fajalitskoj osnovi, uvećanje 500 x II N



Sl. 5. Žilice elementarnog bakra u bakrencu, uvećanje 500 x II N



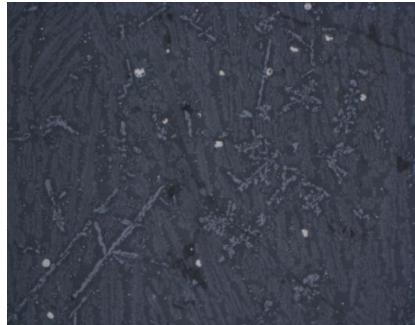
Sl. 6. Zrno halkopirita u fajalitskoj osnovi, prožeto halkozinom, uvećanje 500 x II N



Sl. 7. Magnetit u formi kocke, halkopirit, uvećanje 500 x II N



Sl. 8. Magnetit u različitim formama, uvećanje 500 x II N



**Sl. 9.** Dendriti fajalita,  
uvećanje 500 x II N



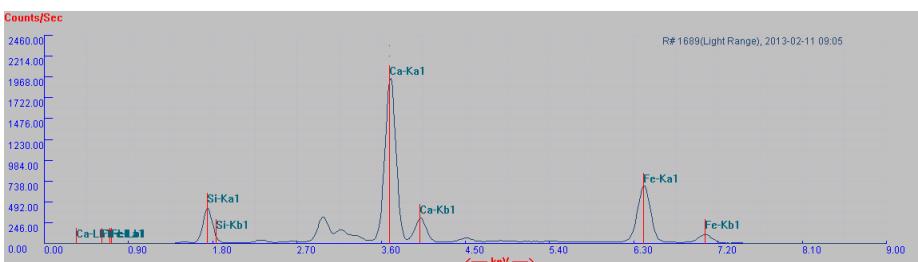
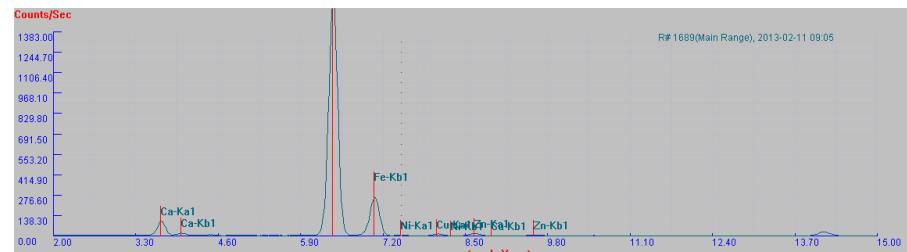
**Sl. 10.** Žilice elementarnog bakra,  
uvećanje 500 x II N

Hemijska analiza uzorka granulisane šljake urađena je na aparatu NITON XL-L3t-900 iz koje se može konstatovati da je gvožđe najzastupljenije 25,791%. To ukazuje na veliki sadržaj minerala

gvožđa, koji nakon termičkog tretmana oksidacijom prelaze u  $\text{Fe}_2\text{O}_3$  i  $\text{Fe}_3\text{O}_4$ . Sadržaj bakra je 0,156%. Dobijeni rezultati su prikazani na u tabeli 2 i na slici 11.

**Tabela 2.** Hemijska analiza dobijena snimanjem na rengenu NITON XL-3t-90

Jedinjenja - hemijski elementi	Cu	S	Fe	Si	Ca	Al	Zn
Sadržaj, %	0,156	1,117	25,791	21,639	11,082	2,588	0,121



**Sl. 11.** Hemijska analiza dobijena snimanjem na rengenu NITON XL-3t-90

## ZAKLJUČAK

Granulisana šljaka iz procesa pirometalurškog topljenja bakra je u obliku sferičnih zrna i zrna oštih ivica. Šljaka sadrži uglavnom oksidne vrste i nekoliko sulfidnih vrsta minerala. Glavna komponenta je fajalitska osnova u koju je prožet bakar, halkopirit, magnetit i bakrenac. Bakar se nalazi u obliku bakrena i elementarnog bakra u obliku žilica u fajalitskoj osnovi. Magnetit se nalazi u formi kocke i drugim različitim formama.

## LITERATURA

- [1] Morales A., Cruells M., Roca A., Bergo R., Treatment of Copper Flash Smelter Dusts for Copper and Zinc Extraction and Arsenic Stabilization, Hydrometallurgy 105(2010), p. 148-154.
- [2] Mitrović Z., i dr., Glavni rudarski projekat otkopavanja šljake iz tehnogenog ležišta „Depo Šljake 1”, verifikacija tehnološkog procesa dobijanja koncentrata i nadvišenje flotacijskog jalovišta „RTH” u Boru do K +378 za godišnju proizvodnju od 1.200.000 t šljake; Institut za bakar Bor, 2006.
- [3] <http://rtb.rs/rtb-bor-doo/rudnik-bakra-bor/flotacija-bor/>
- [4] Magdalinović S., Milanović D., Čadešnović B., Marjanović V., Tehnološki postupak granuliranja šljake radi sniženja krupnoće na ulazu u flotaciju, Rudarski radovi 3(2011), str. 101-110
- [5] Čadešnović B., Marjanović V., Ljubojev V., Milanović D., Mogućnost iskorišćenja bakrena iz topioničke šljake kod njenog direktnog izlivanja iz peći, R. Radovi, 2(2012), str. 137-142.
- [6] Ljubojev V., Petrović J., Krstić S., Mineralogical characteristics of smelting slag in the technogenic deposit “Depo 1” (Bor, Serbia). The Geology in digital Age: Proceedings of the Meeting of the Association of European Geological Societies (MAEGS 17), Belgrade (2011), p. 237-240.
- [7] Ljubojev V., Izveštaj o mikroskopskom ispitivanju granulirane šljake, IRM Bor, Maj, 2013.
- [8] Čadjenović B. Drobnjaković B., Milanović D., Magdalinović S., Novo laboratorijsko postrojenje za granuliranje izmenjenim tehnološkim postupkom izlivanja topioničke šljake, R. radovi 4(2011) str. 93-98
- [9] Požega E., Gomidželović L., Topionice bakra sa plamenom i ISASMELT peći, Bakar 2(2010), str. 25-32.

Zoran Vaduvesković\*, Daniel Kržanović\*, Nenad Vušović\*\*

## CONVERSION OF FLOTATION PROCESSING USING THE HEAP LEACHING METHOD IN THE MINE CEMENTACIJA – KRAKU BUGARESKU IN THE COPPER MINE BOR\*\*\*

### Abstract

RTB Bor is planning to expand the capacity of mining and processing at the Cementacija Kraku Bugaresku site from the current 2.5 million tons per year to 5.5 million. The current processing technology - the classic flotation of the entire excavated ore, without the separation of oxide and sulfide ores, due to the low copper recovery from oxide ore, has achieved the modest financial results. This article discusses an alternative method of copper obtaining using the hydrometallurgical heap leaching and SX/EW extraction method from leach solutions, in terms of economics, i.e. comparative analysis of cash flow and discounted cash flow for both cases (scenarios). The analysis is performed in a software for strategic planning and design in mining - Whittle Fx, with the input techno-economic data for both cases [7].

Due to the frequent breakdowns and causing the accidental situations on the current infrastructure installations of the processing plants, pipeline for pulp-hydro transport from the site to the flotation plant, in conclusion, to emphasize the comparative advantages of hydrometallurgical processing are emphasized in the conclusion not only in terms of the economy but also the environmental protection. In the world, the world's largest copper producers have a tendency to make, besides copper is necessary and valuable metal, also the "green" metal.

**Keywords:** heap leaching, hydrometallurgy, oxide ore, sulfide ore, long-term dynamics of production, cash flow, discounted cash flow

### 1 INTRODUCTION

The deposit Cementacija Kraku Bugaresku has begun the exploitation in 1990 by the investment works in stripping the deposit at the site Cementacija 1. The name of the ore body and complex of ore bodies consisting of Cementacija 1, 2, 3 and 4 talks about the nature of these ore bodies. It is a cementation zone of secondary enrichment with about 40% of oxide ore, mostly at levels near the surface, which is relatively poor to the flotation process. Flotation copper re-

covery from the ore has shown in the previous work a slightly higher level than 50%. Combining the processing methods - flotation of sulfide ore with maximum 10% of oxide (considered not have a negative effect on the recovery coefficient in the flotation) will achieve a significantly better economic effects [1], but the problem is in the possibility of selective excavation and separation of the aforementioned types of ore - sulphide and oxide.

\* Mining and Metallurgy Institute Bor, Zeleni bulevar 35, Srbija

\*\* Technical Faculty Bor, University in Belgrade, Vojiske Jugoslavije 12, 19210 Bor, Serbia

\*\*\* This work is within the Projects of technological development TR33038 "Improving Technology of Exploitation and Processing of Copper Ore with Monitoring the Living and Working Environment in the RTB Bor Group" and TR34004 "The New Production Line for Copper Production by Solvent Extraction of Mine Water", funded by the Ministry of Education, Science and Technological Development of the Republic of Serbia

## **2 DESCRIPTION OF THE PROBLEM**

The major problem is in fact that the flotation processing on the deposit is only to the level of pulp obtaining, i.e. grinding and then concentration, and then the pulp is transported by hydrotransport for further processing in the Flotation Plant Veliki Krivelj. In addition to the increased costs of flotation process, this processing method is also very unfavorable from the aspect of environmental protection due to the frequent accidents on the pipeline and consequences for the environment. (The last one happened in mid-April 2014).

As with the opening of mine, the manner and type of processing were influenced by a lobby for "environmental protection". The decision on the processing method was so made without the expert analyses, not taking into account the nature of the deposit (content over 40% of oxide ore). According to the leaching method, not only due to its potential impact on the environment, but without a detailed knowledge of these matters, an animosity was created even to mention the acid, or cyanide, which are, by their nature, toxic. During the current exploitation a part of deposit, it was proved that the adopted and applied method does not give good economic effects, but also is a major polluter of the environment.

One example of the total conversion of pyrometallurgical process - flotation method of concentration and classical smelting of concentrate with electrolytic anode dissociation, hydrometallurgical process, i.e. heap leaching in combination with the "in situ" leaching assisted by bacterial leaching was applied to the mine Morenci of the Phelps Dodge company, Arizona [7] in early 2001. The existing facilities for concentration were put into a "stand by" condition while the smelter was previously relocated to a place Chino, Mexico.

In addition to this example, where the daily processing is about 75,000 tons of ore (about 360,000 tons of copper a year), the examples of total conversion of pyrometallurgical process are in Cerro Verde, (1993 - 15,000 t/d), Zaldivar (1992 - 20,000 t/d) in Peru, and Kuebrada Blanca (1,993 to 17,300 t/d) in Chile, and many other mines.

The benefits are multiple, the significant energy savings through reducing the total cost of production per tone of copper, whose purity is 99.99%, to the "clear sky" or environmental protection. It is also a way that the activities of copper exploitation and production leave behind them waste as less as possible.

## **3 COMPARATIVE ANALYSIS OF THE ECONOMIC EFFICIENCY OF CLASSICAL METHOD AND LEACHING METHOD WITH SX/EW EXTRACTION MODE**

The analysis was carried out based on the literature techno-economic data for the "heap leaching" method and hydrometallurgical extraction process SX/EW, but bearing in mind the specificity of the cementation deposit Kraku Bugaresku both from the aspect of ore mineralogy in the deposit and the possibility of using this method, and from the aspect of a comparative cost data in relation to the classical processing method for which the relevant (known) data were used.

The following Table presents the techno-economic data with which the analysis was carried out in software for strategic planning in mining, Whittle Fx, whose working principle is based on the Lerch Grosmann algorithm.

**Table 1** Input techno-economic parameters of exploitation for the optimization process

Parameter	Unit	Values
Excavation capacity - excavations	t/year	12 Mt from 3 <sup>rd</sup> year 17 Mt
Capacity of flotation processing – Sulfide ore with max. 10% oxide	t/year	2.5 Mt from 3 <sup>rd</sup> year 5.5 Mt
Capacity of heap leaching – Oxide ore with over 10% of oxide content	t/year	2.5 Mt
Copper price	\$/t cathode	5,000.00
Gold price	\$/kg	40,000.00
Silver price	\$/kg	500.00
Excavation costs	\$/t	2,3.
Costs of flotation processing	\$/t	4,00
Processing costs of heap leaching	\$/t ore	1.00
Costs of metallurgical copper treatment	\$/t cathode	450.00
Costs of metallurgical gold treatment	\$/kg	150.00
Costs of metallurgical silver treatment	\$/kg	15.00
Costs of hydrometallurgical processing (SXEW)	\$/t cathode	100.0
Initial capital costs of leaching and SXEW	\$	20,000,000
Total copper recovery (flot, and metallurgy)	%	0.788
Total gold recovery (flot, and metallurgy)	%	0.50
Silver recovery (flot, and metallurgy)	%	0.40
Copper recovery from oxide ore with over 10% of oxide content	%	0.54
Copper recovery by leaching from sulfide ore		0.55
Discount rate	%	10.0

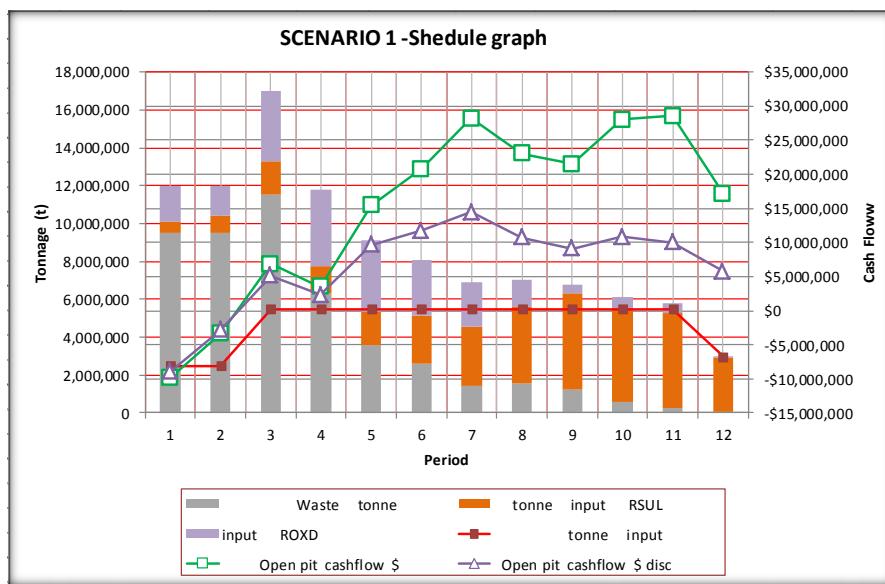
### 3.1 Scenario 1

The obtained results by Scenario 1, or the current processing process, i.e. total ore undergoes to the flotation, without selective excavation and separation on two types of ore - sulphide and oxide. For this purpose, a block model was modified and the aforementioned types of ore were separated, as well as rock types only theoretical due to the demands in the software, but

essentially the whole ore undergoes to the flotation process (mill). Table below shows the long-term dynamics of excavation with the economic indicators - cash flow, undiscounted and discounted. The analysis was done for the whole process of ore processing, both flotation and metallurgical, with the revenue of cathode copper and precious metals.

**Table 2** Long-term dynamics of excavation by Scenario 1, analyzed in the software Whittle Fx

SCENARIO 1 - SCHEDULE GRAPH																			
PB: 19, 26,3																			
Period				Units			Units			Grade			Grade			Open pit	Open pit		
	tonne	Waste	Strip	tonne	input	RSUL	tonne	input	ROXD	tonne	input	CU	tonne	input	PRCU	AU	AG	\$	\$ disc
	input	tonne	ratio	RSUL	CU	CUS	ROXD	CU	CUOX	CU	input	PRCU	AU	input	cashflow	\$	\$	disc	
1	2,497,779	9,502,221	3.8	601,834	241,726	0.2449	1,895,945	462,625	0.0413	0.282	15,4797	0.0753	1.1065	-9,847,862	-8,952,602				
2	2,499,693	9,500,307	3.8	917,321	451,536	0.3076	1,582,372	426,201	0.0484	0.3511	15,7806	0.0802	1.0753	-3,387,689	-2,799,743				
3	5,495,999	11,504,001	2.09	1,769,556	816,733	0.2808	3,726,443	952,774	0.0458	0.322	16,0559	0.0718	1.0124	6,867,290	5,159,496				
4	5,499,999	6,315,358	1.15	1,462,051	427,596	0.2088	4,037,947	887,950	0.0393	0.2392	16,1273	0.0693	1.1278	3,452,064	2,357,806				
5	5,500,000	3,586,533	0.65	1,785,345	533,392	0.2303	3,714,655	929,696	0.0397	0.266	14,6026	0.0791	1.1537	15,477,799	9,610,495				
6	5,500,000	2,599,697	0.47	2,570,586	823,796	0.2542	2,929,414	753,057	0.0361	0.2867	13,4667	0.0727	1.0313	20,814,587	11,749,292				
7	5,500,000	1,403,682	0.26	3,146,090	1,044,249	0.2634	2,353,910	553,530	0.0301	0.2905	11,1239	0.0848	1.0792	28,194,533	14,468,253				
8	5,499,999	1,557,531	0.28	4,021,808	1,109,667	0.2397	1,478,191	300,803	0.0186	0.2564	7,6091	0.0862	1.0487	23,064,615	10,759,813				
9	5,500,000	1,263,215	0.23	5,082,426	1,282,422	0.2367	417,573	85,504	0.0133	0.2487	5,3879	0.0827	1.031	21,474,074	9,107,104				
10	5,500,000	605,505	0.11	4,679,546	1,326,078	0.252	620,454	125,263	0.0133	0.2639	5,2266	0.0996	1.2105	27,995,708	10,793,557				
11	5,500,000	271,792	0.05	5,017,944	1,395,811	0.2582	482,056	88,229	0.0129	0.2698	5,0344	0.0848	1.3015	28,542,461	10,003,959				
12	2,969,102	34,036	0.01	2,916,661	803,531	0.2654	52,440	12,601	0.0105	0.2749	3,7942	0.0994	1.3529	17,194,580	5,724,357				
	57,462,571	48,143,878		34,171,168			23,291,400							179,842,160	77,981,787				



**Figure 1** Graphical presentation of the long-term dynamics of excavation by Scenario 1 – flotation processing

### 3.2 Scenario 2

According to the second Scenario, due to the above given facts and plans of RTB Bor Group – Copper Mine Bor, which owns the concerned mine, to increase the capacity of excavation at this site for the flotation

processing to 5,500,000 t, is the use of leaching method for processing of these amounts [7]. The oxide ore with oxide content of up to 10% during leaching was considered with the recovery coefficient of 0.7,

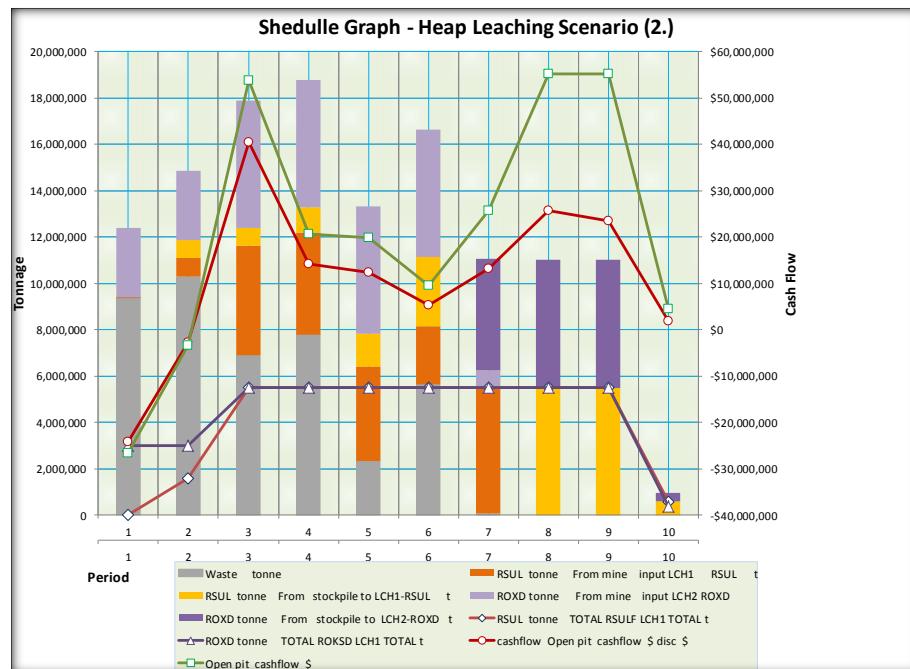
while leaching of sulphide ore was discussed with the recovery coefficient of 0.55 (Table 1.).

The input costs have also included the rehandling costs from the stock pile (0.2 \$/t

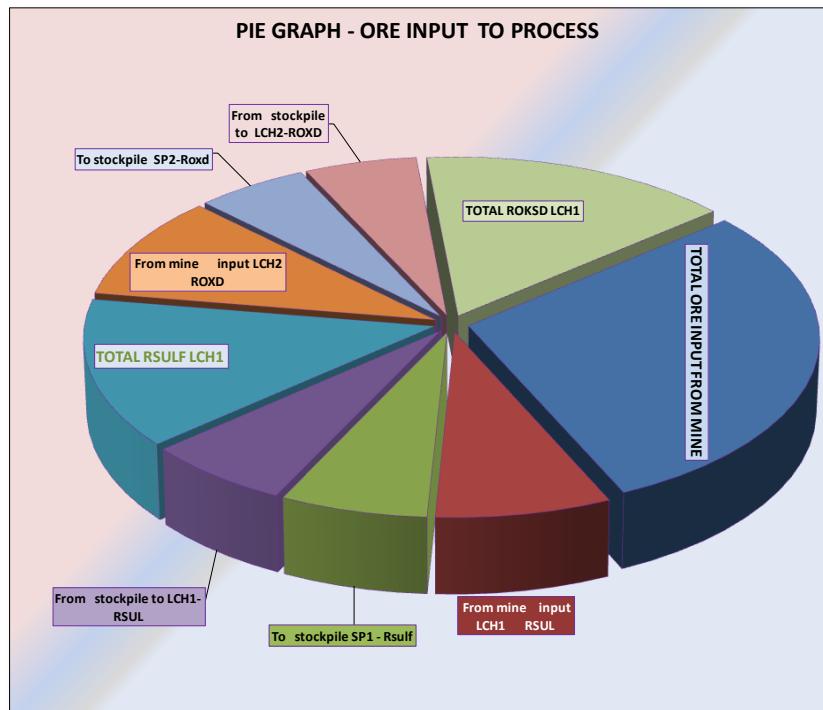
ore), and also the estimated investment costs of \$ 20,000,000 for the construction of infrastructure facilities and installations for hydrometallurgical processing method at the start of production (in the first year).

**Table 3** Long-term dynamics of excavation by Scenario 2, analyzed in the software Whittle Fx

Push backs: 19,26,36										Long Term Schedule -Method Heap Leaching									
Period	Input	tonne	Waste	Strip	Grade	Grade	Grade	RSUL tonne					ROXD tonne					cashflow	
								From mine	to	From	TOTAL	From mine	to	From	TOTAL	Open pit	Open pit	cashflow	cashflow
					CU	AU	AG	RSUL	SP1-Rsulf	LCH1	ROXD	SP2-Roxd	LCH2-ROXD	LCH1	\$	\$disc			
year	tonne	tonne	ratio		%	g/t	g/t	t	t	t	TOTALt	t	t	t	TOTALt	\$	\$		\$
1	7,637,874	9,362,127	1.23	0.1274	0.0329	0.6228	23,404	736,892	0	23,404	3,000,000	3,877,578	0	3,000,000	-26,688,274	-24,362,067			
2	6,729,443	10,270,557	1.53	0.2579	0.06	0.9707	839,606	747,903	736,892	1,576,498	3,000,000	2,141,934	0	3,000,000	-3,444,904	-2,847,028			
3	14,115,539	6,884,461	0.49	0.3268	0.0801	1.0017	4,755,886	2,835,617	744,314	5,500,000	5,500,000	1,024,236	0	5,500,000	53,795,117	40,417,819			
4	13,206,031	7,793,969	0.59	0.2378	0.071	1.0775	4,389,920	859,446	1,110,080	5,500,000	5,500,000	2,456,665	0	5,500,000	20,641,477	14,098,406			
5	18,683,273	2,316,727	0.12	0.2285	0.0724	0.9961	4,102,604	7,296,895	1,397,396	5,500,000	5,500,000	1,783,774	0	5,500,000	19,923,823	12,371,126			
6	15,363,156	5,636,844	0.37	0.19	0.0647	1.0937	2,494,353	2,731,602	3,005,647	5,500,000	5,500,000	4,637,201	0	5,500,000	9,514,108	5,370,466			
7	9,816,632	49,502	0.01	0.1982	0.0603	0.8397	5,500,000	3,365,802	0	5,500,000	695,769	255,061	4,804,231	5,500,000	25,672,382	13,73,991			
8	0	0	#DIV/0!	0	0	0	0	0	0	5,500,000	5,500,000	0	0	5,500,000	5,500,000	55,174,611	25,739,363		
9	0	0	#DIV/0!	0	0	0	0	0	0	5,500,000	5,500,000	0	0	5,500,000	5,500,000	55,174,611	23,399,421		
10	0	0	#DIV/0!	0	0	0	0	0	0	579,829	579,829	0	0	372,218	372,218	4,575,773	1,921,174		
	85,551,948	42,314,187	0.49				22,105,573	18,574,157	18,574,158	40,679,731	28,695,769	16,176,449	44,872,218	214,339,724	109,382,671				



**Figure 2** Graphical presentation of the long-term dynamics and cash flows per years by Scenario 2 – total conversion of flotation process by the leaching method



**Figure 3** Pie graph of sulphide and oxide ore participation in the leaching process

The obtained results by Scenario 2 are with the use of storage technology (stock pile), which serve as a buffer for the planned processing capacity, but also have the option of conducting the leaching time and shortening the period of total exploitation of the planned long-term dynamics. It is important to note that in recent years, when practically the excavation at the open pit was completed, the leaching time and leaching capacity can be adapted to the needs. Therefore, whether the ore from the stock pile will be processed for the time provided for the long-term plan or shorter, depending on the input of particle size distribution of ore, or from the surface of openness of mineral grains and thereby the leaching rate.

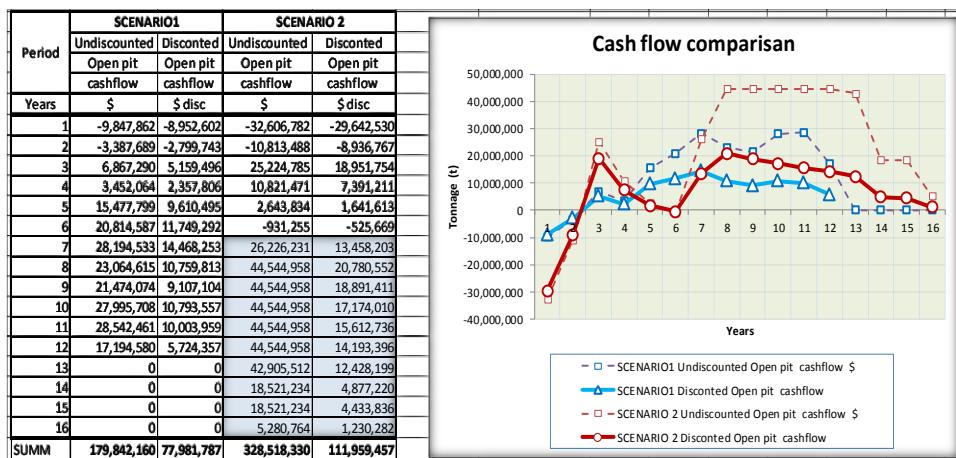
#### 4 CONCLUSION

It can be seen from the following Figure 3, Tables and Graphs of the comparative analysis results by Scenation 1 or Scenatio 2, as well as from Tables 2 and 3 and Graphs 1 and 2 that:

1. Calculated Cash flow by the second scenario is higher than by the first (by which any capital costs are not included for the capacity expansion);
2. That the exploitation period at the open pit (mining period) by the second scenario is almost half shorter than the first. The extended years of the second scenario is the processing of already excavated ore from the stock pile. It certainly brings savings that can be seen from the comparison with the economy by scenario 1;

- As it was noted in the previous section, the amount of excavated ore could be processed in a shorter time than it was presented in a long term scheduling increasing the time of leaching, i.e. with conducting the size of input ore to the leaching heaps or with selection the degree of crushing fragmentation;

Discounted cash flow in scenario 2 is higher, and among other things, as the leaching operation includes the overall mineralization within the open pit limits, without the use of cutoff grade as a boundary factor of ore and waste materials. Thus, the new processing process produces not only more high purity copper for human use, but also removes the uneconomic waste material from the environment.



**Figure 4 Comparative analysis of cash flow Graphics for a wide variety of scenarios, processing and extraction of metals from ore per years**

- Heap leaching process, which is in the case here, has much higher level of security in terms of environmental protection than the flotation process;
- Hydro-metallurgical method of copper extraction as opposed to the conventional pyro-metallurgical method eliminates SO<sub>2</sub> and other harmful impurities from the air in the area of the town of Bor, where the Smelting plant is located and its environment. In the considered case the recommendation is the SX/EW process instead of the current classic pyrometallurgy process. The SX/EW plant requires much less capital investments.
- Due to these facts and previous experience with accidental situations to the environmental protection, it is necessary to make an effort in the education of staff, as well as to introduce population with the bad and good aspects of this method for metal obtaining, also with a reduced risk of accidents.

## REFERENCES

- Z. Vaduvesković, N. Vušović, D. Kržanović: Analysis the Possibilities for Improvement the Economic Indicators for Exploitation the Deposit Cemantacija Kraku Bugaresku – Ore Field Cerovo, Mining and Metallurgy Engineering, Bor, 1(2014), 13-24.  
<http://www.irmbor.co.rs>

- [2] William H. Dreshe: How Hydrometallurgy and the SX/EW Process Made Copper the "Green" Metal, Copper Applications in Mining & Metallurgy <http://www.copper.org/publications/newsletters,innovations>, A copper Alliance member.
- [3] J. Peacey, GUO Xian-Jian, E. Robles: Copper Hydrometallurgy-Current Status, Preliminary Economics, Future Direction and Positioning Versus Smelting, Hatch Associates Ltd., 2800 Speakman Drive, Mississauga, Ontario L5K 2R7, Canada; Hatch Ingenieros Consultores Ltd., San Sebastian 283, Piso 9, Los Condes, Santiago 6760226, Chile.  
<http://www.d.wanfangdata.com.cn>
- [4] J. F. Lupo: Design and Operation of Heap Leach Pads by, Ph.D.Golder Asociates. The Jornal of the Soutern Institute of Mining and Metallurgy, Decembar, 2012, Vol. 112.  
[www.ausimm.com.au/co](http://www.ausimm.com.au/co)
- [5] Carlos Avendaño Varas: Review on Heap Leaching of Copper Ores, LX Users Conferencea Chile, La Serena, Junio 2004. Chemical Engenieer, Sociedad Terral S.A.
- [6] R. Denis, M. Marcotte:1,7 Million Square Meters PVC Heap Leach Pad Case History, Solmax International Inc., Varennes, Qc., Canada, Genivar, Montreal, Draft paper submitted for publication GeoAfrica 2009.
- [7] Phelps Dodge Morenci Has Converted All Copper Production to Mine-for-Leach, Copper Applications in Mining & MetallurgyBy William H. Dresher, Ph.D.,E.P.E.  
<http://www.copper.org/publications/newsletters,innovations>.
- [8] Whittle Strategic Mine Planning, Gemcom Whittle™ Copyright © 2012 Gemcom Software International Inc.
- [9] G. Hovanec, Review the Basic Economic Aspects of Copper Production by the Process of Acid Leaching, Research Associate for mineral processing materials in the Mining Institute, Belgrade.

Zoran Vaduvesković\*, Daniel Kržanović\*, Nenad Vušović\*\*

## KONVERZIJA FLOTACIJSKE PRERADE POSTUPKOM LUŽENJA NA GOMILI NA RUDNIKU CEMENTACIJA – KRAKU BUGARESKU U RUDNIKU BAKRA BOR\*\*\*

### Izvod

RTB Bor planira proširenje kapaciteta otkopavanja i prerade na ležištu Cementacija Kraku Bugaresku sa sadašnjih 2,5 miliona tona godišnje, na 5,5 miliona. Postojećom tehnologijom prerade, klasičnim flotiranjem celokupne otkopane rude, bez selektivnog otkopavanja i razdvajanja sulfidne od oksidne, zbog niskog iskorišćenja metala iz rude, postižu se skromni finansijski efekti. Rad razmatra kompletну konverziju sadašnjeg načina eksploracije, hidrometalurškim dobijanjem bakra luženjem na gomili i SX/EW metodom ekstrakcije iz lužnog rastvora, sa aspekta ekonomije, uporednom analizom novčanog i diskontovanog novčanog toka za oba slučaja (scenarija - sadašnji način flotiranjem i alternativni - luženjem). Analiza je urađena u softveru za strateško planiranje u rudarstvu-Whittle Fx, sa ulaznim tehnoekonomskim podacima za jedan i drugi slučaj [7].

Zbog učestalih havarija i izazivanja akcedentnih situacija na postojećim infrastrukturnim instalacijama postrojenja prerade, cevovodu za hidrotransport pulpe, u zaključku se ističu i komparativne prednosti hidrometalurške prerade ne samo sa aspekta ekonomije nego i zaštite životne sredine. U svetu, kod najvećih svetskih proizvođača bakra, tendencija je da se bakar učini pored skupocenog i "zelenim" metalom.

**Ključne reči:** luženje na gomili, hidrometalurgija, oksidna ruda, sulfidna ruda, dugoročna dinamika proizvodnje, novčani tok, diskontovani novčani tok

### 1. UVOD

Ležište Cementacija Kraku Bugaresku je započelo sa eksploracijom 1990. godine, investicionim radovima na raskrivanju ležištu, na lokaciji Cementacija 1. Sam naziv rudnog tela i kompleksa rudnih tela koji se sastoji od Cementacije 1, 2, 3 i 4, govori o prirodi ovih rudnih tela. Radi se o cementacionoj zoni sekundarnog obogaćenja, sa oko 40% oksidne rude, najviše na nivoima bližim površini, koja se relativno slabo flotira. Flotacijsko iskorišćenje bakra iz rude je,

pokazalo se u dosadašnjem radu, nivoa nešto većeg od 50%. Kombinacijom metoda prerade - flotiranjem sulfidne rude sa maksimalno 10% oksidne (smatra se da se pri tome ne utiče negativno na koeficijent iskorišćenja u flotaciji) postigli bi se znatno bolji ekonomski efekti [1], međutim problem je u mogućnostima selektivnog otkopavanja i izdvajajući pomenutih tipova rude – sulfidne i oksidne.

\* Institut za rudarstvo i metalurgiju Bor, Zeleni bulevar 35, Srbija

\*\* Tehnički fakultet Bor, Univerziteta u Beogradu, Vojske Jugoslavije 12, 19210 Bor, Srbija

\*\*\* Članak je u sklopu projekata tehnološkog razvoja TR 33038 "Usavršavanje tehnologija eksploracije i prerade rude bakra sa monitoringom životne i radne sredine u RTB Bor Grupa" i TR 34004 "Nova proizvodna linija za dobijanje bakra solventnom ekstrakcijom rudničkih voda", koji su finansirani od strane Ministarstva prosvete, nauke i tehnološkog razvoja Republike Srbije

## **2. OPIS PROBLEMATIKE**

Veliki problem je i što je na samom ležištu flotacijska prerada samo do nivoa dobijanja *pulpe*, tj. mlevenja i nakon toga zgušnjavanja, a zatim se hidrotransportom pulpa transportuje na dalju preradu u flotaciju Veliki Krivelj. Osim povećanih troškova flotiranja, ovakav način prerade je vrlo nepovoljan i sa aspekta zaštite životne sredine zbog čestih akcidenata na cevovodu i posledica po okolinu. (Poslednji takav desio se polovinom aprila 2014. godine).

Kao i prilikom otvaranja rudnika, na način i vrstu prerade veliki uticaj je imao lobi za "zaštitu životne sredine" Odluka o metodi prerade je tako donešena bez stručnih analiza, ne vodeći računa o prirodi ležišta (sadržaj preko 40% oksidne rude). Prema metodi luženja, ne samo zbog njenog eventualnog uticaja na životnu sredinu, ali bez detaljnog poznavanja ove problematike, stvoreni je animozitet čak zbog same pomene kiseline, odnosno cijanida koji su, po svojoj prirodi, otrovni. Tokom dosadašnje eksploatacije dela ležišta, pokazalo se da usvojena i primenjena metoda ne samo da ne daje dobre ekonomski efekte, nego je i veliki zagađivač okoline.

Jedan od primera totalne konverzije pirometalurškog procesa – flotacijske metode koncentracije i klasičnog topljenja koncentrata sa elektrolitičkom disocijacijom anode, hidrometalurškim procesom tj. luženjem na gomili u kombinaciji sa "*in situ*" luženjem potpomognutim bakterijskim luženjem, primenjen je na rudniku, *Morenci* kompanije *Phelps Dodge*, Arizona [7], početkom 2001. godine. Postojeći objekti za koncentraciju su stavljeni u stanje "*stand by*", dok je topionica prethodno izmeštena u mesto Chino, u Meksiku.

Osim ovog primera, gde se dnevno prerađuje o ko 75.000 t rude (oko 360.000 t bakra godišnje), primeri totalne konverzije pirometalurškog procesa su još u Cerro Verde (1993 - 15.000 t/d), Zaldivar (1992 - ~ 20.000 t/d) u Peru-u, i Kuebrada Blanca (1993 - 17.300 t/d) u Čileu, i mnogi drugi rudnici.

Koristi su višestruke, od značajne uštede energije, preko smanjenja ukupnih troškova proizvodnje po toni bakra, čija je čistoća 99,99%, do "čistog neba" odnosno zaštite životne sredine. To je takođe način da aktivnosti eksploracije i dobijanja bakra, iza sebe ostavljaju što manje otpada.

## **3. UPOREDNA ANALIZA EKONOMSKE EFIKASNOSTI KLASIČNE METODE I METODE LUŽENJA SA SX/EW NAČINOM EKSTRAKCIJE**

Analiza je sprovedena na bazi literaturnih tehnoekonomskih podataka za metodu "Heap Leaching" i hidrometalurški proces ekstrakcije SX/EW, ali imajući u vidu specifičnosti ležišta cementacija Kraku Bugaresku, kako sa aspekta mineralogije rude u ležištu i mogućnosti primene ove metode, tako i sa aspekta uporednih troškovnih podataka u odnosu na klasičan način prerade, za koji su korišćeni relevantni (poznati) podaci.

U sledećoj tabeli prikazani su tehnoekonomski podaci sa kojima je analiza urađena u softveru za strateško planiranje u rudarstvu, Whittle Fx, čiji je princip rada na osnovu Lerch Grosmann algoritma.

**Tabela 1.** Ulagani tehnoekonomski parametri eksploracije za proces optimizacije (in put)

Parametar	Jedinica	Vrednosti
Kapacitet otkopavanja - iskopine	t/god	12 Mt od 3. godine 17 Mt
Kapacitet flotacijske prerade - Sulfidna ruda sa max. 10% oksidne	t/god	2,5 Mt od 3. godine 5,5 Mt
Kapacitet luženja na gomili – Oksidna ruda sa preko 10% sadržajem oksida	t/god	2,5 Mt
Cena bakra	\$/tkatode	5,000.00
Cena zlata	\$/kg	40,000.00
Cena srebra	\$/kg	500.00
Troškovi otkopavanja	\$/t	2,3.
Troškovi flotacijske prerade	\$/t	4,00
Troškovi prerade luženjem na gomili	\$/t rude	1.00
Troškovi metalurške prerade bakra	\$/t katode	450.00
Troškovi metalurške prerade zlata	\$/kg	150.00
Troškovi metalurške prerade srebra	\$/kg	15.00
Troškovi hidrometalurške prerade (SXEW)	\$/t katode	100.0
Inicijalni kapitalni troškovi luženja i SXEW	\$	20,000,000
Ukupno iskorišćenje bakra (flot i metal)	%	0,788
Ukupno iskorišćenje zlata (flot i metal)	%	0,50
Iskorišćenje srebra (flot i metal)	%	0,40
Iskorišćenje bakra iz oksidne rude sa preko 10% sadržajem oksida	%	0,54
Iskorišćenje bakra luženjem iz sulfidnih ruda		0,55
Diskontna stopa	%	10.0

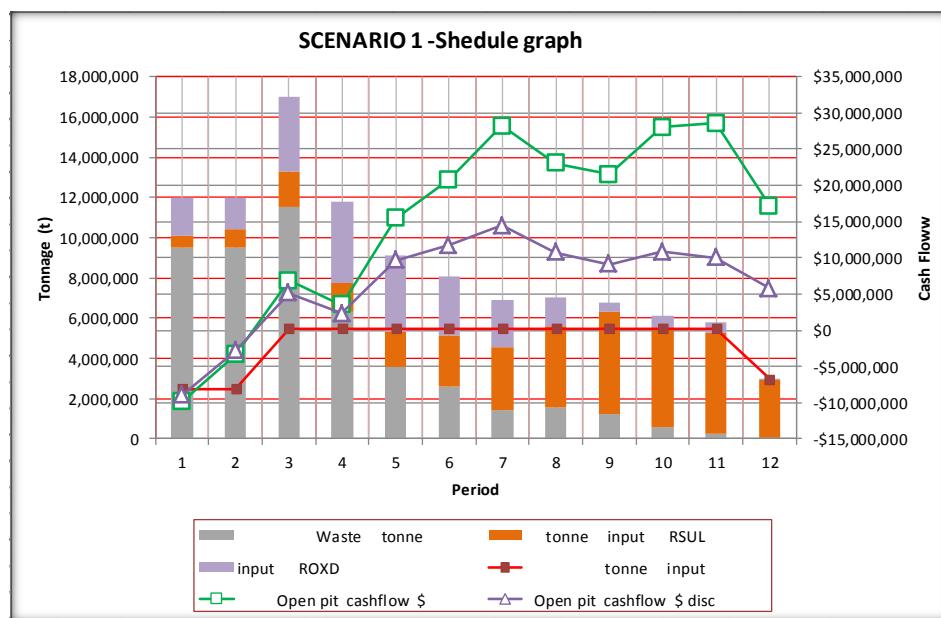
### 3.1. Scenario 1

Dobijeni rezultati po scenariju 1, odnosno postupkom kojim se sada vrši prerada, a to je da ukupna ruda ide na flotiranje, bez selektivnog otkopavanja i razdvajanja na dva tipa rude – sulfidnu i oksidnu. Za ove potrebe je modifikovan blok model i izvršeno razdvajanje pomenutih vrsta rude, kao tipova stena (Rock Types), samo teoretski zbog zahteva u softveru, ali suštinski celo-

kupna ruda ide na process flotiranja (MILL). U narednoj tabeli je prikazana dugoročna dinamika otkopavanja sa ekonomskim pokazateljima - novčanim tokom, nediskontovanim i diskontovanim. Analiza je urađena za ceo process prerade rude, kako flotacijskog, tako i metalurškog, sa prihodom od katodnog bakra i plemenitih metala.

**Tabela 2.** Dugoročna dinamika otkopavanja po scenariju 1, analizirana u softveru Whittle Fx

SCENARIO 1 - SCHEDULE GRAPPH																												
PB: 19, 26,3		Units																										
Period	input	tonne	Waste	Strip	input	RSUL	Grade	tonne	input	Grade	ROXD	input	CUOX	Grade	input	input	Grade	input	input	Open pit	cashflow	Open pit	cashflow					
																x 100		x 100										
1	2,497,779	9,502,221	3.8	601,834	241,726	0.2449	1,895,945	462,625	0.0413	0.282	15.4797	0.0753	1.1065	-9,847,862	\$	-8,952,602												
2	2,499,693	9,500,307	3.8	917,321	451,536	0.3076	1,582,372	426,201	0.0484	0.3511	15.7806	0.0802	1.0753	-3,387,689	\$	-2,799,743												
3	5,495,999	11,504,001	2.09	1,769,556	816,733	0.2808	3,726,443	952,774	0.0458	0.322	16.0559	0.0718	1.0124	6,867,290	\$	5,159,496												
4	5,499,999	6,315,358	1.15	1,462,051	427,596	0.2038	4,037,947	887,950	0.0393	0.2392	16.1273	0.0693	1.1278	3,452,064	\$	2,357,806												
5	5,500,000	3,586,533	0.65	1,785,345	533,392	0.2903	3,714,655	929,696	0.0397	0.266	14.6026	0.0791	1.1537	15,477,799	\$	9,610,495												
6	5,500,000	2,599,697	0.47	2,570,586	823,796	0.2542	2,929,414	753,057	0.061	0.2867	13.4667	0.0727	1.0313	20,814,587	\$	11,749,292												
7	5,500,000	1,403,682	0.26	3,146,090	1,044,249	0.2634	2,353,910	553,530	0.0301	0.2905	11.1239	0.0848	1.0792	28,194,533	\$	14,468,253												
8	5,499,999	1,557,531	0.28	4,021,808	1,109,667	0.2397	1,478,191	300,803	0.0186	0.2564	7,6091	0.0862	1.0487	23,064,615	\$	10,759,813												
9	5,500,000	1,263,215	0.23	5,082,426	1,282,422	0.2367	417,573	85,504	0.0133	0.2487	5,3879	0.0827	1.031	21,474,074	\$	9,107,104												
10	5,500,000	605,505	0.11	4,679,546	1,326,078	0.252	620,454	125,263	0.0133	0.2639	5,2266	0.0996	1.2105	27,995,708	\$	10,793,557												
11	5,500,000	271,792	0.05	5,017,944	1,395,811	0.2582	482,056	88,229	0.0129	0.2698	5,0344	0.0848	1.3015	28,542,461	\$	10,003,959												
12	2,969,102	34,036	0.01	2,916,661	803,531	0.2654	52,440	12,601	0.0105	0.2749	3,7942	0.0994	1.3529	17,194,580	\$	5,724,357												
	57,462,571	48,143,878		34,171,168			23,291,400										179,842,160	\$	77,981,787									



**Sl. 1.** Grafički prikaz dugoročne dinamike otkopavanja po Scenaruju 1 – flotacija prerada

### 3.2. Scenario 2

Prema drugom scenaruju, zbog navedenih činjenica i planova RTB Bor Grupe – Rudnika Bakra Bor u čijem je vlasništvu predmetni rudnik, o povećanju kapaciteta otkopavanja na ovom lokalitetu za flota-

cjsku preradu na 5.500.000 t, jeste da se te količine prerade luženjem [7]. Oksidna ruda sa sadržajem oksida do 10% prilikom luženja razmatrana je sa jednim koeficijentom iskorišćenja (0,7), dok je luženje sulfidne

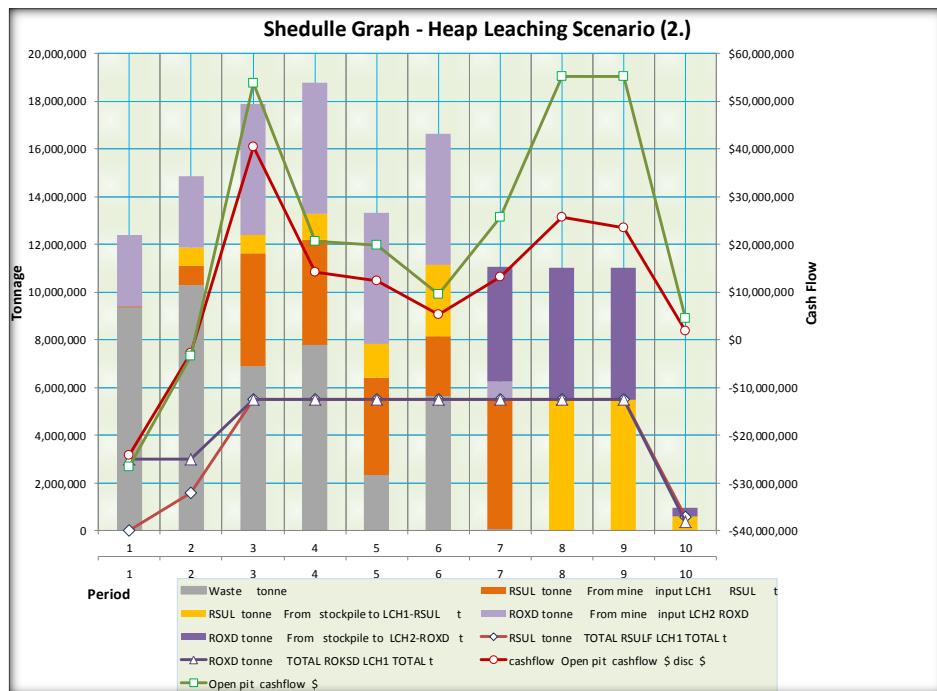
rude razmatrano sa koeficijentom iskorišćenja od 0,55 (Tabela 1.).

U ulazne troškove uračunati su i *re-handling* troškovi sa skladišta (0,2 \$/t rude), a uzeti su u obzir i procenjeni

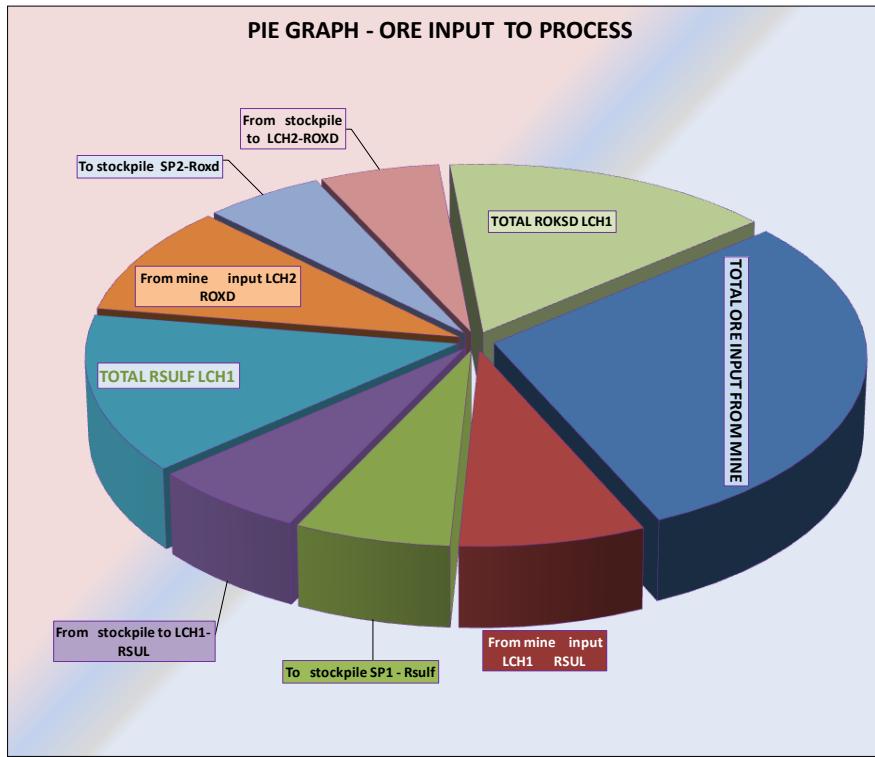
investicioni troškovi od 20.000.000 \$ za izgradnju infrastrukturnih objekata i instalacija za hidrometaluršku metodu prerade, i to na samom startu proizvodnje (u prvoj godini).

**Tabela 3.** Dugoročna dinamika otkopavanja po scenariju 2, analizirana u softveru Whittle Fx

Push backs: 19, 26, 36			Long Term Schedule -Method Heap Leaching														
Period				RSUL tonne						ROXD tonne						cashflow	
	tonne	Waste	Strip	Grade	Grade	Grade	From mine	to	From	TOTAL	From mine	to	From	TOTAL	Open pit	Open pit	
	input	tonne	ratio	CU	AU	AG	input LCH1	stockpile	stockpile to	RSUL	input LCH1	stockpile	stockpile to	ROXD	cashflow	cashflow	
year	tonne	tonne	ratio	%	g/t	g/t	t	t	t	TOTAL t	t	t	t	TOTAL t	\$	\$	
1	7,637,674	9,362,127	1.23	0.1274	0.0329	0.6228	23,404	736,892	0	23,404	3,000,000	3,877,578	0	3,000,000	-26,688,274	-24,262,067	
2	6,729,443	10,270,557	1.53	0.2579	0.06	0.9707	839,606	747,903	736,892	1,576,498	3,000,000	2,141,934	0	3,000,000	-3,444,904	-2,847,028	
3	14,115,539	6,884,461	0.49	0.3268	0.0801	1.0017	4,755,686	2,835,617	744,314	5,500,000	5,500,000	1,024,236	0	5,500,000	53,796,117	40,417,819	
4	13,206,031	7,793,959	0.59	0.2378	0.071	1.075	4,389,920	859,446	1,110,080	5,500,000	5,500,000	2,456,665	0	5,500,000	20,641,477	14,998,406	
5	18,683,273	2,316,727	0.12	0.2285	0.0724	0.9961	4,102,604	7,296,855	1,397,396	5,500,000	5,500,000	1,783,774	0	5,500,000	19,923,823	12,371,126	
6	15,363,156	5,636,844	0.37	0.19	0.0647	1.0937	2,494,353	2,731,602	3,005,647	5,500,000	5,500,000	4,637,201	0	5,500,000	9,514,108	5,370,466	
7	9,816,632	49,302	0.01	0.1982	0.0603	0.8397	5,500,000	3,365,802	0	5,500,000	695,769	255,061	4,804,231	5,500,000	25,672,382	13,173,991	
8	0	0	#DIV/0!	0	0	0	0	0	0	5,500,000	5,500,000	0	0	5,500,000	5,500,000	55,174,611	25,739,363
9	0	0	#DIV/0!	0	0	0	0	0	0	5,500,000	5,500,000	0	0	5,500,000	5,500,000	55,174,611	23,399,421
10	0	0	#DIV/0!	0	0	0	0	0	0	578,829	579,829	0	0	372,218	372,218	4,575,773	1,921,174
	85,551,948	42,314,187	0.49				22,105,573	18,574,157	18,574,158	40,679,731	28,695,769	16,176,449	16,176,449	44,872,219	214,339,724	109,382,671	



**Sl. 2.** Grafik dugoročne dinamike i novčanih tokova po godinama po Scenariju 2. - totalna konverzija flotiranja metodom luženja



Sl. 3. Pie grafik učešća sulfidne i oksidne rude rude u procesu luženja

## ZAKLJUČAK

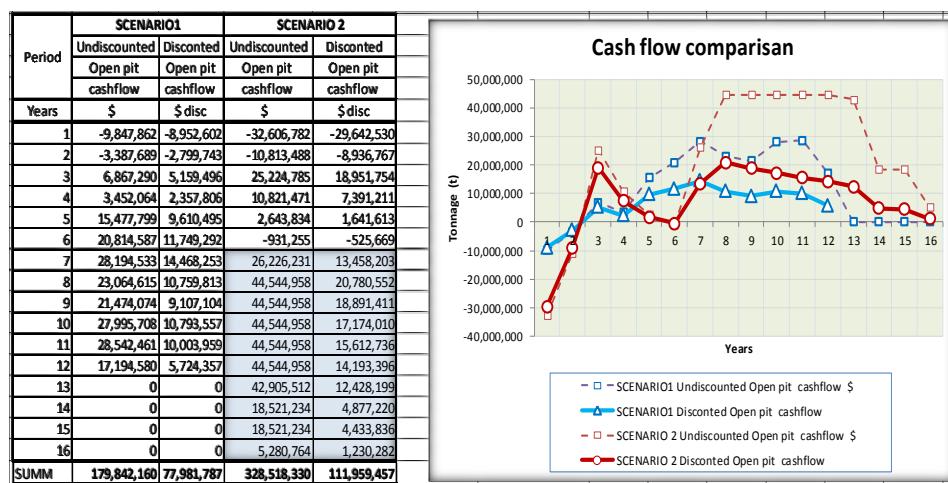
Dobijeni rezultati po Scenariju 2 su sa tehnologijom korišćenja skladišta (Stock pile), koji služe kao bafer za planirani kapacitet prerade, ali stoji i mogućnost dirigovanja vremenom luženja i skraćenjem perioda ukupne eksploatacije predviđenog dugoročnom dinamikom. Bitno je napomenuti i da se u poslednjim godinama, kada je praktično otkopavanje na kopu završeno može vreme luženja, time i kapacitet luženja prilagoditi potrebama. Dakle, da li će se ruda sa skladišta prerađivati za vreme predviđeno dugoročnim planom ili kraće, zavisi od ulaznog granulometrijskog sastava rude, odnosno od površine otvorenosti mineralnih zrna i time brzine izluživanja.

Na sledećoj slici 4 – *Tabela i dijagram uporednih rezultata analize po jednom i drugom scenaruju*, kao i iz Tabela 2 i 3, odnosno grafičkih slika 1 i 2, vidi se:

1. Sračunati Cash flow po drugom scenaruju je veći nego po prvom (po kome nisu uračunati nikakvi investicijski troškovi za povećanje kapaciteta);
2. Da je vek eksploatacije na kopu (otkopavanja) po drugom scenaruju upola kraći nego po prvom. Preostalih godina po drugom scenaruju je prerada sa već otkopanom rudom – rudom sa skladišta. To svakako donosi uštede koje se vide iz upoređenja sa ekonomijom po scenaruju 1.

- Kao sto je u prethodnom poglavlju napomenuto, otkopana ruda se može preraditi i ukraćem vremenu nego što je predstavljeno u dugo-ročnoj dinamici, smanjujući potrebo vreme izluživanja po osnovu veličine ulazne granulacije rudena gomile za luženje, odnosno izborom stepena drobljenja;

Diskontovani novčani tok po scenariju 2. je veći pored ostalog, izbog toga što se procesom luženja zahvata celokupna mineralizacija u granicama kopa, bez korišćenja graničnog sadržaja kao faktora razgraničenja rude i jalovine. Dakle, novi proces prerade stvara ne samo više bakra visoke čistoće za ljudsku upotrebu, već takođe uklanja neekonomični otpad iz životne sredine.



**Sl. 4. Grafik uporedne analize novčanih tokova za različite scenarije prerade i ekstrakcije metala iz rude, po godinama**

- Proces luženja na gomili, o kome se ovde radi, je sa mnogo većim stepenom sigurnosti sa aspekta zaštite životne sredine nego što je process flotiranja;
- Prerada ove rude za razliku od klasične prerade topljenjem, eliminiše SO<sub>2</sub> i druge štetne primese iz vazduha na području topionice, odnosno grada Bora i okoline. Ovde se umešto klasičnog pirometaluršog procesa, primenjuje SX/EW process. Postrojenje zahteva mnogo i manja kapitalna ulaganja.
- Zbog navedenih činjenica, i dosadašnjih iskustava saakcedentnim situacijama po zaštitu životne sredine,

potrebitno je uložiti napor kako u edukaciju kadrova, tako i u upoznavanje stanovništva sa lošim i dobrim stranama ovakve metode dobijanja metala, takođe sa smanjenim rizikom od akcidenta.

## LITERATURA

- Z. Vaduvesković, N. Vušović, D. Kržanović: Analiza mogućnosti poboljšanja ekonomskih pokazatelja eksploracije ležišta Cementacija Kraku Bugaresku-rudno polje Cerovo, Mining and Metallurgy Engineering Bor, 1/2014, str. 25-36, <http://www.irmbor.co.rs>

- [2] William H. Dresher: How Hydrometallurgy and the SX/EW Process Made Copper the "Green" Metal, Copper Applications in Mining & Metallurgy [http://www.copper.org/publications/newsletters\\_innovations](http://www.copper.org/publications/newsletters_innovations), A copper Alliance member
- [3] J. Peacey, GUO Xian-Jian, E. Robles: Copper hydrometallurgy-currentstatus, preliminary economics, future direction and positioning versus smelting. Hatch Associates Ltd., 2800 Speakman Drive, Mississauga, Ontario L5K 2R7, Canada; 2Hatch Ingenieros Consultores Ltda., San Sebastian 283, Piso 9, Los Condes, Santiago 6760226, Chile.  
<http://www.d.wanfangdata.com.cn>
- [4] J. F. Lupo: Design and Operation of Heap Leach Pads, By Ph.D. Golder Asociates. The Jornal of The Soutern Institute of Mining and Metallurgy, Decembar, 2012. Vol. 112.
- [5] Carlos Avendaño Varas: Review on heap leaching of copper ores, LX Users Conferencea Chile, La Serena, Junio 2004., Sociedad Terral S.A
- [6] R. Denis, M. Marcotte: 1,7 Million Square Meters PVC Heap Leach Pad Case History, Solmax International Inc., Varennes, Qc., Canada, Genivar, Montreal, Qc., Canada, Draft paper submitted for publication GeoAfrica 2009;
- [7] William H. Dresher: Phelps Dodge Morenci Has Converted All Copper Production to Mine-for-Leach, Copper Applications in Mining & Metallurgy, [http://www.copper.org/publications/newsletters\\_innovations](http://www.copper.org/publications/newsletters_innovations)
- [8] Whittle Strategic Mine Planning, Gemcom Whittle™ Copyright © 2012 Gemcom Software International Inc.
- [9] G. Hovanec: Osrvt na osnovne ekonomiske aspekte proizvodnje bakra primenom postupka kiselinskog lženja, Rudarski institut Beograd.

Dragan Zlatanović \*, Vladimir Milisavljević \*\*, Milenko Ljubojev \*\*\*,  
Dragan Ignjatovic \*\*\*\*

## FORECAST THE BEHAVIOUR OF ROCK MASS BEFORE TAKING UP THE EXCAVATION AT DEEPER LAYERS OF THE ORE BODY BORSKA REKA \*\*\*\*

### Abstract

This paper presents one possible approach for resolving some important issues related to the stability of underground rock structures at higher depths. The analysis is focused on forecast the behavior of rock mass before performing the mining excavation at deeper levels of the ore body "Borska Reka".

Regardless of extensive previous research of the ore body "Borska reka" and necessary parameters obtained for modeling of stress and strain that occur under the influence of mining excavation, additionally the estimation state of stress in the rock massif is also done. The stability analysis is shown for the roadway at the level XVII and forecast their stability for deeper level. As the result, it is expected that the level of uncertainty and risk associated with many identified geomechanical risks with management of rock massif will be reduced.

**Keywords:** forecast, behaviour of rock mass, roadway stability, ore body Borska reka

### INTRODUCTION

The mining works and roadways construction in deep mines causes instability which may occur as the result of roof falls, wall failures or combination of both. Thus, in order to safety come first when performing the mining operations, the stability of such roadways is very important. The prime concern in excavations is the control of displacements in the rock surrounding the excavation. In each excavation, the design objective is to ensure that displacements of

the rock do not interfere with the specified engineering activities.

Computer modeling for strata control in rock mechanics has significantly developed in recent years. There are various numerical methods and codes available for stability analysis of underground openings. Despite the significant advances that have been made, it must be recognized that the successful application of numerical methods in rock engineering design analyses depends to a

\* University of Belgrade - Faculty of Mechanical Engineering – Innovation Centre, Kraljice Marije 16, Belgrade, e-mail: dr.dragan.zlatanovic@gmail.com

\*\* University of Belgrade - Faculty of Mining and Geology, Djušina 7, Beograd, e-mail: vladimir.milisavljevic@rgf.bg.ac.rs

\*\*\* Mining and Metallurgy Institute Bor, Zeleni bulevar 35, Bor, e-mail: milenko.ljubojev@irmbor.co.rs, dragan.ignjatovic@irmbor.co.rs

\*\*\*\* This work is the result of the Project 33021 "Investigation and Monitoring the Changes of Stress-strain State in the Rock Mass "In-situ" around the Underground Rooms with Development a Model with Special Reference on the Tunel of the Kriveli River and Jama Bor", funded by the Ministry of Education, Science and Technological Development of the Republic of Serbia.

great extent on geomechanical models and boundary conditions developed from the site characterization data. Due to a difficulty in defining some of the input data, the deterministically, probabilistic or stochastic methods are often used to represent mechanical properties of rocks and rock masses, and in the analyses themselves.

Underground mine design requires an iterative process which is often approached in different ways. Initially, the possible mining methods are selected, likely production capacities determined and indicative cut-offs derived. Preferred mining methods are selected followed by more refined ore definition. The primary infrastructure options are then established and the analysis taken through to the global extraction sequencing. Much evaluation has to be done before design commences.

When the primary infrastructures - roadways have to be designed, one of the first questions often put to the rock mechanic & mining engineers is "What is the maximum stable opening?" However, it is often too early and there is rarely anything like enough data available on which to base an informed decision.

Serious consideration of geomechanics problems, associated with deep and high stress mining, began before the advent of modern high-speed digital computers and numerical modelling methods.

In this computer era, a wide range of computer software has been used in numerical analyses of the rock mass behavior. They include the range of displacement discontinuity and related programs, as well as **FEM**<sup>\*</sup> (**Phase2**), **BEM**<sup>†</sup>, **FDM**<sup>‡</sup> and **DEM**<sup>§</sup> codes. [1]

Despite the availability of computer techniques and software and applicable engineering procedures, the geomechanical analysis is even more of an art than real modelling of rock mass.

Obviously, it will never be possible to do enough geomechanical exploration to enable geomechanics risks of this wide range of types to be fully accounted in the planning stages of mining project. However, as the project proceeds through the various stages from concept to detailed design and implementation, the level of uncertainty and risk associated with many sources of geomechanics risk identified previously can be expected to be reduced.

### Applicability of standard strength criteria

Most of numerical analyses, currently used for evaluation the stability of underground excavations, are based on the linear Mohr-Coulomb strength criterion. However, the experimental data and experience of the field engineering showed that the strength of nearly all types of rock mass is followed by the non-linear Hoek-Brown strength criterion. The Hoek-Brown strength criterion for rock mass is widely accepted and applied in a large number of engineering in the world.

The classic Mohr-Coulomb strength criterion consisting of two independent cohesive and frictional components does not provide a realistic representation of progressive fracture and breakdown of rock under stress. The Hoek-Brown criterion is widely applied to jointed rock masses, but may also be applied to intact rock. In fact, much more data

---

<sup>\*</sup> Finite Element (**FEM**) and related methods  
(Beck et al., 2009, 2010; Goodman et al., 1968; Wittke, 1977, 1990; Zienkiewicz, 1977)

<sup>†</sup> Boundary Element Methods (**BEM**) (Beer and Watson, 1992; Brady, 1979, 1987; Crouch and Starfield, 1983)

<sup>‡</sup> Finite Difference Methods (**FDM**) (Hart et al., 2008; Itasca, 2011; Sainsbury et al., 2011)

<sup>§</sup> Discrete Element Methods (**DEM**) (Jing and Stephansson, 2007)

for intact rock than for rock masses were used in its original development by Hoek and Brown (1980) and later. [2]

### CASE STUDY OF ORE DEPOSIT “BORSKA REKA”

For purposes of this paper, this analysis will be mainly focused on forecast the behaviour of rock mass in particular case of ore deposit (body) “Borska Reka” in the underground mine “Jama” in Bor.

This deposit has a length of about 1,000 m and a thickness about 500 m, dipping to the west at an angle of 45° to 55°, according with dipping of Bor conglomerates and sandstones, and it is separated by the Bor fault from hydrothermal zone. Exploration works on the ore body "Borska Reka" deposit have been carried out in the period from 1976 until these days with a large volume of research works. Detailed exploration works were carried out to the level -155 m and it is assumed that the deposit is dipping to elevate at the level of -800 m and even deeper. Part of the deposit above the XIX level K-235, is opened by the transport system for the ore bodies "Tilva Roš" and "P2A".

Mining operations are carried out on the basis of mining project for exploitation of copper ore above the XIX level (K-235). After many years of determination the mineral reserves in the ore body “Borska Reka”, additional explorations and prepared documentations, this ore body is still waiting for exploitation. There are plans to increase the mine production using mining excavation methods with preserving the surface and all constructed facilities, infrastructures and mining works above the ore deposit "Borska Reka", starting with excavation from the

level XIX. The deeper layers will be considered for exploitation in the further steps.

This is certainly a serious challenge in managing the rock massif and geomechanical risks. Therefore, the results of this analysis, on one hand, referred to the need for forecasts the behavior of rock mass before taking up the excavation at deeper layer, and on the other hand, the excavation of deeper layer of the ore body “Borska Reka” requests to carry out all necessary geomechanical testings in order to obtain reliable information as a basis for decision-making.

### PREVIOUS EXPLORATIONS AND MODELING OF STRESS-STRAIN STATE

#### Previous explorations

In order to determine the geomechanical characteristics of working environment, the current technical documentations of geological, geotechnical and hydrogeological investigations and design analysis were reviewed concerning the ore body "Borska Reka" in the underground mine "Jama" Bor. Based on this, it can be generally concluded that much was done and a lot of work and effort and money were invested.

Here, some of the years will only be mentioned when the subject explorations were carried out starting from 1997, 1999, 2007 and 2014 by the Mining and Metallurgy Institute Bor. [3]

So far, according to the carried out analyses within the latest explorations, it was found out that the data show partially lower values of physical and mechanical properties of rock in relation to the previous explorations, Table 1.

**Table 1** Physical-mechanical parameters obtained by laboratory tests on samples of rock mass from the ore body “Borska reka“

Geotechnical environment	$\gamma$ [kN/m <sup>3</sup> ]	$\sigma_c$ [MPa]	$\sigma_i$ [MPa]	$E_t$ [MPa]	$E_s$ [MPa]	$\nu$ -	$\phi$ [°]	$m_i$ -	C [MPa]	RMR <sub>89</sub>	GSI
Pelytes *2014	25.4	49	4.95	5600	3730	0.34	36.0	24	12.13	54	
Andesites *2014	25.9	52	5.37	6927	4633	0.31	36.8	26	12.90	66	
Kaolinized Andesites *2014	27.0	25	3.04	5490	3672	0.37	30.4	20	7.53	34	
Silicified Andesites *2014	27.7	67	7.57	10790	7127	0.32	37.4	28	16.70	51	
(level XVII) K-155	$\gamma$ [kN/m <sup>3</sup> ]	$\sigma_c$ [MPa]	$\sigma_i$ [MPa]	E [MPa]	Ed [MPa]	$\nu$ -	$\phi$ [°]	$m_i$ -	C [MPa]	RMR <sub>89</sub>	GSI
Silicified Andesites *1999	28.2	63.39	6.71	40490	33255	0.216	41.6	15.09	18.9	73	65

### Modeling of stress-strain state

Apart from the standard laboratory tests and “in situ” observations and measurements, the laboratory test procedures were carried out for testing the strength parameters and deformable characteristics of working environment using the triaxial compression. Triaxial experiment is aimed to simulate the conditions that may occur in the rocks surrounding the underground infrastructures – roadways and facilities and these openings could be exposed to the limit pressure and shearing stress. [4]

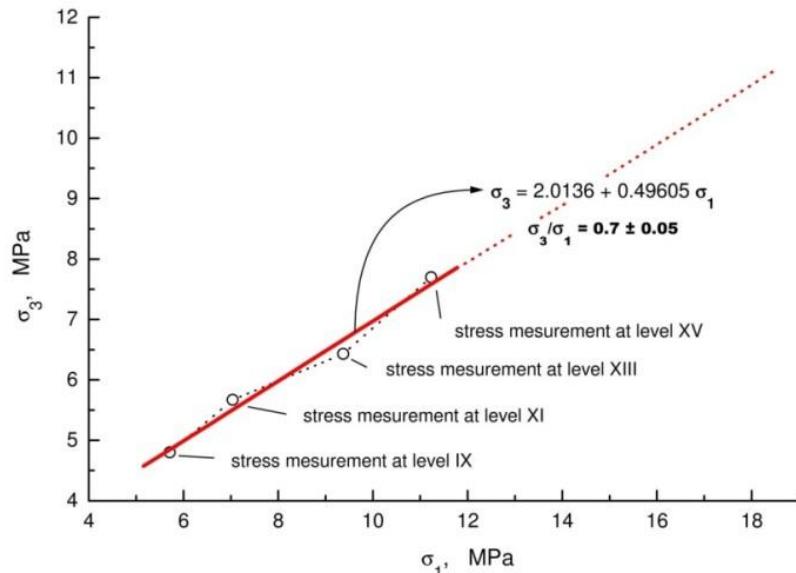
Based on the previous results of conducted laboratory tests on samples of rock massif and core from exploration drill holes, with taking into account the state of rock massif, degree of representativeness of samples, effect of samples size, mechanical strength, deformation characteristics and quality assessment of rock mass, the laboratory values are obtained for parameters of rock mass at the level XVII in the ore body “Borska Reka“. [5]

The rock stability analysis was carried out on a standard cross-section of roadway which is designed and constructed in the underground mine “Jama” Bor (4x3.5m), with a scope of confirmation the relevance of data collected from previous explorations and studies mentioned above.

State of stress in the ore body “Borska Reka” is not measured previously, therefore this data was not available. Due to the lack of knowledge on the stress state of rock massif, the field of stress will be defined through the gravitational component -  $\gamma H$ . Stress was measured in the nearest ore body “Tilva Ros” and given the proximity indicating on relations between the principal stresses (Fig. 1). The ratio is between  $0.7 \pm 0.05$ . This assessment could be also accepted for the ore body “Borska Reka” and XVII level (K -155). [6]

It should be noted that the stress measurements were made more than twenty years ago and only on the roadway contour. It can be assumed that the actual values are higher if the stress was measured deeper into the rock massif. That means the shortage of precise stress values for a specific level of depth in the ore body “Borska Reka” indicate the first problem in accuracy of executed certain calculations and conclusions.

Instead of qualitative rock mass stability analysis, the empirical analysis can be performed based on estimations and assumptions in order to meet the required range of values, but it may be wrong in that required range. [7]



**Figure 1** Linear function of stress measured variations by depth of principal stresses for the ore body "Tilva Ros" in the underground mine "Jama" Bor

Determined value of stresses taken from the (Fig. 1) for level XVII is for  $\sigma_1 = \sigma_v = 14$  MPa, and for  $\sigma_3 = 9.5$  MPa.

### Model design

Boundary conditions are defined so that the stress on model will be only under the influence of gravitational component, and the model external boundary is fixed so it cannot move in the X and Y axis direction.

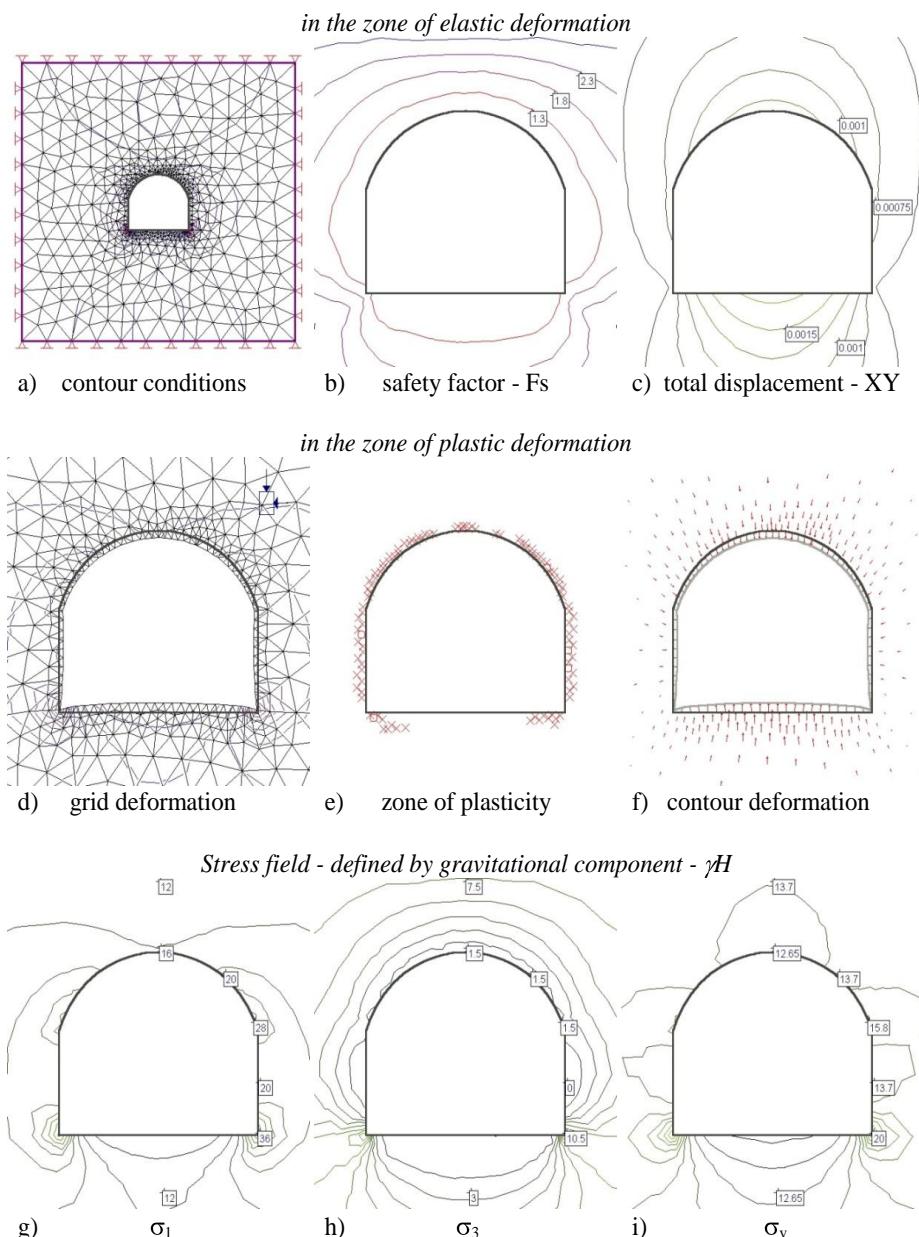
The required density of points (nodes) of which depends the number of finite elements density is determined by the model discretization. A density of 75 points (nodes) on contour profile was chosen in this case. This can show what extent the density of finite element affects the accuracy of results and the interpolation accuracy, i.e. drawing the contours of stress and strain. The finite element grid is composed of triangles and

is shown in any figure of result interpretation.

### Result interpretation and stability assessment

For designed roadway cross section modeling, the finite element mesh is generated with total of 1404 elements and 729 nodes. Data entry for each case only differs in direction of principal stresses. Interpretation of results and stability assessment is given for both defined cases. Calculation results are interpreted with contour lines of safety factor, total displacement and principal stress. Deformation grid is also presented, deformation on model contour lines with the direction of displacement (which is magnified 100 times) as well as the plasticity zone marked with markers. Markers in the form of crosses (x) mark fracture occur due to shear stress, and in the form of circles (o) mark fracture caused by tension stress. (Fig. 2).

*Designed - constructed object (roadway) on the level XVII - 4x3.5 m*



**Figure 2** Stress-strain analyses in case the stress field under the influence of gravitational component -  $\gamma H$

If the rock mass around given premises located in the zone of elastic deformation, so long that zone will be stable to the apportionment factors of safety as it is shown in Fig. 2b. Contour line of the safety factor of 1.3 meets the set criterion of stability. But it is seen that the sides of roadway that line is further from the contours and that consequently this area becomes susceptible to transition from the elastic zones into the zone of plastic deformation. The total displacement along the contour is 1.8 mm (Fig. 2c).

In the parts around the roadway cross section with plastic deformation (Fig. 2e), the plastic zone due to shear stress ( $x$ ) will occur in the roadway arch, and the complex plastic zone due to shear and tension stress ( $x$  and  $o$ ) occurs on the sides of roadway.

It can be concluded that in this case the roadway is stable. However, the appearance of plastic deformation, which is manifested as a sporadic rock fragmentation in the form of flaking and falling down of small pieces, could be appropriately protected with the same roof support system to secure the site from future spread of damage. [8]

#### **FORECAST THE BEHAVIOUR OF ROCK MASS**

To take an advantage of modeling research which allows forecasting the be-

haviour of rock mass before taking up the excavation at deeper layers, the stability analysis of deeper levels of the level XVII will be used in this section.

Depth selection was taken at the level of XIX (K -235), XXI (K -315), XXIII (K -395) and XXV (K -475) and they represent a depth value of about 630 m, 710 m, 790 m and 870 m under surface.

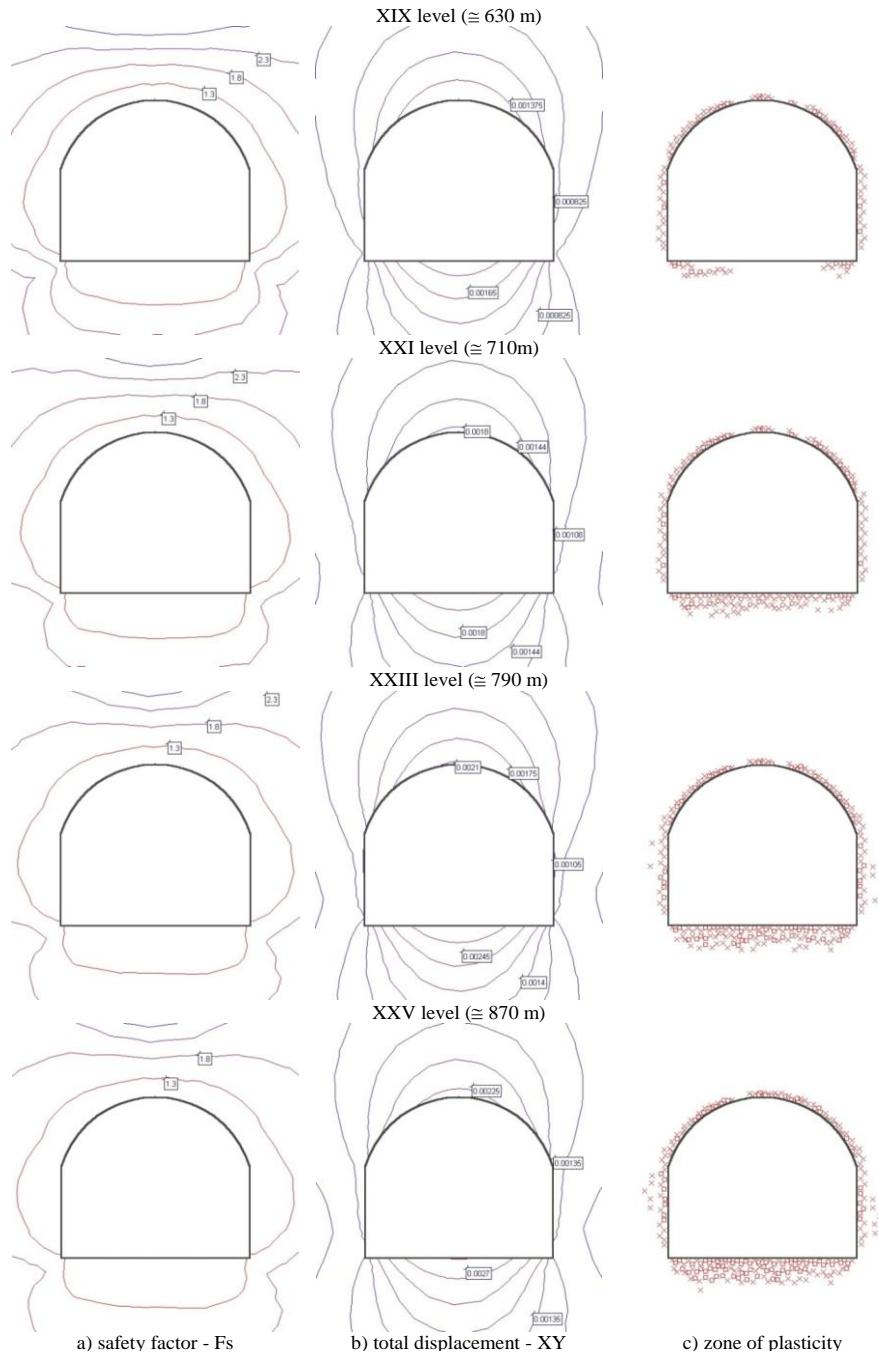
Based on that, it can be said that the chosen levels for stability analyses, XVII and XIX level are included in the new mine design. It can be useful, because the newly constructed facilities at the levels, with the appropriate observations can be useful to demonstrate the validity of this stability analysis assessment. Other three levels are analyzed in order to predict what can be expected at deeper levels at a later stage and will be the subject of further elaboration. [9]

Interpretation of stability assessment results are done as well as stability analysis for level XVII and it might be easier to compare the results.

The values of the principal stress were obtained on the basis of the gravity component  $\sigma_r = \gamma H$ , and the ratio of principal stresses  $\sigma_1$  and  $\sigma_3$  obtained from the analytical equation from the graph in Figure 1.

**Table 2** Prognostic value of the principal streses for selected depth

Level	Ground level	Depth m	$\gamma H$ MPa	$\sigma_1$ MPa	$\sigma_3$ MPa	$\sigma_3/\sigma_1$
XVII	-155	550	14	14	9.5	0.70±0.05
XIX	-235	630	17	17	10.5	0.65±0.05
XXI	-315	710	19.2	19.2	11.5	0.60±0.05
XXIII	-395	790	21.3	21.3	12.6	0.55±0.05
XXV	-475	870	23.5	23.5	13.5	0.55±0.05



**Figure 3** Stress-strain analyses for deeper levels in case the stress field under the influence of gravitational component -  $\gamma H$

## **Forecast the stability model at depth below the level XVII**

The results of model analysis are made for the stress field determined by the gravitational component -  $\gamma H$ . The finite element grid is used for modeling as in the previous analysis.

To define rock mass parameters for the analysis, the fracture criterion and parameters of the rock mass obtained from the parameters at the XVII level were used. It was necessary to simulate those depths for assessment the stability by increase the lateral sample using the triaxial tests, which determined the deformable characteristics of the rock mass at the level XVII. These tests were not carried out and deformable characteristics of the rock mass at the XVII level were used for these analyses.

The stress-strain analysis of rock mass at the levels XIX, XXI, XXII and XXV are shown in Figure 3.

Looking at the results of stability analysis by levels, it can be concluded that the stability of the roadway decreases linearly with increasing depth and it was expected.

Considering that maximum displacements on the model grow with the increase of depth as 2.1 mm, 2.4 mm, 2.76 mm and 3.2 mm, the rock fragmentation and rock deterioration can be expected for deeper levels than the level XXI.

The places with occurrence of plastic deformation, plastic zone on roadway will have such a character that on the roof appear the plastic zone (x), and on the sides appear plastic zone (x and o). This could be applies only for the level XIX while the deeper levels it should be expected plastic zones (x and o) all over the roadway. The size of the plastic zone influence is in the range of 18 cm, 21 cm, 28 cm and 35 cm. In the roof their value is 16 cm, 17 cm, 18 cm and 20 cm, while on the floor only the level XIX deployed in the corners and on the other levels is distributed all over the floor.

In this case of principal stress appointed, contour line of the safety factor on the side of roadway is increasingly moving away from the side. Base on that risk the stability increased due to the stress from the side of the roadway. [10]

It can be estimated that at the level XIX this roadway can stay unsupported, except on places with the plastic zone appearance and the support must be installed in these places. Forecast the stability for the same roadway at the levels XXI, XXIII and XXV indicates that it must have the adequate roof supports in some sections or on the entire length. As the result of increasing, the depth may notice a certain "calming" in plastic zone increasing around the cross-section. That requires redefining the boundary conditions on the model and estimated or measured new value of the principal stresses and their direction.

In the areas of plastic zone, the rock fragmentation is mainly induced by extensive deformation. Deformation starts immediately after excavation, and it is commonly stabilized with reaction of the installed support, reaching the equilibrium of forces, but it could be transformed into deterioration as the result of rheological behaviors of rock mass.

Rock deterioration in proximity of underground openings – roadways might occur for several reasons. The major cause is a stress concentration in immediate roof and floor rocks, as well as in sides. This concentration is generated by the initial equilibrium disturbance following the roadway development, resulting in concentration of vertical stress in sides of the roadway, while the horizontal stress is concentrated in the roof and floor. Deterioration would be manifested as a forming zone of deteriorated rock mass in the roadway roof. This is noted during previous re-

search. In such zones, the rock is very fragmented, and the deterioration zone also continues to expand in the immediate roadway rock mass. [11]

### Future research

The future research certainly should include measuring of the stress in the ore body "Borska reka" with determining the direction of principle stresses. In that case, the field of stress would be defined by the stress components  $\sigma_1$ ,  $\sigma_3$ ,  $\sigma_v$  and also taken into consideration possible influence of the Bor fault zone as well as inclination angle of the ore body "Borska reka". That could greatly change the picture of stability.

In opening every another level, the additional geomechanical investigations should be carried out. These investigations will determine the physical and mechanical parameters of the rock mass which would be used for further numerical analysis and calculations and compared with the previous laboratory tests results. Also, they would odemtify the correlation between the physical-mechanical, structural properties and categorization of rock mass results as well as defining the behavior of rock mass by the Hoek-Brown's strength criterion. Based on this, it can carefully evaluate and determine the parameters relevant to characterize the behavior of rock mass and thereby used for further modeling of the rock mass and a new forecast for deeper levels.

### CONCLUSION

This paper presents a case study forecast of behavior the rock mass for deeper levels in the ore body "Borska reka" where the field of stress is defined only by the influence of gravitational component and vertical stress direction. The principal

stresses were defined by the linear function result from stress measurements in the ore body "Tilva Roš".

Based on laboratory tests on the previous results, which include the rock mass at the level XVII (K -155 m) in the ore body "Borska reka" and the accurate research and triaxial tests that were carried out on test samples taken from the rock mass, the results were analyzed by the Hoek-Brown methodology and are directly used as the input parameters for numerical modeling.

There was a limiting factor in defining values for stress, because the stress measurement for given location was not measured. Stress state is determined on the basis of the gravity component, and since the ratio of principal stresses hase been evaluated on the basis of stress measurement stress for the ore body "Tilva Roš" even 20 years ago and more.

The numerical model is based on the finite element method (FEM) and the software package PHASE<sup>2</sup> is used for this purpose. Analysis and interpretation of the results were carried and shown for designed and constructed roadway. The results are contained within in displacement vectors, principal stress distribution and plastic zone around the analyzed object.

Stability analysis was firstly done for the level XVII where the straingh criterion and necessary data for analyses are defined for the rock mass. Based on that, the analyses were carried out for deeper leyers in the second phase of forecast stability. The included levels are XIX (-235 K), XXI (-315 K), XXIII (-395 K) and XXV (K -475).

Results and forecast stability of the roadway at deeper layers with characteristics of the rock mass and assumed stress, showing that the stability decreases of the roadway on the analyzed model. Model applied in the analysis remains stable up to the level XIX, while at deeper levels have to be safe and secure with the roof support

system or with fully support. This conclusion is based on the parameters at the level XVII which are according to the volume and estimated stress insufficient for qualitative forecasting stability, especially in the deeper levels. Due to these reasons, it is essential that for each new level the additional geomechanical investigations are needed. As the mining operations go deeper, the results of forecast for the same level would be verified or corrected with these new data, and also work out the forecast of behavior the rock mass for the next deeper level.

Certainly that one qualitative analysis such as stability analysis would be fully been worked out with no use of any estimated value as in this case for the stress value and its direction. To this end, the evaluation of stress in the ore body "Borska reka" as well as to define the parameters essential for understanding the behaviour of rock mass is necessary to complement the current geomechanical investigations with appropriate methods for stress measuring.

Synthesis of previous and proposed research would give more complex image of the ore body "Borska reka". Through appropriate models, from that aspect it would be possible to analyze all kinds of mining activities and performed work. Results of these analyzes could be more reliable applied in practice.

## REFERENCES

- [1] E. T. Brown, Progress and Challenges in Some Areas of Deep Mining, Deep Mining 2012, Australian Centre for Geomechanics, Perth, 2012;
- [2] Boek, E., [2002]: A Brief History of the Development of the Hoek-Brown Failure Criterion.  
([http://rocksolid.ca/help/rocksolid/webhelp/rocksolid/Generalized\\_HoekBrown\\_Criterion.htm](http://rocksolid.ca/help/rocksolid/webhelp/rocksolid/Generalized_HoekBrown_Criterion.htm));
- [3] D. Zlatanović, M. Ljubojev, L. Djurdjevac-Ignatović, G. Stojanović: Modeling of Rock Massif in the Jama Bor with Special Focus on the Previous Explorations of the Ore Body »Borska Reka«; Journal Mining & Metallurgy Engineering 3/2014, Mining and Metallurgy Institute – Bor, pp. 17-32;
- [4] V. Čebašek, N. Gojković: Rockmass Investigations for Determination of Failure Criterion, Journal Underground Mining Engineering 17, University of Belgrade - Faculty of Mining and Geology; (2010), pp. 35-47;
- [5] D. Zlatanović, V. Čebašek, M. Ljubojev: Determining the Parameters of a Rock Mass Model in the Function of Fracture Criterion; The 46<sup>th</sup> International October Conference on Mining and Metallurgy 1-3 October 2014, Bor; pp. 529-532; Serbia;
- [6] D. Zlatanović, M. Ljubojev, Z. Stojanović, G. Stojanović: Determining the Stress of Rock Massif, Mining & Metallurgy Engineering Bor, No. 2, 2014, pp. 33-38; Serbia;
- [7] D. Zlatanović: Stability of Underground Facilities of Deep Metallic Deposits in a Case of the Ore Body – Borska reka; Master Thesis, Faculty of Mining and Geology, University of Belgrade (2000);
- [8] M. Ljubojev, D. Ignatović, L. Đurđević-Ignatović, D. Tašić: Probe for Measuring Stress-Strain State in Rock Massif, 45<sup>rd</sup> International October Conference on Mining and Metallurgy, Bor Lake, 16-19 October 2013, pp. 285-288;
- [9] M. Ljubojev, R. Popović, D. Ignatović, M. Jovanović; Prognosis of the Zone Size Deformations Using the Finite Element Method on the Sample of Underground Exploitation of the Ore Body "Borska reka"; The 44<sup>th</sup> International October Conference on

- Mining and Metallurgy, 1-3 October 2012, Bor; pp. 249-252;
- [10] M. Ljubojev, M. Avdić, L. Đurđevac Ignjatović; State around the Mine Workings; The 44<sup>th</sup> International October Conference on Mining and Metallurgy 1-3 October 2012, Bor; pp. 245-248;
- [11] V. Milisavljević, I. Ristović, V. Čokorilo, N. Lilić, M. Denić: Improvement of Roadway Stability in Serbian Underground Coal Mines; Proceedings of the 4<sup>th</sup> Balkan Mining Congress, 18-20 October 2011, Ljubljana, Slovenia, (2011), pp. 533-538.

Dragan Zlatanović\*, Vladimir Milisavljević\*\*, Milenko Ljubojev\*\*\*,  
Dragan Ignjatović\*\*\*\*

**PROGNOZA PONAŠANJA STENSKOG MASIVA  
PRE OTKOPAVANJA NA DUBLJIM HORIZONTIMA  
RUDNOG TELA BORSKA REKA**

*Izvod*

*U ovom radu prikazan jedan od načina na koji bi moglo da se pristupi u rešavanju nekih važnih pitanja vezanih za stabilnost podzemnih objekata na većim dubinama. Analiza je fokusirana na predviđanje ponašanja stenskog masiva pre izvođenja rudarskih radova i to u konkretnom slučaju na dubljim nivoima u rudnom telu "Borska reka" u rudniku Jama u Boru.*

*Pored obimnog dosadašnjeg istraživanja rudog tela "Borska reka" i dobijenih parametra za modeliranje stanja napona i deformacija koji se javljaju pod uticajem rudarskih radova, dodatno je izvršena i procena naponskog stanja u masivu. Prikazana je analiza stabilnosti prostorija na nivou XVII horizonta i izvršena prognoza stabilnosti istih prostorija za dublje nivoe otvaranja. Kao rezultat se očekuje da će nivo neizvesnosti i rizika u vezi sa mnogim identifikovanim geomehaničkim rizicima u upravljanju stenskim masivom biti smanjen.*

**Ključne reči:** predviđanje, ponašanje stenskog masiva, stabilnost prostorije, rt Borska reka

**UVOD**

Rudarski radovi i izrada prostorija u dubokim rudnicima izazivaju nestabilnost u radnoj sredini koja može nastati kao rezultat popuštanja krovine, pukotina i izboja iz bokova ili kombinacije oba. Zbog toga, stavljajući bezbednost na prvom mestu prilikom izvođenja rudarskih radova, stabilnost ovakvih prostorija je veoma važna. Osnovna briga u otkopavanju je kontrola pomeranja u stenskom masivu oko

izgrađene prostorije. Za svaku prostoriju, cilj projektovanja je da osigura da pomeranja oko prostorije nemaju uticaj na određene rudarske aktivnosti.

Modeliranje u kontroli ponašanja nadkopnih stena i slojeva u mehanici stena značajno je razvijan poslednjih decenija. Postoje različite numeričke metode i softveri dostupni za analizu stabilnosti podzemnih otvora. Uprkos značajnom napredku koji je

\* Univerzitet u Beogradu – Mašinski fakultet – Inovacioni Centar, Kraljice Marije 16, Beograd;  
e-mail: dr.dragan.zlatanovic@gmail.com, naučni saradnik

\*\* Univerzitet u Beogradu – Rudarsko-geološki fakultet, Djušina 7, Beograd,  
e-mail: vladimir.milisavljevic@rgf.bg.ac.rs

\*\*\* Institut za rudarstvo i metalurgiju Bor, Zeleni bulevar 35, Bor, e-mail:  
milenko.ljubojev@irmbor.co.rs; dragan.ignjatovic@irmbor.co.rs

\*\*\*\* Ovaj rad je proistekao kao rezultat projekta 33021 „Istraživanje i praćenje promena naponsko deformacijskog stanja u stenskom masivu „in-situ“ oko podzemnih prostorija sa izradom modela sa posebnim osvrtom na tunel Kriveljske reke i Jame Bor“, koga finansira Ministarstvo prosvete, nauke i tehnološkog razvoja Republike Srbije

napravljen, prepoznaće se da uspešna primena numeričkih metoda u projektovanju i analizi stabilnosti, zavise u velikoj meri od geomehaničkog modela i graničnih uslova razvijenih za podatke sa date lokacije. Zbog teškoća u definisanju nekih od ulaznih podataka, često se koriste stohastičke metode i verovatnoća za predstavljanje mehaničkih osobina stena i stenske mase, kao i u samim analizama.

Projekat za rudnik podzemne eksploata-

, utvrđivanje proizvodnih kapaciteta i graničnog sadržaja korisne komponente. Bira se odgovarajuća metoda prateći granice rudnog ležišta. Utvrđuje se plan razvoja osnovne infrastrukture otvaranja i analiza opštег redosleda otkopavanja. Mnogo procena može da se uradi pre nego što projekat započe.

Kada se projektuje osnovna infrastruktura otvaranja, jedno od prvih pitanja koja se često postavlja pred mehaniku stena tj. rudarskim inženjerima je "Koliki je maksimalni stabilan profil prostorije?". Međutim, često je prerano i retko da postoji dovoljno dostupnih i sličnih podataka

ve modernih brzih digitalnih računara i numeričkih metoda modeliranja.

U ovoj kompjuterskoj eri, širok spektar računarskog softvera se koristi u numeričkim analizama ponašanja stenske mase. Oni uključuju različita pomeranja po diskontinuitetu i srodne programe, kao što su **FEM**<sup>\*</sup> (*Phase2*), **BEM**<sup>†</sup>, **FDM**<sup>‡</sup> i **DEM**<sup>§</sup>.[1]

Uprkos dostupnosti računarske tehnike i , geomehanička analiza je još uvek više umetnost nego stvarno modeliranje stenske mase.

uraditi dovoljno geomehaničkih istraživanja u fazi planiranja jednog rudarskog projekt

tipova geomehaničkog rizika bude u potpunosti uzet obzir. Međutim, kako se projekat odvija kroz razne faze od ideje do detaljnog dizajna i implementacije, nivo neizvesnosti i rizika u vezi sa mnogim izvorima geomehaničkog rizika koji su prethodno identifikovani može se očekivati da budu smanjeni.

### Primena standardnih kriterijuma čvrstoće

nutno koriste za procenu stabilnosti podzemnih prostorija se zasnivaju na linearnom Mohr-Coulomb kriterijumu čvrstoće. Međutim, eksperimentalni podaci i inženjersko iskustvo pokazalo je da čvrstoća za skoro sve vrste stenske mase prati ne-linearan Hoek-Braun kriterijum čvrstoće. Hoek-Brown kriterijum čvrstoće za stenske mase

čajeva u svetu.

Klasični Mohr-Coulomb kriterijum čvrstoće sastoji se od dve nezavisne komponente kohezije i ugla unutrašnjeg trenja i ne daje realnu sliku o progresivnom lomu i raspodu stene pod pritiskom. Kriterijum Hoek-Braun je široko zastupljeniji za ispučalu radnu sredinu, ali takođe može da se primeni i na

\* Metode Konačnih Elemenata (**FEM**) (Beck et al., 2009, 2010; Goodman et al., 1968; Wittke, 1977, 1990; Zienkiewicz, 1977)

† Metode Graničnih Elemenata (**BEM**) (Beer and Watson, 1992; Brady, 1979, 1987; Crouch and Starfield, 1983)

‡ Konačne Diferencijalne Metode (**FDM**) (Hart et al., 2008; Itasca, 2011; Sainsbury et al., 2011)

§ Metode Diskretnih Elemenata (**DEM**) (Jing and Stephansson, 2007)

neporemećeni stenski masiv. U stvari, mno-

Inom razvoju Hoek i Brovn modela od (1980), a i kasnije. [2]

### **ANALIZA SLUČAJA NA PRIMERU RUDNOG TELA “BORSKA REKA”**

Za svrhu ovog rada, analiza se uglavnom bazira na ponašanju stenske mase na konkretnom primeru, ležištu – rudnom telu "Borska reka" u rudniku Jama u Boru.

Ovo ležište po pružanju ima dužinu od oko 1.000 metara i moćnost oko 500 m, zaleže ka zapadu pod uglom od  $45^\circ$  do  $55^\circ$ , u skladu sa zaleganjem borskih konglomerata i peščara, a od hidrotermalne zone odvojen je borskim rasedom. Istražni radovi na rudnom telu "Borska reka" su započela u periodu od 1976. do ovih dana i to sa velikim obimom istraživačkih radova. Detaljni istražni radovi su izvedeni na nivou K-155 m, a pretpostavlja se da rudno telo zaleže do nivoa K-800 m, pa čak i dublje. Deo ležišta iznad nivoa K-235, otvoren je transportnim sistemom za rudna tela "Tilva Roš" i "P2A".

Rudarski radovi se obavljaju na osnovu rudarskog projekta eksploatacije rude bakra iznad nivoa (K-235). Nakon više godina od utvrđivanja rezervi mineralnih sirovina u rudnom telu "Borska reka", dodatnih istraži-

-  
vanja sa očuvanjem površine terena i svih izgrađenih objekata, infrastrukture i rudarskih radova iznad ležišta "Borska reka", počevši sa otkopavanjem od nivoa XIX

za eksploataciju u sledećoj fazi.

Ovo je svakako i ozbiljan izazov u upravljanju stenskim masivom i geomehaničkim rizicima. Dakle, rezultati ove analize, s jedne strane, odnose se na potrebu za prognozu ponašanja stenske mase pre nego što otkopavanje počne na dubljim nivoima rudnog tela "Borska reka", i sa druge strane, zahtev da se izvrše sva potrebna geomehanička ispitivanja u cilju dobijanja pouzdanih informacija kao osnova za dalje donošenje odluka.

### **PRETHODNA ISTRAŽIVANJA I MODELIRANJE NAPONSKO- DEFORMACIJSKOG STANJA**

#### **Prethodna istraživanja**

U cilju utvrđivanja geomehaničkih karakteristika radne sredine, pregledana je sadašnja tehnička dokumentacija geoloških, geotehničkih i hidrogeoloških ispitivanja i analiza koja se odnose za rudno telo "Borska reka" u rudniku Jama Bor. Na osnovu toga, može se generalno zaključiti da je mnogo toga urađeno i da je mnogo rada, truda i novca uloženo.

Ovde će se samo pomenuti neke od godina kada su predmetna istraživanja rađena, počevši od 1997, 1999, 2007 i 2014 godine od strane Instituta za rудarstvo i metalurgiju iz Bora. [3]

Do sada, prema analizama koja su urađena u okviru najnovijih istraživanja, došlo se do podataka koji pokazuju delimično niže vrednosti koji opisuju fizičko-mehanička svojstva stenskog materijala u odnosu na prethodna istraživanja, tabela 1.

**Tabela 1.** Fizičko-mehanički parametri dobijeni laboratorijskim ispitivanjima na uzorcima uzetih iz stenskog masiva rudnog tela "Borska reka"

Geotehnička sredina	$\gamma$ [kN/m <sup>3</sup> ]	$\sigma_c$ [MPa]	$\sigma_i$ [MPa]	$E_t$ [MPa]	$E_s$ [MPa]	$\nu$ -	$\phi$ [°]	$m_i$ -	C [MPa]	RMR <sub>89</sub>	GSI
Borski peliti *2014	25,4	49	4,95	5600	3730	0,34	36,0	24	12,13	54	
Andeziti *2014	25,9	52	5,37	6927	4633	0,31	36,8	26	12,90	66	
Andeziti kaolinisani *2014	27,0	25	3,04	5490	3672	0,37	30,4	20	7,53	34	
Andeziti silifikovani *2014	27,7	67	7,57	10790	7127	0,32	37,4	28	16,70	51	
(XVII level) K-155	$\gamma$ [kN/m <sup>3</sup> ]	$\sigma_c$ [MPa]	$\sigma_i$ [MPa]	E [MPa]	Ed [MPa]	$\nu$ -	$\phi$ [°]	$m_i$ -	C [MPa]	RMR <sub>89</sub>	GSI
Andeziti silifikovani *1999	28,2	63,39	6,71	40490	33255	0,216	41,6	15,09	18,9	73	65

### Modeliranje naponsko-deformacijskog stanja

Pored standardnih laboratorijskih testova i "in situ" opažanja i merenja, izvršeni su postupci laboratorijskih ispitivanja za testi-

jalne kompresije. Triaksijalni eksperiment ima za cilj da simulira uslove koji se mogu pojaviti u okolnim stenama podzemne infrastrukture - hodnika i objekata i ove prostorije mogu biti izložene graničnom pritisku i naponu smicanja. [4]

Na osnovu prethodnih rezultata laboratorijskih testova sprovedenih na uzorcima stena iz masiva i jezgra istražnih bušotina, uz uzimanje u obzir stanje stenskog masiva, stepena

, deformacionih karakteristika i kvaliteta procene stenske mase, laboratorijske vrednosti su dobijene za parametre stenske mase na nivou XVII horizonta u rudnom telu "Borska reka". [5]

Analiza stabilnosti stena je izvedena na standardnom poprečnom preseku prostorije koja je projektovana i izrađena u Jami Bor (4x3,5m), sa potvrdom relevantnosti obima podataka prikupljenih iz prethodnog istraživanja i gore pomenutih istraživanja.

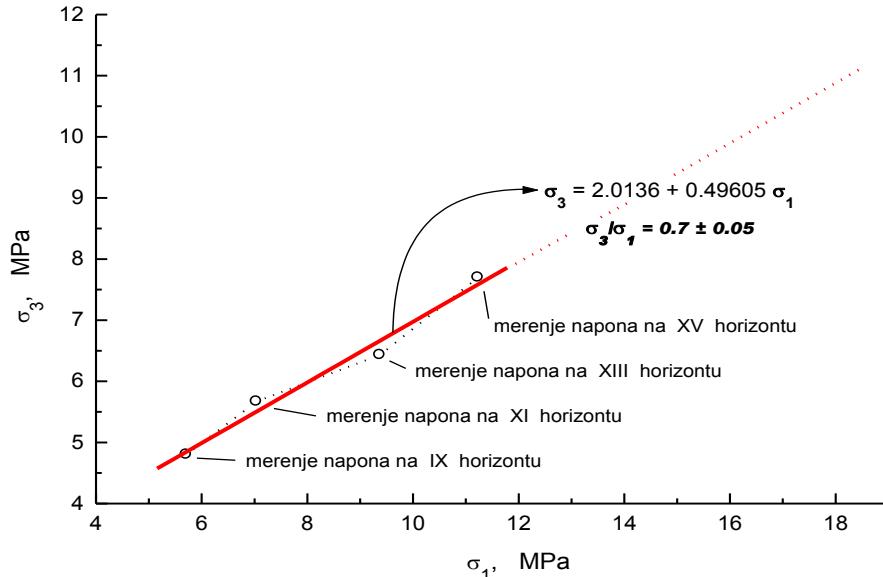
Stanje napona u rudnom telu "Borska reka" ranije nije mereno, zato ovi podaci nisu dostupni. Zbog nedostatka poznavanja naponskog stanja u stenskom masivu, napol-

ciono komponente -  $\gamma H$ . Napon je meren u najблиžem u vidu blizinu, ukazuje na odnose između glavnih napona. Odnos je između  $0,7 \pm 0,05$ . (Slika 1.) Ova procena će se prihvati i za rudno telo "Borska reka" za nivo XVII horizonta (K-155). [6]

Ovde treba napomenuti da su merenja napona urađena pre više od dvadeset godina i samo na konturi prostorije. Može se prête-

je napon meren dublje u stenskom masivu. To znači da nedostatak preciznih vrednosti napona za određeni nivo dubine u rudnom telu "Borska reka" ukazuje na prvi problem u tačnost izvršenih određenih proračuna i zaključaka.

Umesto kvalitativne analize stabilnosti stenske mase, empirijska analiza može da se vrši na osnovu procene i pretpostavke sa namerom da se nademo u traženom opsegu vrednosti, ali možemo i da pogrešimo. [7]



**Sl. 1.** Linearna funkcija odnosa promene izmerenih glavnih napona sa dubinom za rudno telo "Tilva Ros" u rudniku Jama Bor

Utvrđena vrednost napona uzeta je sa slike 1. Za nivo XVII horizonta je za  $\sigma_1 = \sigma_v = 14$  MPa, i za  $\sigma_3 = 9,5$  MPa.

### Izrada Modela

Konturni uslovi su odabrani tako da je opterećenje na modelu samo pod uticajem gravitacijske komponente, tako da je model fiksiran i da nema pomeranja u pravcu X i Y ose.

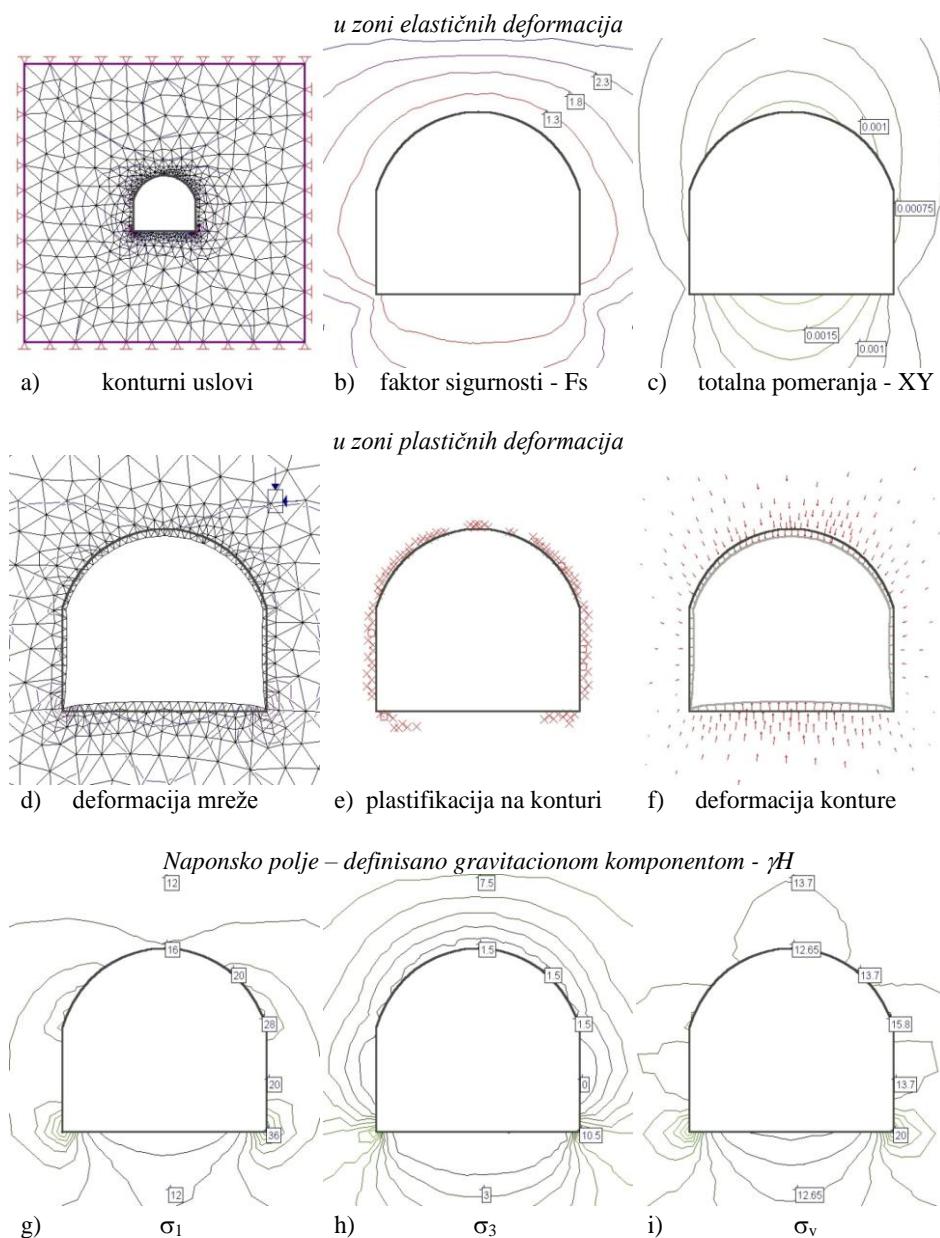
Diskretizacijom modela se određuje potrebna gustina tačaka (čvorova) na konturi profila od koje zavisi broj konačnih elemenata sa kojima će se ući u proračun. U ovom slučaju izabrana je gustina od 75 tačaka (čvorova) po konturi profila. Sa ovim se pokazuje da li i u kojoj meri gustina mreže konačnih elemenata utiče na tačnost rezultata i preciznost kod interpolacije tj. iscrtavanja izolinija napona i deformacija. Mreža konačnih elemenata je sastavljena od tro-

uglova i prikazana je na svakoj slici kod interpretacije rezultata.

### Interpretacija rezultata i ocena stabilnosti

Za modeliranje projektovanog profila prostorije generisana je mreža konačnih elemenata sa ukupno 1.404 elementa i 729 čvorova. Unos podataka se vrši za svaki model posebno, s'time što se razlikuju u pravcima delovanja glavnih napona. Interpretacija rezultata i ocena stabilnosti se prikazuje za sva tri urađena slučaja. Rezultati proračuna su interpretirani izolinijama faktora sigurnosti, totalnih pomeranja i glavnih napona. Takođe je dat prikaz deformacije mreže, deformacija konture sa smerom delovanja pomeranja (koja je uvećana 100 puta) kao i zone plastičnosti obeležene markerima. Markeri u obliku krstića (x) obeležavaju da do loma dolazi usled uticaja napona smicanja, a kružići (o) obeležavaju da do loma dolazi usled napona na zatezanje (Slika 2).

*Projektovani-izvedeni objekat (prostorija) na XVII horizontu - 4x3,5 m*



**Sl. 2.** Naponsko-deformacijska analiza - u slučaju kada je polje napona pod uticajem gravitacione komponente -  $\gamma H$

Ukoliko se stenski masiv oko date prostorije nalazi u zoni elastičnih deformacija, dotele će zona oko prostorije biti stabilna sa raspodelom faktora sigurnosti kako je to na slici 2b prikazano. Ako projektante konturna linija faktora sigurnosti od 1,3 zadovoljava postavljeni kriterijum stabilnosti, vidimo da je u bokovima prostorije ta linija udaljenja od konture i da samim tim ta oblast postaje podložna prelasku iz zone elastičnih u zonu plastičnih deformacija. Maksimalna pomeranja po konturi su 1,8 mm, slika 2c. Na slici su vrednosti totalnih pomeranja date u metrima.

Na mestima na kojima se pojave plastične deformacije, slika 2e, plastifikacija po konturi imaće takav karakter da se po svodnom delu javljaju plastične zone (x), a na bokovima se javljaju plastične zone (x i o).

Može se zaključiti da je ova prostorija stabilna, s'tim da je pojava plastičnih deformacija koje se manifestuju u vidu ljuštenja i otpadanja manjih komada iz bokova i stropa sporadična i da se na tim mestima može na odgovarajući način poduhvatiti i zaštititi prostoriju od daljeg širenja oštećenja. [8]

## PROGNOZA PONAŠANJA STENSKOG MASIVA

Da bi se iskoristila prednost modelskih istraživanja koja nam omogućavaju da

prognoziramo ponašanje stenskog masiva i na dubinama koje još nisu obuhvaćene rudarskim radovima, u ovom delu će se u analizama stabilnosti koristiti veće dubine od nivoa XVII horizonta.

Za izbor dubina uzeti su nivoi XIX (K -235), XXI (K -315), XXIII (K -395) i XXV (K -475) horizonta i predstavljaju vrednosti od oko 630 m, 710 m, 790 m i 870 m dubine.

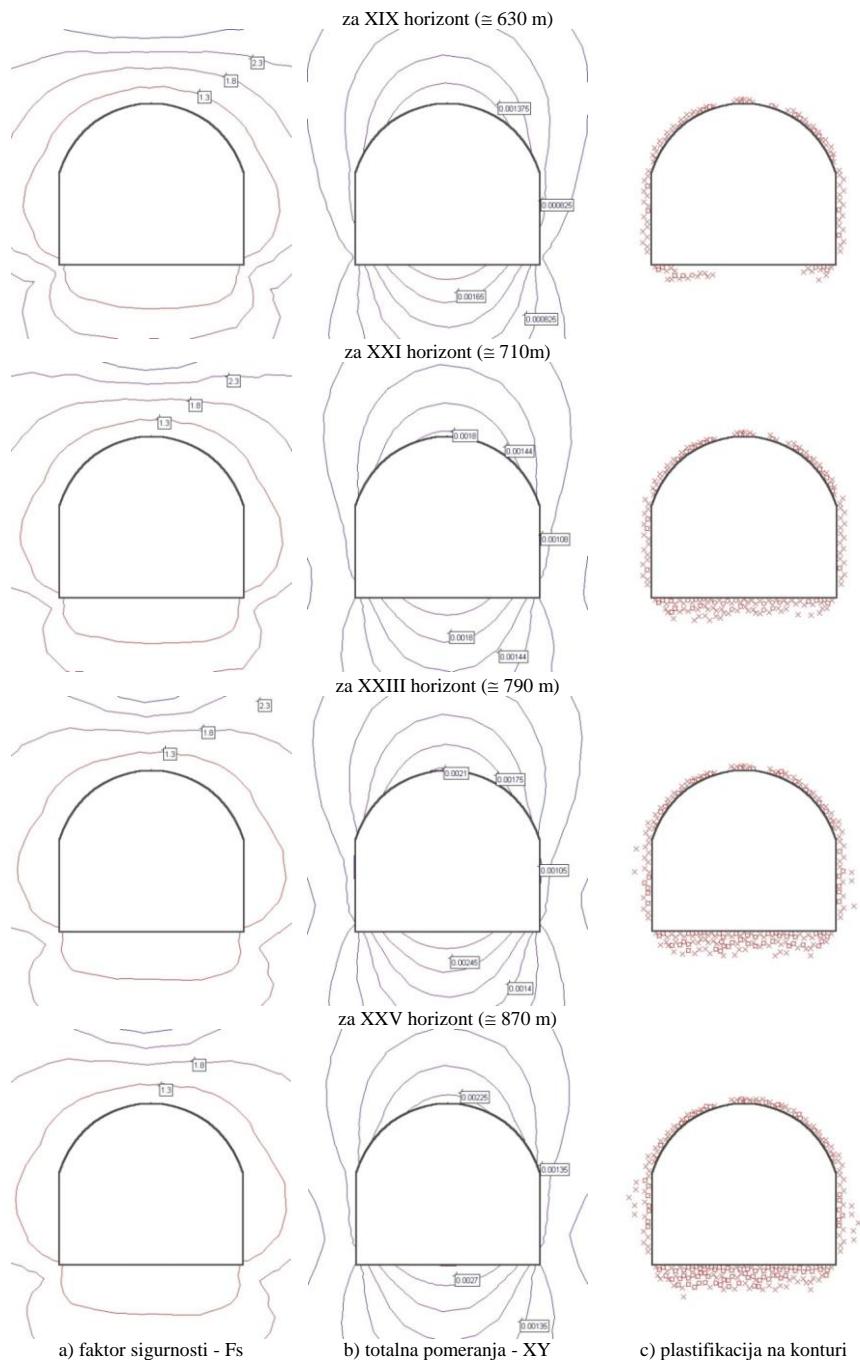
Na osnovu toga se može reći da od izabranih horizonata za procenu stabilnosti, XVII i XIX horizont su obuhvaćeni u projektovanju, što može biti od koristi, jer izgrađeni objekti na ovim horizontima, uz odgovarajuća snimanja, mogu u startu da prikažu valjanost procene ovih analiza. Ostala tri horizonta se analiziraju da bi se predvidelo šta se može očekivati na dubljim nivoima u nekoj kasnijoj fazi i sigurno će biti predmet dalje razrade. [9]

Interpretacija rezultata i ocena stabilnosti su urađeni na način kao i analiza stabilnosti na XVII horizontu da bi se moglo lakše izvršiti upoređivanje rezultata.

Vrednosti primarnih napona su dobijane na osnovu gravitacijske komponente  $\sigma_v = \gamma H$ , a odnos glavnih napona  $\sigma_1$  i  $\sigma_3$  je dobijen iz analitičkog izraza sa grafika na slici 1.

**Tabela 2. Prognozne vrednosti primarnih napona**

Horizont	Kota	okvirna dubina m	$\gamma H$ MPa	$\sigma_1$ MPa	$\sigma_3$ MPa	$\sigma_3/\sigma_1$
XVII	-155	550	14	14	9,5	0,70±0,05
XIX	-235	630	17	17	10,5	0,65±0,05
XXI	-315	710	19,2	19,2	11,5	0,60±0,05
XXIII	-395	790	21,3	21,3	12,6	0,55±0,05
XXV	-475	870	23,5	23,5	13,5	0,55±0,05



**Sl. 3. Naponsko-deformacijska analiza u slučaju kada je naponsko polje pod uticajem gravitacione komponente -  $\gamma H$**

## **Prognoza stabilnosti modela po dubini ispod nivoa XVII horizonta**

Rezultati analize modela su dobijeni za naponsko polje koje je određeno gravitacionom komponentom -  $\gamma H$ . Za modeliranje profila je korišćena mreža konačnih elemenata kao i kod predhodnog ispitivanja.

Za definisanje parametara radne sredine u analizama je korišćen kriterijum loma i parametri stenskog masiva dobijeni na osnovu parametara za XVII horizont. Triaksialnim ispitivanjima, kojima su određivane deformabilne karakteristike stenskog masiva na XVII horizontu, bilo je potrebno, povećanjem bočnog pritiska simulirati i one dubine za koje želimo uraditi procenu stabilnosti. Ova ispitivanja nisu rađena pa su u ovim analizama korišćene deformabilne karakteristike stenskog masiva na XVII horizontu.

Na slici 3, prikazane su naponsko-deformacijske analize stenskog masiva na XIX, XXI, XXIII i XXV horizontu.

Posmatrajući rezultate analize stabilnosti po dubini, može se zaključiti da stabilnost prostorije linearno opada sa povećanjem dubine, što je i bilo očekivano.

Obzirom da su maksimalna pomeranja po konturi u porastu sa povećanjem dubine i to 2,1 mm; 2,4 mm; 2,76 mm i 3,2 mm, a za dublje nivoe od XXI horizonta mogu se očekivati pojačana deformacija i otpadanja komada stenskog materijala iz bokova i stropa prostorije, ukoliko se prostorija ostavi nepodgrađena.

Mesta na kojima se pojavljuju plastične deformacije, plastifikacija po konturi imaće takav karakter da se po svodnom delu javljaju plastične zone (x), a na bokovima se javljaju plastične zone (x i o). Ovo važi samo na XIX horizontu dok se na dubljim horizontima očekuju plastične zone (x i o) po celoj konturi. Veličine zone plastičnog delovanja se kreću u bokovima 18 cm, 21 cm, 28 cm i 35 cm. U stropu im je vrednost 16 cm, 17 cm, 18 cm i 20 cm, dok je u podu samo na XIX horizontu raspore-

đen po uglovima, a na ostalim horizontima raspoređen je po celom podu.

Ono što može narušiti stabilnost konture profila su naponi iz boka prostorije, pri ovako usvojenom odnosu glavnih napona, jer se konturna linija faktora sigurnosti u boku sve više udaljava od samog profila. [10]

Može se proceniti da na nivou XIX horizonta ta prostorija može ostati nepodgrađena osim na mestima gde se pojave plastične zone i gde se ta mesta moraju osigurati. Prognoza stabilnosti za istu prostoriju na XXI, XXIII i XXV horizontu upućuje da mora imati odgovarajuću podgradu na nekim deonicama ili celom dužinom. Kao posledica povećanja dubine može se primebiti određeno "smirivanje" u povećanju plastične zone oko konture profila što nas navodi da je potrebno redefinisati konturne uslove opterećenja na modelu sa predpostavljenim ili izmerenim novim vrednostima glavnih napona kao i nihovim pravcем delovanja.

U prostoru plastične zone rastresanje stena uglavnom je izazvana visokom deformacijom. Deformacija počinje odmah nakon iskopa i obično se stabilizuje sa ugradnjom podgrade kada dolazi do ravnoteže sile ali se može doći do pogoršanja i propadanja krovine kao rezultat reoloških ponašanja stenske mase.

Pogoršanje i propadanje krovinskih stena u podzemnim prostorijama bi moglo da se javi iz nekoliko razloga. Glavni uzrok je koncentracija napona u neposrednoj krovini i podinskim stenama, kao i u bokovima prostorije. Ova koncentracija se generiše poremećajem inicijalne ravnoteže nakon izrade prostorije, stvarajući koncentraciju vertikalnog napona u bokovima prostorije, dok je horizontalni napon koncentrisan u krovnom delu i podu. Propadanje stena bi se manifestovalo kao formiranje zone narušene stenske mase u stropu prostorije. Ovo je

zabeleženo u jednom od prethodnih istraživanju. U takvim zonama stena je veoma rastresena, a zona propadanja takođe nastavlja dalje širenje u neposrednoj krovini prostorije. [11]

### Buduća istraživanja

Buduća istraživanja svakako moraju uključiti merenje naponskog stanja u rudnom telu Borska reka, ali i utvrđivanjem pravca njegovog delovanja. U tom slučaju bi naponsko polje bilo definisano sa komponentama napona  $\sigma_1$ ,  $\sigma_3$ , i  $\sigma_v$  uz uzimanje uzbir promenu pravca delovanja napona zbog mogućeg uticaja Borske rasedne zone kao i samog ugla zaledanja rudnog tela "Borska reka", mogao u mnogome da promeni sliku o stabilnosti.

Prilikom otvaranja svakog sledećeg nivoa, izvršiti dodatna geomehanička istraživanja. Ovim istraživanjima će se odrediti fizičko-mehanički parametri stenskog masiva koji bi se koristili za dalju numeričku analizu i proračune, a ujedno bi se uporedjivale sa rezultatima prethodnih laboratorijskih ispitivanja. Takođe bi se utvrdile korelace veze između fizičko-mehaničkih, strukturnih svojstava i rezultata kategorizacije stenskih masa, kao i definisanje čvrstoće stenskog masiva po Hoek-Brown-ovom kriterijumu loma. Na osnovu toga se mogu pažljivo proceniti i odrediti parametri koji će biti relevantni da karakterišu ponašanje stenske mase i sa time ući u dalje modeliranje stenskog masiva i novu prognozu za dublje nivoe.

### ZAKLJUČAK

U ovom radu prikazana je analiza slučaja prognoze ponašanja stenskog masiva za dublje nivoe u rt „Borska reka“ gde je naponsko polje definisano samo sa gravitacionom silom i vertikalnim delovanjem

napona, pri čemu su glavne komponente napona definisane odnosom proizašlim iz merenja napona u rt Tilva Roš.

Na osnovu prethodnih rezultata laboratorijskih ispitivanja gde je obuhvaćen stenski masiv sa XVII horizonta (K -155 m) u rudnom telu "Borska reka" i odgovarajućih istraživanja i triaksijalnih ispitivanja koja su rađena na probnim telima iz uzetih uzoraka, dobijeni rezultati obrađivani su po Hoek-ovoј metodologiji i direktno su se koristili kao ulazne veličine za numeričko modeliranje.

Ovde je bio ograničavajući faktor u proizvoljnosti uzimanja vrednosti za definisanje naponskog stanja, jer merenja napona za datu lokaciju nije bilo. Naponsko stanje je određeno na osnovu gravitacijske komponente, a dok je odnos glavnih napona procenjen na osnovu izvršenih merenja napona za rudno telo "Tilva roš" još pre 20 i više godina.

Numerički model je baziran na metodi konačnih elemenata (MKE) i za tu svrhu je korišćen programski paket PHASE<sup>2</sup>. Analiza i interpretacija rezultata istraživanja je urađena i prikazana za projektovanu i izvedenu prostoriju. Rezultatima su obuhvaćeni vektori pomeranja, raspodela napona sa izolinijama glavnih napona kao i zone plastifikacije oko analiziranih objekata.

Analiza stabilnosti je obuhvatila prvo XVII horizont za čiju radnu sredinu imamo definisan kriterijum loma i potrebne ulazne podatke za sam tok proračuna. Na osnovu njih je u drugoj fazi vršena prognoza stabilnosti za dublje horizonte. Obuhvaćeni su nivoi XIX (K -235), XXI (K -315), XXIII (K -395) i XXV (K -475).

Rezultati i prognoza stabilnosti prostorija na dubljim horizontima sa predpostavljenim osobinama stenskog masiva i naponskog stanja, pokazuju da se stabilnost prostorija na analiziranim profilima smanjuje. Primjenjeni model u analizi ostaje stabilan do nivoa XIX horizonta, dok za dublje hori-

zonte morao bi biti osiguran i podgrađen. Ovaj zaključak se izvodi na osnovu parametara radne srednine sa XVII horizonta koji su po obimu i predpostavljenom naponskom stanju sami po sebi nedovoljni za kvalitativnu prognozu stabilnosti, a pogotovo na dubljim horizontima. Iz tih razloga je neophodno da se za svaki novi horizont urade sva potrebna geomehanička istraživanja. Kako se radovi budu spuštali na veću dubinu, sa tim podacima bi se verifikovali ili korigovali rezultati prognoza za isti nivo, a ujedno i vršila prognoza za ponašanja stenskog masiva sledećeg dubljeg nivoa.

Naravno da bi jedna kvalitativna analiza, poput analize stabilnosti, bila održana do kraja, ne bi smelo da u nju ulazi ni jedna procenjena vrednost, kao što je u ovom slučaju bila vrednost napona u masivu kao i njegov pravac. U tom cilju, za ocenu naponskog stanja u rudnom telu "Borska reka" kao i za definisanje parametara bitnih za sagledavanje ponašanja stenskog masiva potrebljano dosadašnja geomehanička istraživanja upotpuniti i sa primenom adekvatnih metoda za merenje naponskog stanja.

Sinteza dosadašnjih i predloženih istraživanja bi dala potpuniju sliku o rudnom telu "Borska reka". Sa tog aspekta bi bilo moguće kroz odgovarajuće modele analizirati sve vrste rudarskih radova koji bi se izvodili. Rezultati tih analiza bi se mogli sa većom pouzdanošću primeniti u praksi.

## LITERATURA

- [1] E. T. Brown, Progress and Challenges in Some Areas of Deep Mining, Deep Mining 2012, Australian Centre for Geomechanics, Perth, 2012.
- [2] Boek, E., [2002]: A Brief History of the Development of the Hoek-Brown Failure criterion ([http://rocscience.ca/help/roCDATA/webhelp/roCDATA/Generalized\\_Hoek-Brown\\_Criterion.htm](http://rocscience.ca/help/roCDATA/webhelp/roCDATA/Generalized_Hoek-Brown_Criterion.htm));
- [3] D. Zlatanović, M. Ljubojević, L. Đurđević-Ignjatović, G. Stojanović: Modeliranje stenskog masiva u Jami Bor sa posebnim osvrtom na dosadašnja istraživanja rudnog tela "Borska Reka", Mining and Metallurgy Engineering Bor, 3/2014, str. 25-32;
- [4] V. Čebašek, N. Gojković: Rockmass Investigations for Determination of Failure Criterion, Journal „Underground Mining Engineering 17“, University of Belgrade - Faculty of Mining and Geology; (2010), str. 35-47;
- [5] D. Zlatanović, V. Čebašek, M. Ljubojević: Determining the Parameters of a Rock Mass Model in the Function of Fracture Criterion; The 46<sup>th</sup> International October Conference on Mining and Metallurgy 1-3 October 2014, Bor; str. 529-532; Serbia
- [6] D. Zlatanović, M. Ljubojević, Z. Stojanović, G. Stojanović: Određivanje napona stenskog masiva, Mining and Metallurgy Engineering Bor, 2 (2014), str. 39-44;
- [7] D. Zlatanović: Stabilnost podzemnih objekata dubokih metaličnih ležišta na primeru rudnog tela - Borska reka; Magistarska teza, Rudarsko-geološki fakultet, Univerzitet u Beogradu (2000);
- [8] M. Ljubojević, D. Ignjatović, L. Đurđević-Ignjatović, D. Tašić: Probe for Measuring Stress-strain State in Rock Massif, 45<sup>rd</sup> International October Conference on Mining and Metallurgy. Bor Lake, 16-19 October 2013, str. 285-288;
- [9] M. Ljubojević, R. Popović, D. Ignjatović, M. Jovanović; Prognosis of the Zone Size Deformations Using the Finite Element Method on the Sample of Underground Exploitation of the Ore Body "Borska reka"; The 44<sup>th</sup> International October Conference on Mining and Metallurgy 1-3 October 2012, Bor; str. 249-252;

- [10] M. Ljubojev, M. Avdić, L. Đurđevac Ignjatović; State around the Mine Workings; The 44<sup>th</sup> International October Conference on Mining and Metallurgy 1-3 October 2012, Bor; str. 245-248;
- [11] V. Milisavljević, I. Ristović, V. Čokorilo, N. Lilić, M. Denić: Improvement of Roadway Stability in Serbian Underground Coal Mines; Proceedings of the 4<sup>th</sup> Balkan Mining Congress, 18-20 October 2011, Ljubljana, Slovenia, (2011), str. 533-538.

*Miodrag Miljković\**, *Rodoljub Stanojlović\**, *Jovica Sokolović\**

## DETERMINATION THE NECESSARY STRENGHT OF STOPE FILLINGS AT TOTAL LAYER EXCAVATION\*\*

### **Abstract**

*The basic aims of layer excavation by filling methods are: increasing or total layer spending without ore impoverishment, layer excavation in complex mining and geological conditions, environmental factors preservation, improvement of ergonomic and safety work conditions and recirculation the waste material.*

*For achievement of these aims, it is necessary to put in the stope the filling material of appropriate physical and mechanical characteristics, especially the pressure strength. This work presents a discussion of procedure of filling material selection with necessary strength, and application of filling stoping methods at complete layer excavation and protection of the earth surface and objects on it from damages.*

**Keywords:** total excavation, filling of the stopes, stoping strength

## 1 INTRODUCTION

Complete excavation of the mineral ore layer without depletion of mineral ore and with preservation the environmental factor in the exploitation field can be only realized by the mining method with filling the cavities in ascending or descending order of excavation and filling [1]. Depending on the objectives of full deposit excavation with filling the cavities, the required strength of backfill can be determined and selection the type of filling material with which that the strength can be achieved [2].

This can be achieved by applying of solidifying backfill [3].

Completely obtaining of layers without getting ore dilution can be carried by the following groups of excavation methods [4]:

1. The central excavation of corridors, steep ore veins and lenses is a) from bottom to top, standing of equipment on the back fill, b) from top to bottom, under backfill, when the equipment is at a solid rock (ore).

2. Single-or multi-layer excavation of powerful ore deposits; a) vertically layered

\* University of Belgrade, Technical Faculty Bor, Vojiske Jugoslavije 12, 19210, Bor, Serbia,  
e-mail address: jsokolovic@tf.bor.ac.rs

\*\* This paper presents the results of the Projects TR 33007, "Implementation of Modern Technical-Technological and Environmental Solutions in the Existing Production Systems of the Copper Mine Bor and Copper Mine Majdanpek" and TR 33038 "Improving Technology of Exploitation and Processing of Copper Ore with Monitoring the Living and Working Environment in the RTB Bor Group", funded by Ministry of Education, Science and Technological Development of the Republic of Serbia. The authors are grateful to the Ministry for financial support

excavation from bottom to top (equipment moves on the backfill), b) horizontal layered excavation from top to bottom and beneath concrete slab (equipment is moving on solid ground).

3. Sublevel excavation of ore deposits with subsequent excavation back filling; a) curing over burden with movement of the excavation front from bottom to top, b) under concrete slabs, by excavation back filling with curing over burden (excavation fronts are moving from top to bottom).

4. Chamber pillar ore deposits excavation with ore storage, filling of stope by solidifying backfill and subsequent obtaining the protective ore pillars in filling by the same stoping method. It can be applied as: a) panel and b) cross-excavation of chambers.

Depending on the order of mining, construction and excavation geometry, objectives, implementation costs of excavation methods, physical and mechanical characteristics of the deposit and associated rocks, as well as the depth of the deposit, the necessary strength of backfill will be determined.

## **2 RELATIONS BETWEEN ASSOCIATED DEPOSITS ROCKS AND FILLED EXCAVATED AREAS IN THE DEPOSIT**

Strength of solidifying backfill is satisfactory (normative) if it is possible to secure the opening of the artificial, (backfilling) massive of designed mining areas and excavation, and if the earth's surface and objects above the deposits can be maintained from deformation. The gravitational and tectonic (static) and blasting (dynamic) powers have effect on massive from backfilling material. Mass of backfilled excavation may be subjected to deformation under pressure, stretching, shearing, bending in uniaxial, biaxial and volume of stressed state. Strength of filling material shall be selected to suit the strength of the uniaxial pressure. For choice and control the necessary strength of filling materials considering the role to be met,

regardless of the character of the load. The required strength of filling material is determined by one or more factors:

- a) stability (holding) of vertical open sides,
- b) horizontally open ceilings,
- c) the allowable deformation of the earth's surface,
- d) the ability to move of equipment on the backfill surface, etc.

Mass from the filling material and surrounding rocks, in certain circumstances, form a complex spatial system backfill-rock. The main structural elements of such system roof and floor rocks and filling space are very different.

Calculation of strength of backfill is based on the knowledge of the stress-deformation characteristics of natural and artificial rock, (from backfill), mass in the excavation area, character of their interaction and is reduced to solution of three tasks.

1. Finding a load to the mass of back-filled excavation,
2. Determination of stresses in the backfill as an integral element of the system of rocks (rocks back-filled area),
3. Determining the necessary strength of backfill, resulting in the required ratio of manifestation (safety) for a given stress state, with the impact of other technological factors in the excavation of deposits.

Load to an artificially massive backfill of excavation depends on: the physical-mechanical characteristics of surrounding rocks, stress in them, backfilled excavation geometry, (size, depth and slope) and physical-mechanical characteristics of backfill, as well as the role of construction of backfilling materials fulfill during the further exploitation and termination of deposit exploitation.

In total deposit excavation (excavation by prior filling), the roof of deposit, near the excavation area, forms a zone of reduced pressure (loading), and in mineral massif in front of the zone of advancement

occurs a zone of high support pressure, Fig. 1 With the increase in width of excavated space and backfilled space, the roofing rocks and backfill in the space filled, behave like the surrounding rocks and permissive support units, until backfill receives the entire burden of roofing rocks pillar. Load on the excavation comes from roofing rock slab, which is partly supported on the back-filled part of excavation area, and partially on the ore massif. Dimensions of unloading zones are proportional to the deformation characteristics of the backfill,  $\varepsilon$ . Deformation characteristics of backfill depend on the type of backfill and installation. At  $\varepsilon \leq 3\%$  moving of leaning rocks is performed by folding without cracking and fragmentation. At  $\varepsilon \geq 3\%$  in the roof occurs cracking and layering of rocks. The value of stress concentration coefficient in the ore massif is determined by the width of excavated space L and the stress concentration in the ore massif, by the formula:

$$K_k = 2.1 - 1.1 e^{-(L/80)^{1.5}}$$

$$K_k = (0.8 l_e \cdot n + 14) H^{-0.33}$$

where:

e - base of natural logarithm

L - width of excavated space m,  $L = n \cdot l_e$

$l_e$  - excavation width (tape, layer) in getting (the equivalent pillar width of the excavation ceiling)

n - number of tracks in simultaneous getting to achievement the critical width

$$l_k = n \cdot l_e$$

H - depth of works for which stresses in the roof are related;

$$\tau = \rho g H, (\text{Pa})$$

Tests have shown that maximum pressure of support at width of excavation space  $L=30-40$  m is  $(1.5 - 1.6) \rho g H$ . Maximum is at 15 - 20 m from the forehead of excavation front, and the width of stressed zone is about 50 m. Backfill material suffers loading only at width of excavated space 40 - 60 m.

During excavation of backfill below deposits, backfill material plays the role of artificial roofing below which the unloading zone is also formed in the area of excavation and zone of support pressure on the sides in front of excavation forehead and in the backfilled space. The load depends of backfill weight and roofing rocks pressure, if they already have the suffered deformations.

### 3 REQUIRED BACKFILL STRENGHT AT CHAMBERS EXCAVATION WITH BACKFILL

Economical massive excavation of the low-grade (low value) ore deposits applying excavation method with filling the cavities, can only be performed by the use of highly productive excavation methods. The chamber pillar excavation method can be one of them with ore storage, with chamber backfilling after ore discharge by curing backfill and subsequent obtaining of protective pillars of ore using the same stoping method, for which an analysis of required backfill strength have to be carried out (Fig. 2). The required backfill strength can be viewed for three stages where a pillar of backfill material can be found in excavation area.

1. When the chamber is located between the protective pillars from ore (stage I),
2. When the chamber is located between the pillar of ore and the pillar from hardened backfill adjacent to the excavated chamber (stage II) or backfilled space,
3. When the chamber is located between the protective pillars from hardened backfill.

**1. In the first stage** backfill in the chamber will not be burdened by any vertical load of more lying rocks, except its own mass. Lateral load in the pillar of backfill may occur due to deformations the sides of chamber. The stable range of chamber ceiling ( $l_e$ ) is determined from strict conditions

of stability the mine premises and excavation and chamber ceiling. Stability of the undermined ceiling to critical deformation is determined from the condition.

$$g_r > g_d$$

where:

$g_d$  - allowable deformation of ceilings at which the ceiling of chamber is stable,

$g_r$  - relative deformation of chamber ceiling. It is determined by the formula:

$$g_r = 1/[1+(H_R/l_e)^f]$$

$H_R$  - reduced for monolithic mass requirements, depth of chamber ceiling

$$H_R = (1-K_g) H_k$$

$H_k$  - thickness of the roofing sediments at the surface to the plane of ceiling chamber.

$K_g$  - stability loss coefficient of ceiling due to cracking and structural properties of rocks (depend of RQD characteristics). Its value can be determined based on the percentage of the extracted core.

$$K_g = 0.84 + 0.01 N_j - 0.0002 N_j^2$$

where:

$N_j$  - percentage of extracted core (often showing a high value),

$f$  - coefficient of rocks strength by Pro-togakonov,

$l_e$  - equivalent stable range of chamber cavity (width).

Equivalent stable range (width) of chamber can be determined, if adopted boundary conditions, and solved explicitly by the formula  $l_e$ .

$g < 0.001$  - stable range of chamber,

$g = (0.001-0.04)$  - state between stability and complete caving in,

$g \leq 0.04$  - complete collapse of leaning roofing

$$l_e = f \sqrt{\frac{g H_R^f}{1-g}} = H_R f \sqrt{\frac{g}{1-g}}, \text{ (m)}$$

Stresses will be concentrated in the sides of chamber as shown in Fig. 1.

They will not be transferred to the backfill in the chamber, or more chambers. While undermined cavity beneath the roofing reaches a critical range (talking about the cavity because at excavation filling it will never completely include roofing materials).

$$l_k = H_k f \sqrt{\frac{g}{1-g}}, \text{ (m) at } g > 0.04$$

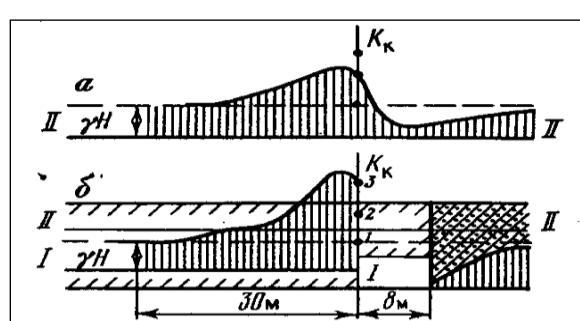


Figure 1 Chart of changes of the stress concentration in the ore and massif of the backfill

**2 The second stage** of chamber position in the excavation and backfilled space is the most common. The exploitation of large steep ore bodies, critical range of excavated areas where the roof caving occurs, is less

than the length of excavation front. Blocks of caved rocks will load the backfilled space if the backfill is compressible (plastic) that will result in larger deformations in the roof, and even to the deformations of the earth's

surface (in shallower deposits). Yet the filled space represents the relief zone. At the moving of excavation front from the periphery of the ore body to the opening premises, the following cases of stress can be logged:

a) Above the first of excavated chambers at width of excavated space  $L = nl_e < l_k$  (stable equivalent widths), the clamping stresses appeared in the excavation roof and the comprehensive stresses are concentrated on the sides of excavation and undisturbed rocks, depending on the width of excavated space. Coefficient of power concentration is

determined by formula  $K_k$ , and vertical stress in the massif is:

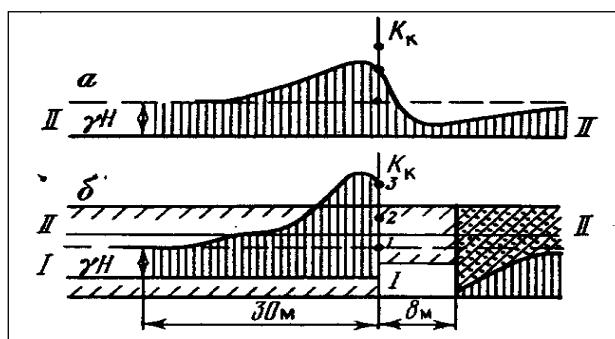
$$\sigma_p = K_k \rho_s g H, (\text{Pa})$$

Horizontal stress  $\sigma_y$  on the chamber side according to Fig. 2 is:

$$\sigma_y = \frac{\mu}{1-\mu} K_k \rho_s g H, (\text{Pa})$$

where:

$\mu$  - is the Pauson coefficient  $\mu=(0.4\div 0.6)$  (coefficient of side load).



**Figure 2** Scheme for calculation the stress of protective pillars on backfill in the chamber

Concentration of stress coefficient as in front of the forehead excavation front in the mine, and as in the final pillars of the backfill will increase with each subsequent excavation chamber, until the range of the excavated space does not exceed the critical width  $L > l_k$ .

b) When it excavated more chambers, so that the range of excavated space  $L$  becomes unstable or crashes, it will cause occurrence vertical stress in the backfill massif. Size of the vertical stress, which can occur in artificial pillars of the backfill, is calculated using the principle of simultaneous deformation of combined supports, pillars of the ores and pillars of backfill by the formula:

$$\sigma_1 = \frac{K_a \rho_s g H S_k}{10^6 (S_z + 0.77 S_p \frac{E_s}{E_z})} + 10^{-6} \rho_z g h_z$$

where:

$\rho_s, \rho_z$  - density of rock material and backfill material

$H$  - depth of excavated ceiling space

$S_k, S_z$  - surface of ore pillars and pillars of the backfill

$E_s, E_z$  - deformation modulus of ore deposit and backfill material

$K_a$  - impact coefficient of the deposit inclination angle to the load of backfill

$$K_a = \cos^2 \alpha - \eta \sin^2 \alpha ; \eta = \mu / (1 - \mu)$$

$h_z$  - height of backfill pillar (height of excavated and backfilled space)

$\alpha$  - deposit inclination angle (slope of filled cavity).

Strength of backfill in the excavated area must be greater than vertical stress that occurs in the backfill to prevent loosening and compacting of backfill and further deformation of roofing.

$$\sigma_z > \sigma_1$$

In deep thin deposit, a compacting of backfill may be allowed to a certain height, at which the illicit deformations of the earth's surface will not occur and the reduction of safety coefficient K [4].

c) The final event of the second stage occurs at the movement of excavation front so that the getting of chambers is performed between the massive of ore and massive of backfill. The roof is based on excavated ore front, with console of not supported roofing on backfill of length  $l < l_e$ ;  $l < n \cdot l_e$  and part of the roofing which is caved under more lying masses. Chamber of excavation is located under the console, where the vertical stresses are reduced. Maximum vertical stress is in front of excavation front in ore massif. And in the excavation chamber at a distance  $l < l_k$  there is a zone of reduced vertical stress. At a distance  $L > l_k$ , the massive and backfill are under concentrated vertical stress, the same as in the ore massif. For finding the necessary strength of backfill to preserve the earth's surface from deformation, it is necessary to take into account the possible allowed backfill compression at which there will be no damage to the earth's surface.

For blind isolated deposits with proper form, influence of size (height) of excavated areas and backfilled area to deformation (settlement) of the earth's surface, depending on the compression properties of backfill, is evaluated based on the safety coefficient whose value should be greater than are permitted by Table 1 [5].

$$K_s > K_d = H / \Delta P$$

The vertical acceptable size of deformation of backfilled space  $\Delta P$  is determined by the formula:

$$\Delta P = \varepsilon_o h_z (1-e) \sigma_1 / \sigma_z, \text{ (m)}$$

where:

$\Delta P$  - decrease of height of pillars by backfill under load  $\sigma_1$ , (m)

$\sigma_1$  - acting vertical stress, (Pa)

$\varepsilon_o$  - deformation characteristics of certain type of backfill

$h_z$  - thickness (height) of backfill pillar

$\sigma_z$  - strength of backfill to the pressure

$K_s$  - safety coefficient which evaluates the stability of roofing.

The necessary or sufficient strength of backfill  $\sigma_z$  for thin deep deposits can be calculated from the above formula, where due to roofing load backfill will be overloaded and partially compressed. Permitted backfill compression will be  $\Delta P = H/Kd$ , and the necessary strength of backfill  $\sigma_z$ :

$$\sigma_z = \frac{\sigma_1 \ln \cdot \varepsilon_o h_z}{\ln(\Delta P)}, \text{ (Pa)}$$

3. The stage of performing excavation of protective pillar or chamber which is located between the pillars of hardened protective backfill (in the backfill) is the most dangerous, because the stress concentrations occur in the pillars on both sides from excavated areas. Stresses are added, and can be calculated by equations for  $\sigma_p$  and  $\sigma_y$ . The manifestation of dynamic phenomena and rock bursts can occur in the preparation rooms. Rock bursts will not occur if the rock of pillars is not prone to the accumulation of elastic deformations energy and if concentrated stresses are less than rock hardness to the pressure  $\sigma_p < \sigma_{cs}$ .

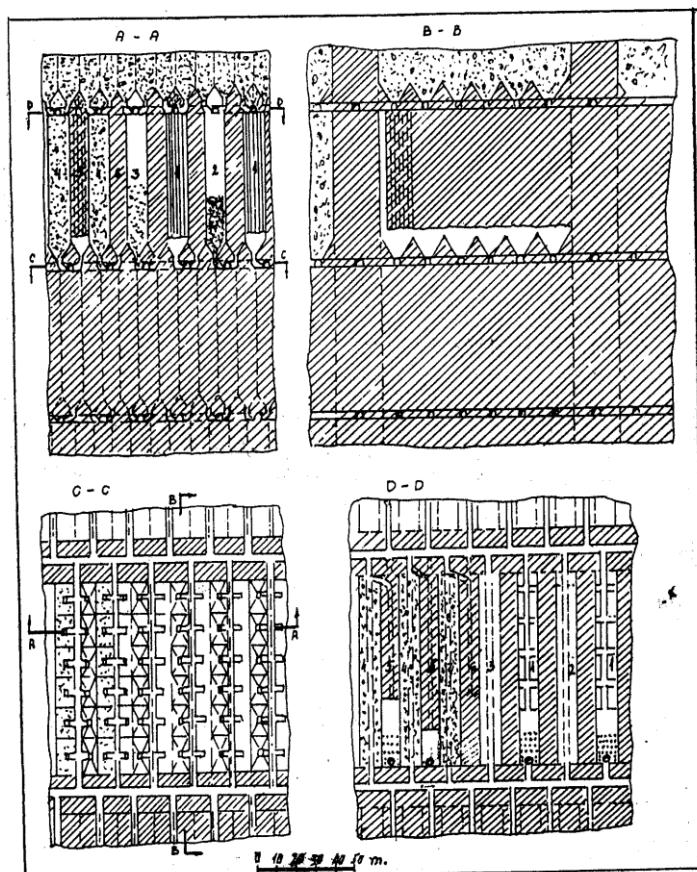
Rock bursts will not occur if the backfill in filled space has a corresponding compressive strength, so that can perform stiffening of ore pillar and ensure the stability of excavation chamber during the excavation. Normative compressive strength backfill in the process of obtaining of chambers between the pillars of backfill materials shall be as follows:

$$\sigma_z = \frac{\sigma_s K_z}{K_f \cdot K_o}$$

where:

$$\begin{aligned}\sigma_s &= \text{stress in backfill pillars}, \\ \sigma_s &= K_a K_{hp} g H \cdot L_s / 10^6 L_z, \\ K_z &= \text{coefficient of safety } K_z = (1.5-3),\end{aligned}$$

$K_f$  - coefficient of pillar form (given the influence of shape and dimensions of pillar on supporting ability [ $K_f = (a/h_s)^{0.5}$  at  $a > h_s$ ] or [ $K_f = 0.6 + 0.4/a/h_s$  at  $a < h_s$ ]);



**Figure 3** Stoping with backfilling of chambers and subsequent obtaining of columns

**Table 1** Safety coefficients

Object category on surface	Permitted horizontal deformations (mm/m)	$K_d$ - for layers	
		Ore	Coal
I	2.0	150	300
II	3.5	100	200
III	5.5	50	100

$a$  - backfill pillar width,

$h_s$  - height of the pillar from curing backfill),

$K_o$  - coefficient that takes into account the increasing of strength pillars at pressure due to compression;  $K_o = \sigma_k / \sigma_o$ ,

$H$  - depth of the upper surface of the pillar,  
 $K_h$  - coefficient that takes into account the degree of load of backfill pillar by caved rocks from roofing,  
 $L_p$  - width of the panel block (chamber) in the backfill,  
 $L_z$  - width of the panel of artificial pillars of backfill.

For the unexplored "in situ" conditions  $K_h = 0.5$  and for chambers between the pillars of backfill which are not backfilled  $K_h = L / h < 1$ , where  $L$  - chamber width (undermined pillar).

Strength of backfill materials for ensuring the stability of horizontal rooms respectively, projected span of rooms in the fill is determined by the formula:

$$\sigma_e = K_z [0.49 \rho g H_z \cos \alpha (0.95 - e^{-0.06a}) - 1.76], \text{ Pa}$$

Selection of dimensions of chambers and pillars and their arrangement at excavation, strength of backfill of chamber and pillar mining method with storage of ore and subsequent back filling of stopes by curing backfill, if more horizons are dug, should be done by equations  $\Delta P$  and  $\sigma_z = f(\Delta P)$ . In them, there will be a change of values  $H_z = N h_H$ ;  $H_z$  - height of backfilled space depends on the  $N$  height of excavated horizons  $h_H$ . Allowable deformation of backfilling area  $\Delta P' = (\Delta_1 + \Delta_2 + \Delta_3)N$  does not depend on the elastic deformation (10 mm) of roofing of each horizon  $\Delta_1$  incomplete filling of chambers about 1%  $\Delta_2$ , and backfill compression due to load  $\Delta_3 = \epsilon_o h_H$ , and changes in vertical stress  $\sigma_1$ .

$$\sigma_1 = K_v K_v \rho g H_s$$

$$\Delta_p' = H_{sr} / K_d$$

$$\sigma_z = \sigma_1' \cdot \ln \epsilon_o \cdot N h_H / \ln \Delta P'$$

Besides the well-known marks  $K_v$  - coefficient which takes the stress change in the fill, depending on the ratio of ore body width and the depth of deposit  $K_v = (A_R / H_s) + 0.61$ ;  $A_R$  - size of ore body by stretching or declining.

From this formula it is evident that protection of the earth's surface from deformation besides strength of backfill, its compressibility is an important parameter, because the strength of backfill on pressure may be less than the vertical stress.  $\text{Pri } \Delta P' = \epsilon_o N h_H ; \sigma_z = \sigma'$ .

## CONCLUSION

For the known geometry of layer, physical and mechanical properties of deposit rocks and accompanying rocks of roofing and bottom, and objectives to be achieved, using the chamber pillar mining method with storage of ore and filling the excavated chambers after discharge of ore, curing backfill, in order to obtain the remaining protective pillars from backfill, according to Fig. 3. It is possible on the basis of considered mutual work of deposit rocks and backfill, in chambers filled, to choose the best dynamics of deposit excavation, arrangement of excavation, backfill material of adequate strength and compressibility, etc.

## REFERENCES

- [1] D. M. Broninkov et al., Backfill Works in the Mines Nedra, Moscow, Russia 1989, p. 146, (In Russian);
- [2] V. I. Homyakov, Foreign Experience Tab in the Mines Nedra, Moscow, Russia, 1984, p. 143, (In Russian);
- [3] V. R. Imenitov, V. F. Abramov, V. V. Popov, Localization of Emptiness in the Underground Ore Mining, Nedra, Moscow, Russin, 1983, p. 72, (In Russian);
- [4] M. Miljković, R. Stanojlović, J. Sokolović, Safety and Deformation Characteristics of Stopping Materials in Mines, Mining Engineering, Bor, 2(2012), pp. 13-28;
- [5] V. Jovičić, M. Miljković, J. Nujić, H. Uljić, M. Vukić, Security Systems in Mining Industry, Tuzla, Univerzal, 1987, p. 423.

*Miodrag Miljković\**, *Rodoljub Stanojlović\**, *Jovica Sokolović\**

## ODREĐIVANJE POTREBNE ČVRSTOĆE ZASIPA PRI POTPUNOM OTKOPAVANJU LEŽIŠTA\*\*

### *Izvod*

*Osnovni ciljevi otkopavanja ležišta metodama sa zapunjavanjem otkopanih prostora su: povećanje ili potpuno iskorišćenje ležišta bez osiromašenja rude, otkopavanje ležišta u složenim rudarsko-geološkim uslovima, očuvanje ekoloških faktora u životnoj okolini, poboljšanje ergonomsko sigurnosnih uslova rada i recirkulacija otpadne jalovine.*

*Za postizanje ovih ciljeva potrebno je u otkope ugrađivati zasipni materijal odgovarajućih fizičko-mehaničkih karakteristika, a posebno u pogledu čvrstoće na pritisak. U radu je razmatran postupak izbora zasipnog materijala potrebne čvrstoće pri primeni otkopnih metoda sa zapunjavanjem otkopnih prostora pri potpunom dobijanju ležišta i zaštiti zemljine površine i objekata od oštećenja.*

**Ključne reči:** potpuno otkopavanje ležišta, zapunjavanje otkopa, čvrstoća zasipa

### 1. UVOD

Potpuno otkopavanje ležišta mineralne sirovine bez osiromašenja rude uz očuvanje ekoloških faktora u eksploatacionom polju može da se realizuje samo otkopnim metodama sa zapunjavanjem otkopanih prostora u uzlaznom ili silaznom poretku otkopavanja i zapunjavanja [1]. Zavisno od ciljeva potpunog otkopavanja ležišta sa zapunjavanjem otkopanih prostora, određuje se potrebna čvrstoća zasipa i bira se vrsta zasipnog materijala kojim se ta čvrstoća može postići [2]. Čvrstoća zasipa naziva se normativnom ako je moguće njime obezbediti sigurno držanje potrebnih

otvorenih prostora. To se može postići primenom očvršćavajućeg zasipa [3].

Potpuno dobijanje ležišta bez osiromašenja rude može se realizovati sledećim grupama otkopnih metoda [4]:

1. Etažno otkopavanje hodnicima, strmih rudnih žica i sočiva; a) odozdo na gore, stajanjem opreme na zasipu, b) odozgo na dole, ispod zasipa, kada oprema стоји на čvrstoj steni (rudi).

2. Jednoslojno ili višeslojno otkopavanje moćnih rudnih ležišta; a) vertikalno slojno otkopavanje odozdo na gore, (oprema se kreće po zasipu), b) horizontalno slojno

\* Univerzitet u Beogradu, Tehnički fakultet u Boru, Vojiske Jugoslavije 12, 19210 Bor, Srbija,  
e-mail: jsokolovic@tf.bor.ac.rs

\*\* im proizvodnim sistemima Rudnik bakra Bor i Rudnika bakra Majdanpek" i TR 33038 "Usavršavanje tehnologije eksploracije i prerade rude bakra sa monitoringom životnog i radnog okruženja u RTB Bor Grupi", koje je finansiralo Ministarstvo za obrazovanje, nauku i tehnološki razvoj Republike Srbije. Autori se zahvaljuju Ministarstvu za finansijsku podršku.

otkopavanje odozgo na dole, ispod betonske ploče (oprema se kreće po čvrstom podu).

3. Podetažno otkopavanje ležišta sa naknadnim zapunjavanjem otkopa; a) očvrščavajućim zasipom sa kretanjem otkopnog fronta odozdo na gore, b) ispod betonske ploče, sa zapunjavanjem otkopa očvrščavajućim zasipom (kretanjem otkopnog fronta odozgo na dole).

4. Komorno stubno otkopavanje ležišta sa magazioniranjem rude, zapunjavanjem otkopa po istakanju rude očvrščavajućim zasipom i naknadnim dobijanjem zaštitnih stubova rude u zasipu istom otkopnom metodom. Tu se može primeniti: a) panelno i b) unakrsno otkopavanje komora.

U zavisnosti od poretku otkopavanja, konstrukcije i geometrije otkopa, ciljeva, troškova primene otkopne metode, fizičko-mehaničkih karakteristika ležišta i pratećih stena, kao i dubine ležišta, vrši se određivanje potrebne čvrstoće zasipa.

## 2. ODNOSI PRATEĆIH STENA LEŽIŠTA I ZAPUNJENIH OTKOPANIH PROSTORA U LEŽIŠTU

Čvrstoća stvrdnjavajućeg zasipa je zadovoljavajuća (normativna) ako je moguće sigurno otvaranje veštačkog, (zasipnog), masiva projektovanim rudničkim prostorijama i otkopima, i ako obezbeđuje očuvanje zemljine površine i objekata iznad ležišta od deformacija. Na masiv od zasipnog materijala deluju gravitacione i tektonске (statičke) i od minerskih radova (dinamičke) sile. Masa zapunjene otkopa može biti podvrgnuta deformacijama usled pritiska, rastezanja, smicanja, izuvijanja u uslovima jednoosnog, dvoosnog i zapreminskog napregnutog stanja. Za izbor i kontrolu potrebne čvrstoće zasipnog materijala, s obzirom na uloge koje treba da zadovolji, nezavisno od karaktera opterećenja, čvrstoća zasipnog materijala bira se prema potreboj čvrstoći na jednoosni pritisak.

Potrebna čvrstoća zasipnog materijala određuje se po jednom ili više faktora:

- a) stabilnosti (držanja) vertikalnih otvorenih bokova
- b) horizontalno otvorenih plafona,
- c) dopuštenih deformacija zemljine površine,
- d) mogućnosti kretanja opreme po površini zasipa itd.

Masa od zasipnog materijala i okolne stene, u određenim uslovima obrazuju složeni prostorni sistem zasip - stene. Glavni strukturni elementi takvog sistema - stene krovine i podine i zasipnog prostora, veoma se razlikuju.

Proračun potrebne čvrstoće zasipa bazira se na znanjima o naponsko - deformacionim karakteristikama prirodnog stenskog i veštačkog, (od zasipa), masiva u zoni otkopavanja, karaktera njihovog uzajamnog delovanja i svodi se na rešavanje triju zadataka.

1. Nalaženja opterećenja na masu zasipanog otkopa
2. Određivanja napona u zasipu kao sastavnog elementu sistema stene, (stena zasipani prostor).
3. Utvrđivanja neophodne čvrstoće zasipa, koja proistiće iz potrebnog koeficijenta pokazanosti, (sigurnosti), za određeno naponsko stanje, uz uticaj ostalih tehnoloških faktora pri otkopavanju ležišta.

Opterećenje na veštački masiv zasipa u otkopu zavisi: od fizičko-mehaničkih karakteristika okolnih stena, napona u njima, geometrije zapunjene otkopa, (veličine, dubine i nagiba), i fizičko-mehaničkih karakteristika zasipa, kao i od uloge koju konstrukcija od zasipnog materijala ispunjava u toku dalje eksploatacije i po završetku eksploatacije ležišta.

Pri potpunom otkopavanju ležišta (otkop uz predhodni zapunjeni otkop), u krovini ležišta, u blizini otkopa, obrazuje se zona smanjenog pritiska (rasterećenja), a u rudnom masivu ispred fronta napredovanja

otkopa pojavljuje se zona povišenog oslonačkog pritiska sl. 1. Sa povećanjem širine otkopanog prostora i zapunjenoj prostora, stene krovine i zasip u zapunjenoj prostoru ponašaju se kao okolne stene i popustljiva podgrada, dok zasip ne primi celokupno opterećenje stuba krovinskih stena. Opterećenje na otkopu potiče od ploče stena krovine, koja se jednim delom oslanja na zasipani deo otkopa, a drugim delom na rudni masiv. Dimenzije zone rasterećenja su proporcionalne deformacionim karakteristikama zasipa  $\varepsilon$ . Deformaciona karakteristika zasipa zavisi od vrste zasipa i načina ugradnje. Pri  $\varepsilon \leq 3\%$  pomeranje nalegajućih stena vrši se povijanjem bez pucanja i komadanja. Pri  $\varepsilon \geq 3\%$  u krovini dolazi do pucanja i raslojavanja stena.

Vrednost koeficijenta koncentracije napona u rudnom masivu određuje se na osnovu širine otkopanog prostora  $L$  i koncentracije napona u rudnom masivu, po obrascima:

$$K_k = 2,1 - 1,1 e^{-(L/80)^{1,5}}$$

$$K_k = (0,8 l_e \cdot n + 14) H^{-0,33}$$

gde su:

$e$  - osnova prirodnog logaritma

$L$  - širina otkopanog prostora m,  $L = n \cdot l_e$

$l_e$  - širina otkopa (trake, sloja) u dobijanju (ekvivalentna stubna širina plafona otkopa)

$n$  - broj traka u jednovremenom dobijanju do postizanja kritične širine  
 $l_k = n \cdot l_e$

$H$  - dubina izvođenja radova za koju su vezani naponi u krovu;

$$\tau = \rho g H, (\text{Pa})$$

Ispitivanja su pokazala da maksimalni oslonački pritisak, pri širini otkopnog prostora  $L = 30 - 40$  m iznosi  $(1,5 - 1,6)\rho g H$ . Maksimum se nalazi na 15-20 m od čela otkopnog fronta, a širina opterećene zone iznosi oko 50 m. Zasipni materijal trpi opterećenje tek pri širini otkopanog prostora 40 - 60 m.

Pri otkopavanju ležišta ispod zasipa, zasipni materijal igra ulogu veštačke krovine, ispod koje se takođe obrazuje zona rasterećenja u zoni otkopa i zone oslonačkog pritiska na bokove ispred čela otkopnog fronta i u zapunjenoj prostoru. Opterećenje zavisi od sopstvene težine zasipa i pritisku krovinskih stena, ako su već pretrpele deformacije.

### 3. POTREBNA ČVRSTOĆA ZASIPA PRI OTKOPOVANJU KOMORA ZA ZAPUNJAVANJEM

Ekonomično otkopavanje masivnih siromašnih (niske vrednosti) rudnih ležišta primenom otkopnih metoda sa zapunjavanjem otkopanih prostora, može da se izvrši samo primenom visoko produktivnih otkopnih metoda. Jedna od njih može biti komorno stubna otkopna metoda sa magazioniranjem rude, zapunjavanjem komora po istakanju rude očvršćavajućim zasipom i naknadnim dobijanjem zaštitnih stubova rude istom otkopnom metodom, za koju treba izvršiti analizu potrebne čvrstoće zasipa (sl. 2.).

Potrebna čvrstoća zasipa može se posmatrati za tri stadijuma u kojima se može naći stub od zasipnog materijala u otkopnom prostoru.

1. Kada se komora nalazi izmeđut zaštitnih stubova od rude (I stadijum).
2. Kada se komora nalazi između stuba od rude i stuba očvrslog zasipa susedne otkopane komore (II stadijum) ili zapunjenoj prostoru.
3. Kada se komora nalazi između zaštitnih stubova od očvrslog zasipa.

**1. U prvom stadijumu** zasip u komori neće biti opterećen nikakvim vertikalnim opterećenjem više ležećih stena, osim sopstvenom masom. Bočno opterećenje u stubu zasipa može se pojavitvi usled deformacija bokova komore. Stabilni raspon plafona komore ( $l_e$ ) određuje se iz strogih uslova stabilnosti rudničkih prostorija i otkopa, odnosno plafona komora.

Stabilnost potkopanog plafona prema krtičnim deformacijama određuje se iz uslova.

$$g_r > g_d$$

gde su:

$g_d$  - dopuštena deformacija plafona, pri kojoj je plafon komore stabilan.

$g_r$  - relativna deformacija plafona komore. Ona se određuje po formuli:

$$g_r = 1/[1+(H_R/l_e)^f]$$

$H_R$  - redukovana za uslove monolitnog masiva, dubina plafona komore

$$H_R = (1-K_g) H_k$$

$H_k$  - debljina krovine od nanosa na površini do ravni plafona komore

$K_g$  - koeficijent gubitka stabilnosti plafona zbog raspucalosti i strukturnih osobina stena (zavisno od RQD karakteristike). Njegova vrednost može biti određena na osnovu procenata izvađenog jezgra

$$K_g = 0,84 + 0,01 N_j - 0,0002 N_j^2$$

gde su:

$N_j$  - procenat izvađenog jezgra (često se prikazuje visoka vrednost)

$f$  - koeficijent čvrstoće stena po Protodjakonovu

$l_e$  - ekvivalentni stabilni raspon šupljine (širine) komore

Ekvivalentni stabilni raspon (širina) komore može biti određen, ako se usvoje granični uslovi, i formula reši eksplicitno po  $l_e$ .

$g < 0,001$  - stabilni raspon komore

$g = (0,001-0,04)$  - stanje između stabilnosti i potpunog zarušavanja

$g \leq 0,04$  - potpuno obrušavanje nalegaće krovine

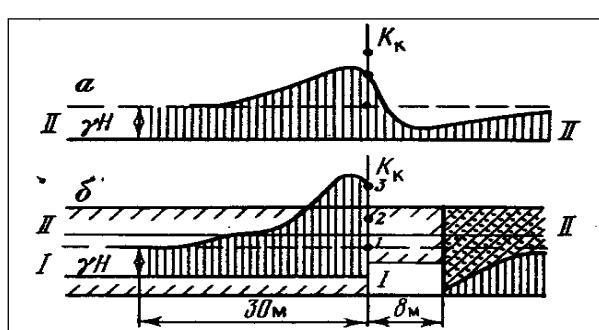
$$l_e = f \sqrt{\frac{g H_R^f}{1-g}} = H_R f \sqrt{\frac{g}{1-g}}, \text{ (m)}$$

Naponi će se koncentrisati u bokovima komore prema sl. 1.

Oni se neće prenositi na zasip u komori, ili čak i više komora, dok šupljina ispod podkopane krovine ne dostigne kritičan raspon (govori se o šupljini jer se pri zapunjavanju otkopa nikad neće potpuno poduhvatiti krovina).

$$l_k = H_k f \sqrt{\frac{g}{1-g}}, \text{ (m)}$$

pri  $g > 0,04$



Sl. 1. Grafik promene koncentracije napona u rudnom i masivu od zasipa

**2. Drugi stadijum** položaja komora u otkopavanju i zapunjenoj prostoru je najčešći. Pri eksploataciji velikih strmih rudnih tela, kritični raspon otkopanog prostora pri kome dolazi do zarušavanja kro-

vine, manji je od dužine otkopnog fronta. Zarušeni blokovi stena opterećivaće zapunjeni prostor. Ako je zasip stišljiv (plastičan) doći će do većih deformacija u krovini, pa čak i do deformacija zemljinje povr-

šine (kod pličih ležišta). Ipak zapunjeni prostor predstavlja zonu rasterećenja. Pri kretanju otkopnog fronta od periferije rudnog tela, prema prostorijama otvaranja, mogu se prijaviti sledeći slučajevi rasporeda napona:

a) Iznad prvih otkopanih komora pri širini otkopanog prostora  $L = nl_e < l_k$  (stabilne ekvivalentne širine) u krovini otkopa pojavljuju se zatezni naponi, a nabokovima otkopa i neporemećenih stena koncentrišu se naponi pritiska, zavisno od širine otkopanog prostora. Koeficijent koncentracije napona

određuje se po formuli za  $K_k$ , pa vertikalni napon u masivu iznosi:

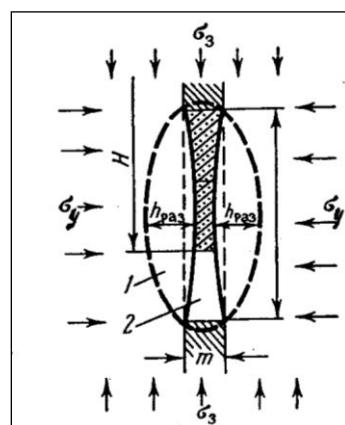
$$\sigma_p = K_k \rho_s g H, \text{ (Pa)}$$

Horizontalni napon  $\sigma_y$  na boku komore prema slici 2. iznosi:

$$\sigma_y = \frac{\mu}{1-\mu} K_k \rho_s g H, \text{ (Pa)}$$

gde je:

$\mu$  - koeficijent Pausona  $\mu = (0,4 \div 0,6)$   
(koeficijent bočnog opterećenja)



Sl. 2. Šema za proračun napona iz zaštitnih stubova na zasip u komori

Koeficijent koncentracije napona kako ispred čela otkopnog fronta u rudniku, tako i u krajnjim stubovima od zasipa povećavaće se sa otkopavanjem svake naredne komore, dok raspon otkopanog prostora ne pređe kritičnu širinu  $L > l_k$ .

b) Kada bude otkopano više komora, tako da raspon otkopanog prostora  $L$  postane nestabilan ili se zaruši, doći će do pojave vertikalnog napona i u masivu od zasipa. Veličina vertikalnog napona koji se može pojaviti u veštačkim stubovima od zasipa proračunava se koristeći princip istovremene deformacije kombinovanih oslonaca, stubova od rude i stubova zasipa po formuli:

$$\sigma_1 = \frac{K_a \rho_s g H S_k}{10^6 (S_z + 0,77 S_p \frac{E_s}{E_z})} + 10^{-6} \rho_z g h_z$$

gde su:

$\rho_s$ ;  $\rho_z$  - gustine stenskog materijala i zasipnog materijala

$H$  - dubina plafona otkopanog prostora

$S_k$ ;  $S_z$  - površine stubova rude i stubova od zasipa

$E_s$ ;  $E_z$  - moduli deformacije stena rudnog ležišta i zasipnog materijala

$K_a$  - koeficijent uticaja ugla nagiba ležišta na opterećenje zasipa

$$K_a = \cos^2 \alpha - \eta \sin^2 \alpha ; \eta = \mu / (1 - \mu)$$

$h_z$  - visina stuba od zasipa (visina otkopanog i zapunjeno prostora)

$\alpha$  - ugao nagiba ležišta (nagib zapunjene šupljine).

Čvrstoća zasipa u otkopanom prostoru mora biti veća od vertikalnog naponu koji se pojavljuje u zasipu, da ne bi došlo do popuštanja i sabijanja zasipa i dalje deformacije krovine.

$$\sigma_z > \sigma_1$$

Kod dubokih tankih ležišta može se dopustiti i sabijanje zasipa do određene visine, pri kojoj neće doći do nedopuštenih deformacija zemljine površine i smanjenja koeficijenta sigurnosti K [4].

c) Krajnji slučaj drugog stadijuma pojavljuje se pri kretanju otkopnog fronta tako da se dobijanje komora vrši između masiva rude i masiva zasipa. Krovina se oslanja na otkopni front rude, sa konzolom ne oslonjene krovine na zasip dužine  $l < l_c$ ;  $l < n \cdot l_c$  i dela krovine koji je popustio pod naponom višeletećih masa. Komora u otkopavanju se nalazi u zoni ispod konzole, gde su vertikalni naponi smanjeni. Maksimalni vertikalni napon se nalazi ispred otkopnog fronta u rudnom masivu. I za komore u otkopavanju na rastojanju  $l < l_c$  nalazi se zona smanjenog vertikalnog naponu. Na rastojanju  $L > l_c$  i masiv zasipa se nalazi pod koncentrisanim vertikalnim naponom istim kao u rudnom masivu.

Za iznalaženje potrebne čvrstoće zasipa za očuvanje zemljine površine od deformacija potrebno je uzeti u obzir moguće dopušteno sabijanje zasipa pri kome neće doći do oštećenja zemljine površine.

Za slepa izolovana ležišta pravilnog oblika, uticaj dimenzija (visine) otkopanog i zapunjeno područja na deformaciju (sleganje) zemljine površine u zavisnosti od kompresionih svojstava zasipa ocenjuje se na osnovu koeficijenta sigurnosti, čija vrednost treba da bude veća od dopuštene prema tabeli 1 [5].

$$K_s > K_d = H / \Delta P$$

Vertikalna prihvatljiva veličina deformacije zasipanog prostora  $\Delta P$  određuje se po formuli:

$$\Delta P = \varepsilon_o h_z (1-e) \sigma_1 / \sigma_z, \text{ (m)}$$

gde su:

$\Delta P$  - smanjenje visine stuba od zasipa pod opterećenjem  $\sigma_1$ , (m)

$\sigma_1$  - dejstvojući vertikalni napon, (Pa)

$\varepsilon_o$  - deformaciona karakteristika određene vrste zasipa

$h_z$  - debљina (visina) stuba zasipa

$\sigma_z$  - čvrstoća zasipa na pritisak

$K_s$  - koeficijent sigurnosti kojim se ocenjuje stabilnost krovine

Iz prethodne formule može se izračunati potrebna ili dovoljna čvrstoća zasipa  $\sigma_z$  za tanka duboka ležišta, kod kojih će usled opterećenja krovine zasip biti preopterećen i delimično sabijen. Dopušteno sabijanje zasipa biće  $\Delta P = H/K_d$ , a potrebna čvrstoća zasipa  $\sigma_z$ :

$$\sigma_z = \frac{\sigma_1 \ln \cdot \varepsilon_o h_z}{\ln(\Delta P)}, \text{ (Pa)}$$

3. Stadijum kada se vrši otkopavanje zaštitnog stuba ili komore koja se nalazi između zaštitnih stubova od očvrslog zasipa (u zasipu) je najopasniji, jer u stubovima dolazi do koncentracije napona sa obe strane iz otkopanih prostora. Naponi se sabiraju, a mogu se proračunati po formulama za  $\sigma_p$  i  $\sigma_y$ . U pripremnim prostorijama može doći do ispoljavanja dinamičkih pojava i gorskih udara. Do gorskih udara neće doći ako stena stuba nije sklona akumulaciji energije elastične deformacije i ako su koncentrisani naponi manji od čvrstoće stene na pritisak  $\sigma_p < \sigma_{cs}$ .

Do ispoljavanja gorskih udara neće doći i ako zasip u zapunjrenom prostoru ima odgovarajući pritisnu čvrstoću, tako da može da izvrši ukrućenje stuba rude i obezbedi stabilnost otkopne komore pri otkopavanju. Normativa pritisna čvrstoća zasipa u fazi dobijanja komora između stubova od zasipnog materijala treba da iznosi:

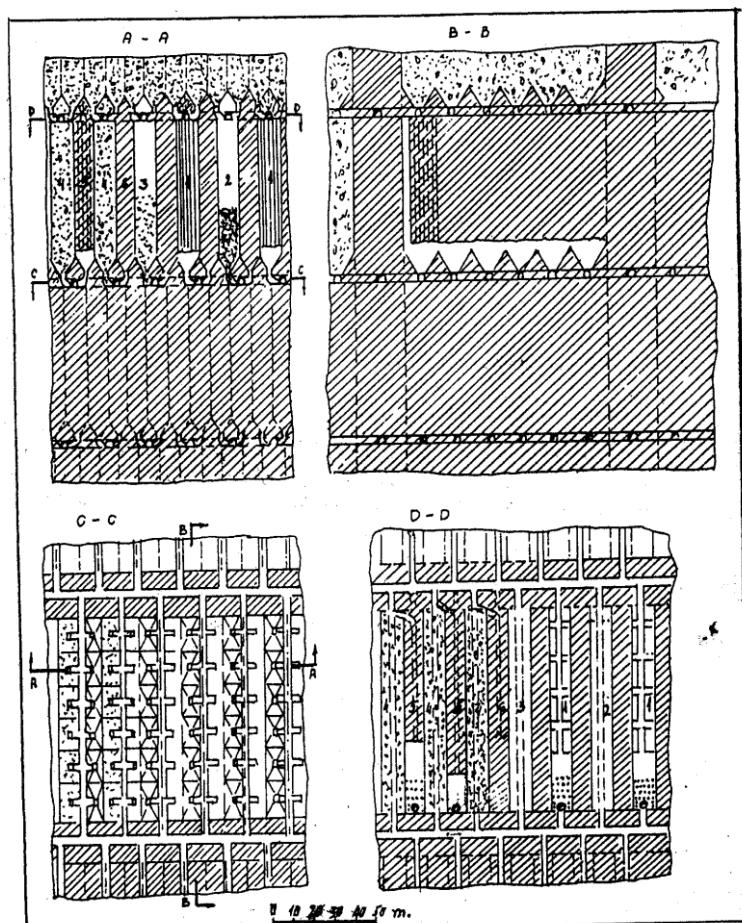
$$\sigma_z = \frac{\sigma_s K_z}{K_f \cdot K_o}$$

gde su:

$$\sigma_s = K_a K_{hp} g H \cdot L_s / 10^6 L_z - \text{napon u stubovima zasipa}$$

$K_z$  - koeficijent sigurnosti  $K_z = (1,5-3)$

$K_f$  - koeficijent forme stuba. S obzirom na uticaj oblika dimenzija stuba na noseću sposobnost  $[K_f = (a/h_s)^{0,5}]$  pri  $a > h_s$  ili  $[K_f = 0,6 + 0,4 a/h_s]$  pri  $a < h_s$ ;



Sl. 3. Otkopavanje sa zapunjavanjem komora i naknadnim dobijanjem stubova

Tabela 1. Koeficijenti sigurnosti

Kategorija objekata na površini	Dopuštene horizontalne deformacije (mm/m)	$K_d$ - za ležišta	
		Rudna	Ugljena
I	2,0	150	300
II	3,5	100	200
III	5,5	50	100

$a$  - širina stuba zasipa,

$h_s$  - visina stuba od očvršćavajućeg zasipa

$K_o$  - koeficijent kojim se uzima u obzir povećanje čvrstoće stubova na pritisak usled sabijanja;  $K_o = \sigma_k / \sigma_o$

H - dubina gornje površine stuba  
 $K_h$  - koeficijent kojim se uzima u obzir  
 stepen opterećenja stuba zasipa  
 obrušenim stenama krovine  
 $L_p$  - širina panela bloka (komore) u zasipu  
 $L_z$  - širina panela veštačkih stubova od  
 zasipa

Za neistražene "in situ" uslove  $K_h=0,5$

$\frac{L}{H} < 1$ , a za komore između stubova od  
 $H$   
 zasipa koje nisu zapunjeno  $K_h=L / h < 1$ ,  
 gde je  $L$  - širina komore (potkopanog stu-  
 ba).

Čvrstoća zasipnog materijala za obezbe-  
 đenje stabilnosti horizontalnih prostorija  
 odnosno, projektovanih raspona prostorija u  
 zasipu određuje se po formuli:

$$\sigma_e = K_z [0,49 \rho g H_z \cos \alpha (0,95 - e^{-0.06a}) - 1,76] \text{ Pa}$$

Izbor dimenzija komora i stubova i  
 njihovog rasporeda pri otkopavanju, čvrs-  
 toće zasipa kod komorno stubne otkopne  
 metode sa magazioniranjem rude i nakna-  
 dnim zapunjavanjem odkopa očvršćava-  
 jućim zasipom, ako se otkopava više hori-  
 zonata treba da se izvrši po formulama za  
 $\Delta P$  i  $\sigma_z = f(\Delta P)$ . U njima će doći do izmena  
 vrednosti veličina.  $H_z = N h_H$ ;  $H_z$ - visina zasi-  
 panog prostora zavisi od  $N$  visina otkopanih  
 horizonata  $h_H$ . Dopuštena deformacija  
 zasipnog prostora  $\Delta P' = (\Delta_1 + \Delta_2 + \Delta_3)N$  ne za-  
 visi od elastične deformacije (10 mm) kro-  
 vine svakog horizonta  $\Delta_1$  nepotpunog zapu-  
 njavanja komora oko 1%  $\Delta_2$ , i sabijanja za-  
 sipa usled opterećenja  $\Delta_3 = \epsilon_o h_H$ , kao i pro-  
 mene vertikalnog napona  $\sigma_1$ .

$$\sigma_1 = K_v K_v \rho g H_s$$

$$\Delta_p' = H_{sr} / K_d$$

$$\sigma_z = \sigma_1 \cdot \ln \epsilon_o \cdot N_h h_H / \ln \Delta P'$$

Pored poznatih oznaka  $K_v$  - koeficijent  
 kojim se uzima promena napona u zasipu u  
 zavisnosti od odnosa širine rudnog tela i  
 dubine ležišta  $K_v = (A_R / H_s) + 0,61$ ;  $A_R$ -dimen-  
 zija rudnog tela po pružanju ili padu.

Iz ovih formula vidi se da je za zaštitu  
 zemljine površine od deformacija pored  
 čvrstoće zasipa, bitan parametar njegova  
 stišljivost, jer čvrstoća zasipa na pritisak  
 može biti i manja od vertikalnog napona.  
 Pri  $\Delta P' = \epsilon_o N_h h_H$ ;  $\sigma_z = \sigma'$ .

## ZAKLJUČAK

Za poznatu geometriju ležišta, fizičko-  
 mehaničke karakteristike stena ležišta i  
 pratećih stena krovine i podine, kao i ciljeva  
 koji se žele postići, primenom komorno  
 stubne otkopne metode sa magazioniranjem  
 rude i zapunjavanja otkopanih komora  
 nakon istakanja rude, očvršćavajućim zasi-  
 pom, u cilju dobijanja zaostalih zaštitnih  
 stubova iz zasipa, prema slici 3 moguće je  
 na osnovu razmotrenog uzajamnog rada  
 stena ležišta i zasipa u zapunjениm komo-  
 ramama odabratи najpovoljniju dinamiku otko-  
 pavanja ležišta, raspored otkopa, zasipni  
 materijal odgovarajuće čvrstoće i stišljivosti,  
 itd.

## LITERATURA

- [1] D. M. Broninkov i sarad., Backfill works in the mines Nedra, Moscow, Russia 1989, p. 146. (In Russian)
- [2] V. I. Homyakov, Foreign experience tab in the mines Nedra, Moscow, Russia, 1984, p. 143. (In Russian)
- [3] V. R. Imenitov, V. F. Abramov, V. V. Popov, Localization of emptiness in the underground ore mining (In Russian), Nedra, Moscow, Russin, 1983, p. 72.
- [4] M. Miljković, R. Stanojlović, J. Soko-  
 lović, Sigurnosne i deformacione  
 karakteristike zasipnih materijala u  
 rudnicima, Rudarski radovi, Bor,  
 2(2012), str. 13-28.
- [5] V. Jovičić, M. Miljković, J. Nujić,  
 H. Uljić, M. Vukić, Sigurnost i tehnici-  
 ka zaštita u rудarstvu, Tuzla, Uni-  
 verzal, 1987, p. 423.

*Daniel Kržanović\*, Nenad Vušović\*\*, Zoran Vadiuvesković\*, Milenko Ljubojev\**

## **ANALYSIS THE LONG-TERM DEVELOPMENT OF THE OPEN PIT NORTH MINING DISTRICT MAJDANPEK FOR THE CAPACITY OF $5 \times 10^6$ TONS OF ORE ANNUALLY\*\*\***

### **Abstract**

*The work presents a consideration of a long-term development of the open pit North Mining District in terms of achieving maximum profit for the planned capacity of 5 million tons of copper ore annually, using the modern software Whittle for strategic planning of production. Software provides the ability to achieve a positive development of cash flow and maximum net present value by optimization the excavation limit and long-term mining dynamics. For planned technical and economic parameters, which are the input data for analysis, the boundary of the open pit is obtained for the service life of 26 years, and the value of the net present value is \$ 252,591,906.*

**Keywords:** open pit North Mining District Majdanpek, optimization, development phase of open pit, cash flow, net present value, software Whittle

### **INTRODUCTION**

Within the company, Copper Mine Majdanpek, which is part of the company Mining and Smelting Basin Bor (RTB Bor), there are two open pit mines as well as the North Mining District and South Mining District. Since the deposit stripping is done at the open pit South Mining District, the holder of copper ore production in recent years is the North Mining District with a capacity of 3.5 million tons per year. The construction of a new smelter in Bor It is necessary to provide the raw material for operation the New Smelter in Bor through increasing the capacity of excavation at open pit mines operating within RTB Bor. Due to this, an analysis of possibilities for long-term mining of copper ore at the open pit North

Mining District Majdanpek for a capacity of 5 million tons per year, which includes:

- 1) optimization the open pit and selection the optimum contour of open pit
- 2) defining the mining phase (push-backs)
- 3) optimization the mining dynamics
- 4) economic analysis in the Whittle software, which is based on an analysis of trends the discounted cash flow over the mining period, or the realized net present value, and that is an indicator of achieved economic results of mining the North Mining District for the given initial conditions.

\* Mining and Metallurgy Institute Bor, e-mail: daniel.krzanovic@irmbor.co.rs

\*\* University of Belgrade, Technical Faculty Bor

\*\*\* This work is the result of the Project TR 33038: Improvement the Technology of Exploitation and Processing of Copper Ore with Monitoring the Environment in RTB Bor Group, funded by the Ministry of Education, Science and Technological Development of the Republic of Serbia

Techno-economic analysis was carried out for the part of the copper deposits "North Mining District - Majdanpek" and deposit of polymetallic mineral resources (Zn-Pb-Cu) "Tenka - North Mining District Majdanpek" in the software Whittle.

## **TECHNO-ECONOMIC PARAMETERS FOR ANALYSIS**

A long term development of the open pit is defined on the basis of the following initial techno-economic parameters [1].

### 1 Mining recoveries and dilutions

- Dilution of copper ore 4.0%
- Dilution of lead-zinc ore 6.0%
- Exploitation losses of copper ore 4.0%
- Exploitation losses of PbZn ore 6.0%

### 2 Flotation recoveries:

Cu ore:

- Cu recovery 82.0%
- Ag recovery 50.0%
- Au recovery 50.0%

Pb-Zn ore:

- Zn recovery 60.0%
- Pb recovery 60.0%
- Ag recovery 51.5%
- Au recovery 35.0%

### 3 Metallurgical recoveries:

Cu concentrate:

- Cu recovery 95.0%
- Ag recovery 90.0%
- Au recovery 90.0%

Pb-Zn concentrate:

- Zn recovery 96.5%
- Pb recovery 95.0%
- Ag recovery 90.0%
- Au recovery 90.0%

### 4. Selling prices of metals:

- Copper (Cu) 6,000 US \$/t
- Silver (Ag) 800 US \$/kg
- Gold (Au) 30,000 US \$/kg

- Zinc (Zn) 1,800 US \$/t
- Lead (Pb) 1,800 US \$/t

### 5 Metal values in concentrate:

Cu concentrate:

- Copper (6.000 – 600) = 5,400 US \$/t,
- Gold (30.000 – 150) = 29,850 US \$/kg
- Silver (800 – 15) = 785 US \$/kg

Pb-Zn concentrate:

- ❖ Zinc (1,800×0.55) = 990 US \$/t
- ❖ Lead (1,800×0.55) = 990 US \$/t
- ❖ Gold (30,000×0.93) = 27,900 US \$/kg
- ❖ Silver (800×0.88) = 700 US \$/kg
- ❖ Profit 0.55%

### 6 Mining costs:

- ❖ Ore and waste mining 2.0 US \$/t excavation

### 7 Flotation costs:

- Cu flotation 4.0 US \$/t ore
- Pb-Zn flotation 6.0 US \$/t ore

### 8 Metallurgical treatment costs:

- Cu concentrate: 600 US \$/t concentrate
- Pb-Zn concentrate: 0.45 %

### 9 Adopted discount rate 10%

## **CAPACITY OF MINING AND DISPOSAL**

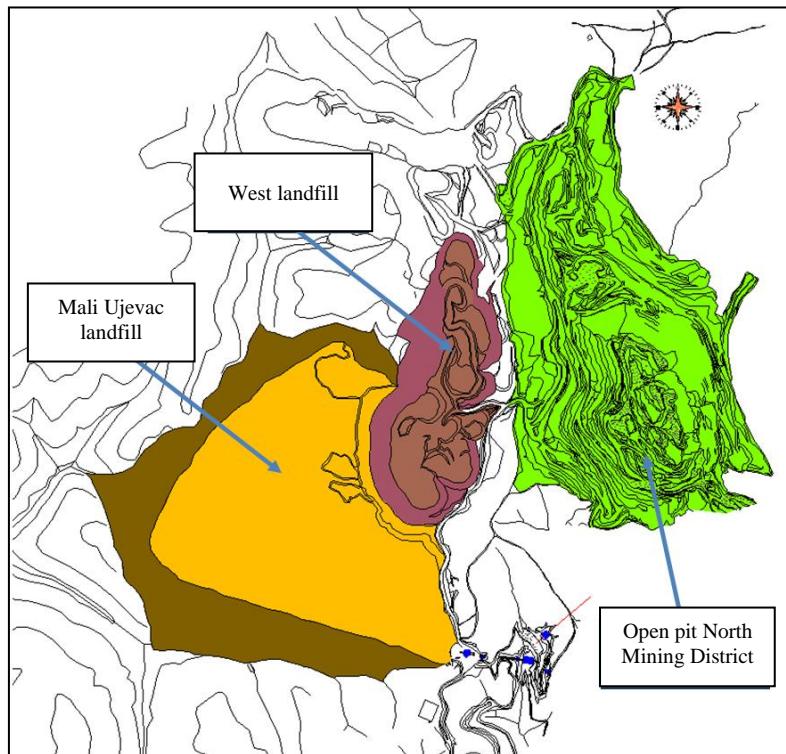
The planned value of ore mining capacity per annum is as follows:

- in the 1<sup>st</sup> year of 3,000,000 t of ore
- from the 2<sup>nd</sup> year until the end of exploitation period 5,000,000 t of ore

Capacity of waste mining is limited to 16 million tons in the first year of operation. From the second to the fourteenth year, the

mining capacity of waste is 14 million tons per year, and then has steadily declined, except for the period from the eighteenth to the twentieth year when it is at the level of 12 ÷ 13 million tons (Table 3).

Figure 1 shows the landfill Mali Ujevac and West landfill. The spatial capacity of these landfills allows accommodation of the total amount of waste that is mined during the exploitation period.

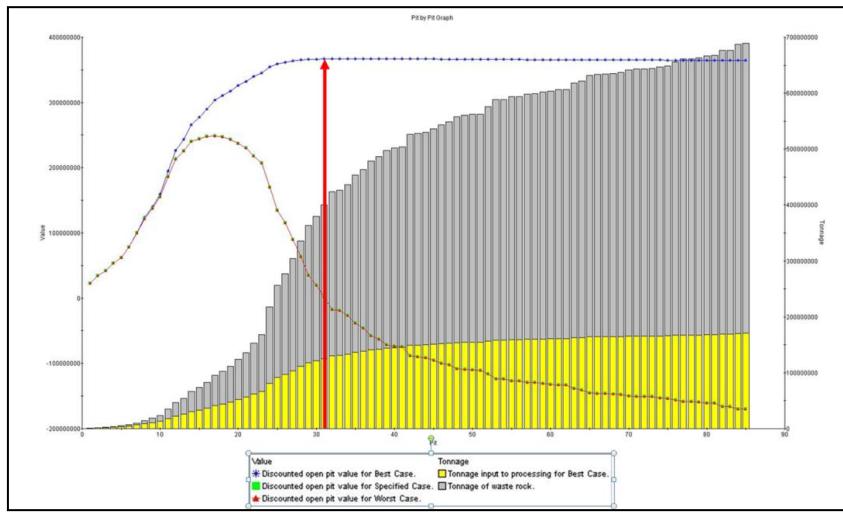


**Figure 1** View the landfill location of the open pit North Mining District

## OPTIMIZATION THE BOUNDARY OF THE OPEN PIT

An optimal boundary of open pit mining for the established techno - economic parameters was determined using the software Whittle for optimization and strategic planning of the open pits [2], [3]. The software generates several possible optimal contours of the open pits, using the revenue factor

(Revenue Factor). The obtained open pits (85 open pits were generated and shown in Table 1 and Figure 2) are further analyzed and selection of optimum open pits is done according to the criteria of discounted present value. The open pit No.31 was selected for further consideration [4].



**Figure 2** Graphical presentation the optimization results of open pit and selection the optimal contour

**Table 1** Results of open pit optimization and selection the optimal contour

Kop	Faktor prihoda	Cena metals (Cu)	Ruda	Jalovina	Izkopine	Novčani tok best	Novčani tok specified	Novčani tok worst	Kop	Faktor prihoda	Cena metals (Cu)	Ruda	Jalovina	Izkopine	Novčani tok best	Novčani tok specified	Novčani tok worst
(S)	(S)	(S)	(S)	(S)	(S disc)	(S disc)	(S disc)	(S)	(S)	(S)	(S)	(S)	(S)	(S)	(S disc)	(S disc)	(S disc)
1	0.30	1.800	948.181	203.712	1.171.893	22.594.298	22.594.298	22.594.298	43	1.14	8.640	149.446.138	378.583.793	528.049.931	364.614.915	-99.778.395	-99.718.295
2	0.32	1.920	1.023.349	450.874	2.074.723	34.312.916	34.312.916	34.312.916	44	1.16	9.660	150.016.034	378.958.771	529.974.805	366.595.864	-91.100.702	-91.100.702
3	0.34	2.040	2.122.198	606.769	2.729.987	41.789.193	41.789.193	41.789.193	45	1.18	10.680	150.850.043	385.656.957	536.507.000	366.104.741	-94.941.362	-94.941.362
4	0.36	2.160	2.929.255	1.092.474	4.021.723	53.519.236	53.519.236	53.519.236	46	1.20	1.200	151.819.471	391.796.162	543.615.833	368.423.017	-99.707.899	-99.707.899
5	0.38	2.280	3.659.220	1.181.582	4.948.782	62.533.173	62.494.501	62.494.501	47	1.22	1.220	152.797.499	395.913.738	548.710.877	368.360.418	-101.886.755	-101.886.755
6	0.40	2.400	4.909.725	2.181.611	7.084.338	79.708.554	78.355.255	78.355.255	48	1.24	1.440	154.049.441	404.049.912	558.144.753	368.242.969	-108.521.832	-108.521.832
7	0.42	2.520	7.071.198	1.860.726	10.232.122	100.864.035	99.650.269	99.650.269	49	1.26	1.560	154.593.811	405.961.093	560.554.904	368.208.247	-109.366.215	-109.366.214
8	0.44	2.640	9.286.522	5.407.075	13.821.914	131.872.114	121.872.114	121.872.114	50	1.28	1.780	154.781.049	407.179.922	561.960.971	368.188.588	-110.048.394	-110.048.394
9	0.46	2.760	11.047.158	7.406.538	18.473.434	140.101.765	137.641.892	137.641.892	51	1.30	1.800	154.934.895	407.043.052	562.777.947	368.167.200	-110.353.097	-110.353.097
10	0.48	2.880	13.157.839	10.175.045	23.323.284	159.269.009	155.303.894	155.303.894	52	1.32	1.920	158.993.452	419.211.707	576.203.159	365.977.282	-116.030.127	-116.030.127
11	0.50	3.000	17.927.373	16.172.168	34.400.141	194.154.291	186.303.811	186.303.811	53	1.34	1.940	158.440.134	419.799.959	588.239.093	365.812.883	-127.772.883	-127.772.883
12	0.52	3.120	22.771.807	23.883.135	46.594.942	226.403.894	219.021.965	219.021.965	54	1.36	1.960	158.496.574	429.947.701	588.444.375	365.809.317	-123.864.338	-123.864.338
13	0.54	3.240	25.863.252	28.182.938	54.045.648	246.162.348	228.051.272	228.051.272	55	1.38	1.980	159.558.554	434.347.740	593.905.302	365.731.291	-124.450.957	-124.450.957
14	0.56	3.360	30.724.154	35.998.077	66.722.231	246.819.394	240.625.139	240.625.139	56	1.40	2.040	159.592.857	434.537.270	594.133.127	365.719.666	-124.794.454	-124.794.454
15	0.58	3.480	33.471.174	40.271.847	73.749.020	277.037.488	244.277.282	244.277.282	57	1.42	2.120	160.056.057	437.834.259	597.800.316	365.664.818	-128.710.097	-128.710.098
16	0.60	3.600	37.192.913	45.485.293	82.678.200	289.634.825	247.798.051	247.798.051	58	1.44	2.140	160.326.982	438.293.394	598.418.379	365.638.059	-129.382.131	-129.382.131
17	0.62	3.720	41.443.509	53.842.430	95.181.988	288.020.909	248.831.219	248.831.219	59	1.46	2.160	160.579.643	441.490.045	602.069.688	365.603.014	-130.873.99	-130.873.99
18	0.64	3.840	44.205.138	58.448.831	102.653.945	31.021.840	247.430.866	247.430.866	60	1.48	2.180	160.755.530	442.824.454	603.759.992	365.580.228	-131.900.169	-131.900.169
19	0.66	3.960	47.502.046	64.495.512	111.997.854	317.442.656	243.140.799	243.140.799	61	1.50	2.200	161.049.360	443.038.006	608.087.366	365.542.337	-132.029.393	-132.029.393
20	0.68	4.080	52.113.561	71.835.689	123.949.210	325.693.173	237.056.588	237.056.588	62	1.52	2.220	161.058.864	445.077.720	608.136.587	365.541.347	-133.068.655	-133.068.655
21	0.70	4.200	56.271.861	79.412.771	135.694.452	332.198.250	230.075.446	230.075.446	63	1.54	2.240	161.495.935	445.211.290	618.211.233	365.537.655	-134.432.927	-134.432.927
22	0.72	4.320	60.823.345	83.403.094	155.514.469	339.836.560	218.071.798	218.071.798	64	1.56	2.260	163.095.722	458.854.209	621.649.931	365.302.145	-140.311.918	-140.311.918
23	0.74	4.440	66.812.254	101.754.105	168.166.519	345.104.837	207.145.843	207.145.843	65	1.58	2.280	163.216.904	467.153.477	631.056.151	365.154.330	-146.380.524	-146.380.524
24	0.76	4.560	81.051.136	147.438.453	217.487.589	354.419.784	170.356.756	170.356.756	66	1.60	2.300	164.397.954	468.929.719	633.327.673	365.133.146	-145.788.727	-145.788.727
25	0.78	4.680	91.336.045	164.730.023	256.071.090	359.948.432	134.987.260	134.987.260	67	1.62	2.320	164.131.945	469.717.084	634.238.089	365.119.229	-146.339.169	-146.339.169
26	0.80	4.800	98.781.198	180.400.615	277.181.814	361.514.658	115.608.954	115.608.954	68	1.64	2.340	164.640.566	470.502.220	635.142.786	365.105.246	-146.775.402	-146.775.402
27	0.82	4.920	103.609.177	200.782.071	304.382.248	383.567.349	89.619.201	89.619.201	69	1.66	2.360	165.335.210	476.023.343	641.358.562	365.014.381	-149.455.086	-149.455.086
28	0.84	5.040	111.265.888	223.954.422	335.220.307	409.420.437	865.774.873	865.958.872	70	1.70	2.380	165.542.870	478.091.662	643.434.532	364.983.174	-150.521.876	-150.521.876
29	0.86	5.160	117.624.186	246.649.397	365.774.008	461.993.171	865.958.872	865.958.872	71	1.72	2.400	165.547.260	478.132.427	643.679.693	364.982.590	-150.534.725	-150.534.725
30	0.88	5.280	123.760.039	281.450.437	424.000.516	565.951.994	-16.975.216	-16.975.216	72	1.74	2.420	165.424.374	478.459.438	644.083.812	364.975.915	-150.924.026	-150.924.026
31	0.90	5.400	123.341.154	275.079.007	409.420.438	366.299.742	2.209.940	2.209.940	73	1.76	2.440	165.802.740	480.927.784	646.733.543	364.940.595	-152.992.138	-152.992.138
32	0.92	5.520	132.760.039	303.470.052	461.237.091	367.047.835	26.505.753	26.505.753	74	1.78	2.460	166.131.945	482.706.428	643.833.173	364.903.502	-155.443.235	-155.443.235
33	0.94	5.640	131.114.458	281.642.492	428.715.750	366.939.137	-18.886.084	-18.886.084	75	1.80	2.480	166.027.893	489.333.478	646.785.419	364.951.439	-156.132.521	-156.132.521
34	0.96	5.760	132.760.039	303.470.052	461.237.091	367.047.835	26.505.753	26.505.753	76	1.82	2.500	167.453.655	493.441.141	660.881.794	364.734.158	-159.135.513	-159.135.513
35	0.98	5.880	136.622.733	317.405.907	453.817.740	367.007.144	-38.381.700	-38.381.700	77	1.84	2.520	167.442.250	493.530.873	660.972.926	364.732.931	-159.407.791	-159.407.791
36	1.00	6.000	136.161.223	324.954.695	461.117.518	367.007.0291	-45.357.457	-45.357.457	78	1.86	2.540	167.446.540	493.530.873	664.977.624	364.737.223	-159.499.233	-159.499.233
37	1.02	6.120	140.499.913	337.397.211	479.398.544	-57.484.923	-57.484.923	80	1.90	2.560	168.322.556	498.800.288	667.122.844	364.640.649	-160.849.859	-160.849.859	
38	1.04	6.240	142.503.976	344.482.084	487.188.000	366.987.239	-52.747.899	-52.747.899	81	1.92	2.580	168.349.852	498.937.026	667.208.878	364.637.998	-160.888.912	-160.888.912
39	1.06	6.360	144.045.208	355.072.437	497.117.661	366.914.456	-71.308.357	-71.308.357	82	1.94	2.600	168.216.976	507.066.195	678.283.171	364.514.195	-161.887.727	-161.887.727
40	1.08	6.480	145.132.028	358.664.972	503.798.601	366.873.490	-73.811.424	-73.811.424	83	1.96	2.620	169.277.495	507.628.162	678.905.857	364.508.058	-165.824.049	-165.824.049
41	1.10	6.600	145.473.922	358.036.674	503.510.598	366.880.801	-74.384.990	-74.384.990	84	1.98	2.640	170.327.443	518.924.107	687.251.559	364.365.855	-169.860.134	-169.860.134
42	1.12	6.720	149.261.428	377.000.767	526.842.195	366.852.022	-83.298.985	-83.298.985	85	2.00	2.660	170.560.					

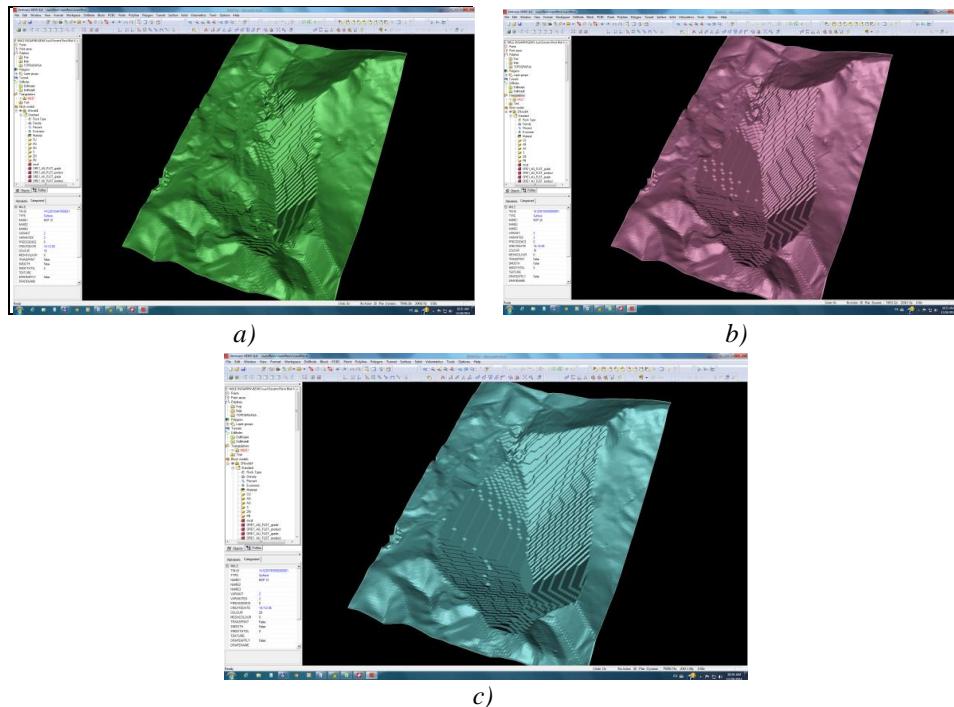
The results obtained in the software Whittle are shown in Table 2.

**Table 2** Results of defining the mining phases

Basic exploitation parameters	Mining phases (pushbacks)		
	Phase 1 (pushback 1)	Phase 2 (pushback 2)	Phase 3 (pushback 3)
Total amount of excavations, t	46 631 341	170 986 143	183 003 754
Total amount of overburden, t	23 883 136	112 553 318	138 642 554
Amount of ore, t	22 748 205	58 432 825	44 361 200
Cut-off grade of copper in the ore, % C <sub>u</sub>	0.100	0.100	0.100
Average copper content in the ore, % C <sub>u</sub>	0.385	0.291	0.302
Cut-off grade of zinc in the ore, % Z <sub>n</sub>	1.000	1.000	1.000
Average zinc content in the ore, % Z <sub>n</sub>	1.924	1.658	1.508
Overburden coefficient, t/t	1.050	1.930	3.130

View the final contours of development phases of the open pit, resulting in

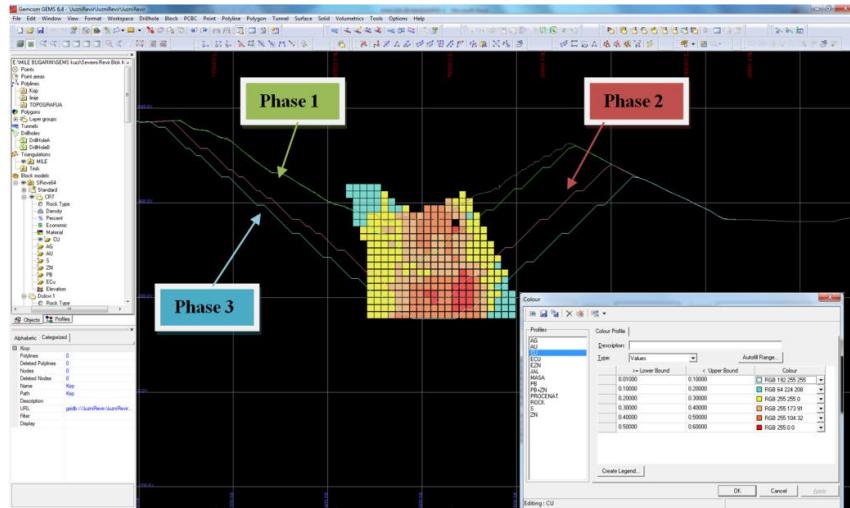
the software Whittle, is shown in Figure 3.



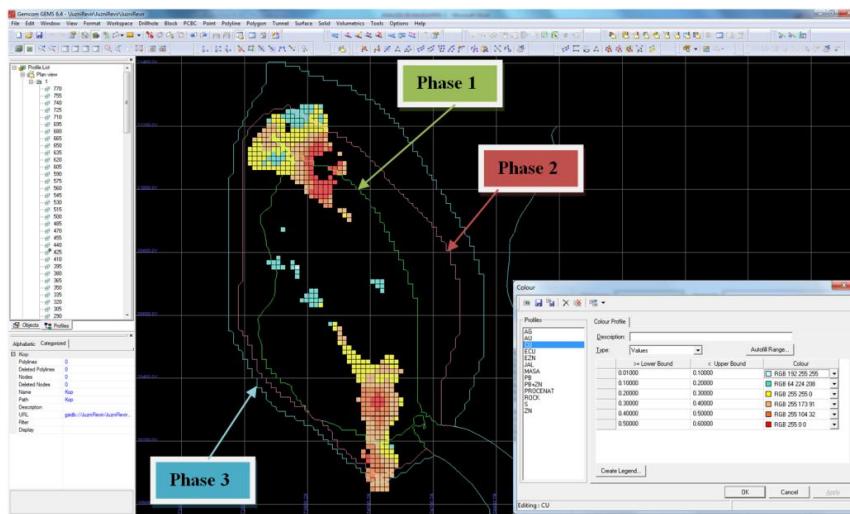
**Figure 3** View the final contours of development phases of the open pit (3D view)  
a) Phase 1, b) Phase 2, c) Phase 3

Figures 4 and 5 show the mining phases in the software Gemcom Gems where, in addition to the phase boundary, it is

also noticed the block model of metal content in the ore in the deposit North Mining District.



**Figure 4** Cross section of the open pit with a view of development phases of the open pit and block model of copper content (coordinates of the points X = 4973341 and Y = 7520652; X = 4974575 and Y = 7520652; azimuth v=90°)



**Figure 5** View the development phase of open pit and block model of copper content in the plan (level of floor E + 425)

## OPTIMIZATION THE MINING DYNAMICS

Mining dynamics by years of exploitation was obtained in the software Whittle, in the module New Schedule Graf. To optimi-

ze the mining dynamics, the software uses the Milava algorithm, which can operate in NPV mode when maximum net present

value (NPV) is required or in the balancing regime in which maximum utilization of production capacities in mining and flotation processing is required in the first years of

exploitation. A balancing regime (Milawa Balanced) was used in this work.

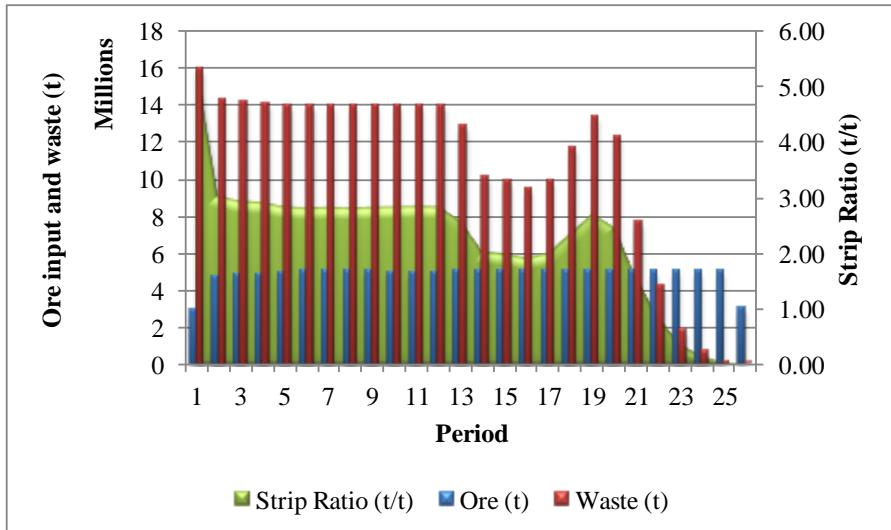
Results of optimization the mining dynamics are shown in Table 3.

**Table 3** Mining dynamics by years of exploitation with a view of cash flow

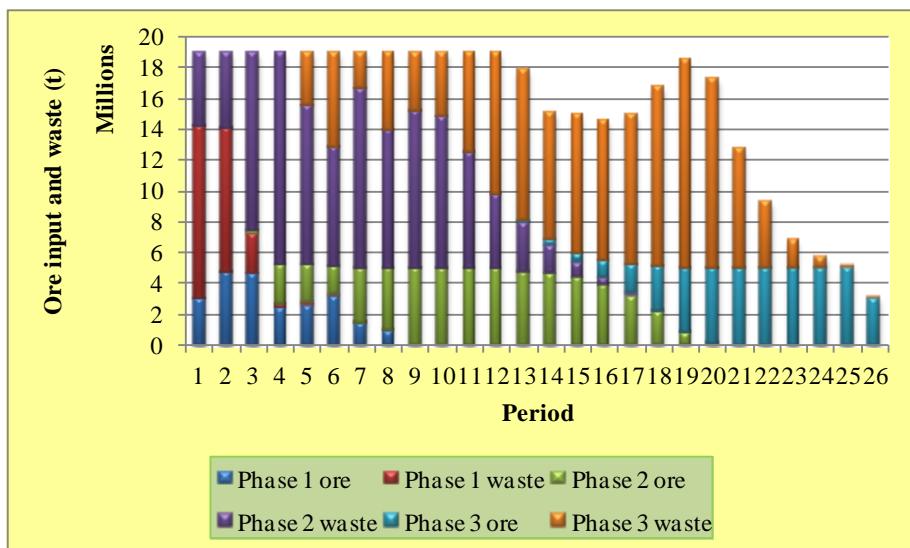
Year	Ore	Waste	Excavation	Overburden coefficient	Cash flow	Cash flow disc
	(t)	(t)	(t)	(t/t)	\$	\$
1	2 979 345	16 020 655	19 000 000	5.38	11 246 634	10 224 213
2	4 734 069	14 265 931	19 000 000	3.01	34 996 063	28 922 366
3	4 845 618	14 154 382	19 000 000	2.92	33 451 016	25 132 244
4	4 876 619	14 123 381	19 000 000	2.90	31 150 733	21 276 370
5	4 971 615	14 028 385	19 000 000	2.82	34 912 504	21 677 918
6	4 996 616	14 003 384	19 000 000	2.80	40 871 924	23 071 135
7	4 982 021	14 017 979	19 000 000	2.81	21 689 710	11 130 251
8	4 994 294	14 005 706	19 000 000	2.80	26 008 360	12 133 092
9	4 985 137	14 014 863	19 000 000	2.81	13 143 992	5 574 336
10	4 969 517	14 030 484	19 000 001	2.82	18 102 666	6 979 361
11	4 964 874	14 035 126	19 000 000	2.83	17 222 757	6 036 471
12	4 975 731	14 024 269	19 000 000	2.82	18 713 860	5 962 812
13	5 000 000	12 848 645	17 848 645	2.57	25 731 559	7 453 516
14	5 000 000	10 082 085	15 082 085	2.02	36 509 799	9 614 171
15	4 999 998	9 922 013	14 922 011	1.98	37 432 610	8 961 069
16	5 000 000	9 538 805	14 538 805	1.91	31 437 699	6 841 759
17	5 000 000	9 939 543	14 939 543	1.99	24 695 897	4 885 952
18	4 999 998	11 698 016	16 698 014	2.34	22 904 849	4 119 638
19	5 000 000	13 430 083	18 430 083	2.69	18 038 165	2 949 384
20	5 000 000	12 269 592	17 269 592	2.45	23 636 188	3 513 369
21	5 000 000	7 704 188	12 704 188	1.54	33 055 309	4 466 783
22	5 000 000	4 216 883	9 216 883	0.84	31 765 187	3 902 225
23	5 000 000	1 814 944	6 814 944	0.36	35 382 772	3 951 483
24	5 000 000	715 856	5 715 856	0.14	43 949 792	4 462 029
25	5 000 000	162 320	5 162 320	0.03	57 185 004	5 277 947
26	3 065 906	11 490	3 077 396	0.00	46 774 308	4 072 012
Total	125 341 358	275 079 008	400 420 366	2.19	770 009 357	252 591 906

Figure 6 presents the amount of ore and waste by years of exploitation with associated stripping ratio.

Figure 7 shows the changes in the amount of ore and waste by years of exploitation and development phases of open pit.



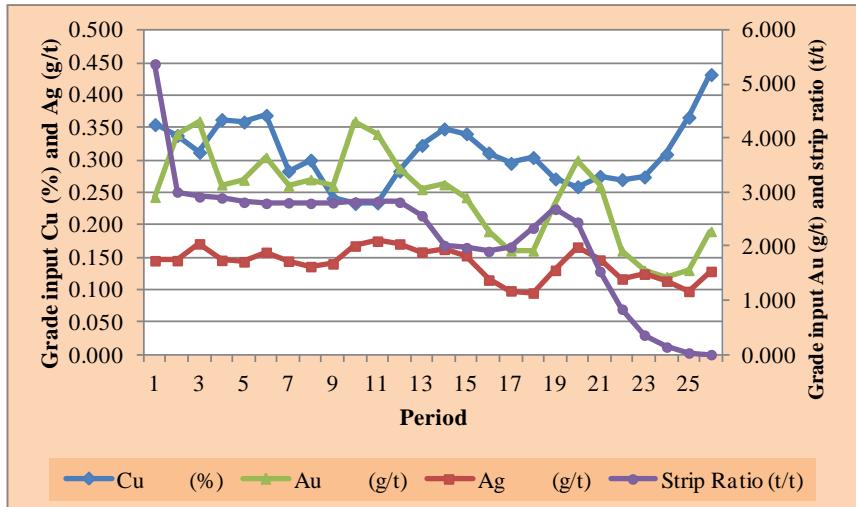
**Figure 6** Amount of ore and waste by years of exploitation with associated stripping ratio



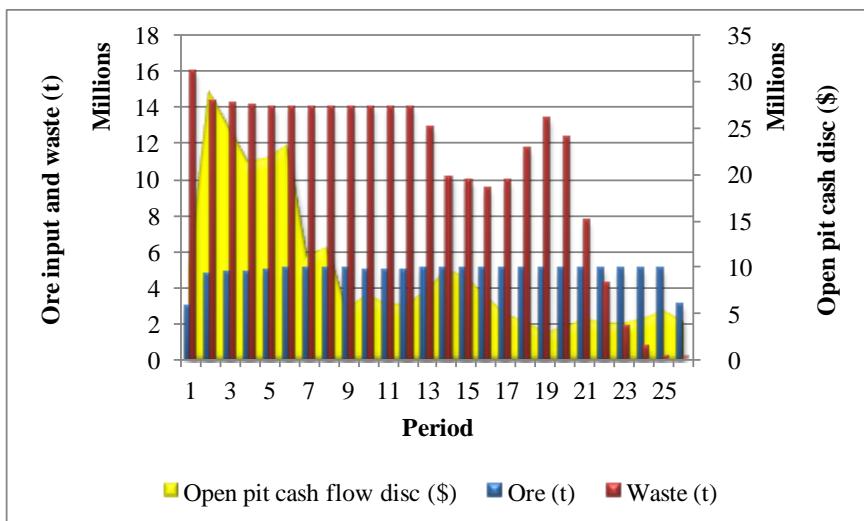
**Figure 7** Amounts of ore and waste by years of exploitation and development phases of open pit

Change of medium content of copper, silver and gold in copper ore and stripping ratio by years of exploitation can be read from the graph in Figure 8.

Figure 9 shows the movement of discounted cash flow and amount of ore and waste by years of exploitation.



**Figure 8** Change of medium content of copper, silver and gold in copper ore and stripping ratio by years



**Figure 9** Change of discounted cash flow and amount of ore and waste by years of exploitation

## CONCLUSION

Based on the carried out analysis, the following is concluded:

- 1) The specified capacity in copper ore mining at the open pit North Mining District Majdanpek of 5 million tons per year is achieved in the second year of operation. In the first year, the capacity is at the level of 3 million tons.
- 2) Service life of the open pit is 26 years.

- 3) The stripping ratio in the first year of exploitation is 5.38 t/t. From the second to the fourteenth year, this ratio has a value of around 2.8 t/y, and then steadily declines, except for a period from the eighteenth to the twentieth year when it is at approximately level of 2.5 t/t.
- 4) Movement in cash flow is positive during the whole period of exploitation.
- 5) The net present value is achieved in the amount of **\$ 252,591,906** (calculation in the software Whittle).

## REFERENCES

- [1] Elaborate on reserves of the Copper Deposit “South Mining District – Majdanpek” and Deposit of Polymetallic Mineral Resources (Zn-Pb-Cu) ”Tenka – North Mining District Majdanpek“, Mining and Metallurgy Institute Bor, 30/06/2011;
- [2] D. Kržanović, R. Rajković, M. Mikić: The Effect of Open Pit Slope Design on Net Present Value for Long Term Planning, The 46<sup>th</sup> International October Conference on Mining and Metallurgy, Bor Lake, Serbia, 2014;
- [3] G. Whittle, W. Stange and N. Hanson, Optimizing Project Value and Robustness, Project Evaluation Conference, Melbourne, Vic, 19 - 20 June 2007, pp. 1-10;
- [4] D. Kržanović, R. Rajković, M. Mikić: Application of Software Packages Gemcom and Whittle for Design in Mining Aimed to Rational and Cost-Effective Utilization the Copper Deposit Veliki Krivelj near Bor, Serbia, Mining Engineering, Mining and Metallurgy Institute Bor, 2012, pp. 91-98;
- [5] D. Kržanović, R. Rajković, M. Mikić, M. Ljubojev: Effect of Stage Development of Mining Operations on Maximization the Net Present Value in Long-Term Planning of Open Pits, Mining and Metallurgy Engineering Bor, 4/2014, pp. 33-40.

Daniel Kržanović\*, Nenad Vušović\*\*, Zoran Vadiuvesković\*, Milenko Ljubojev\*

**ANALIZA DUGOROČNOG RAZVOJA  
POVRŠINSKOG KOPA SEVERNI REVIR MAJDANPEK  
ZA KAPACITET  $5 \times 10^6$  TONA RUDE GODIŠNJE\*\*\***

*Izvod*

U radu je izvršeno sagledavanje dugoročnog razvoja površinskog kopa Severni revir sa aspekta ostvarivanja maksimalne dobiti za planirani kapacitet od 5 miliona tona rude bakra godišnje, primenom savremenog softvera za strateško planiranje proizvodnje Whittle.

Softver pruža mogućnost da se optimizacijom granice otkopavanja i dugoročne dinamike otkopavanja ostvari pozitivno kretanje novčanog toka i maksimalna neto sadašnja vrednost.

Za planirane tehnoekonomske parametre, koji su ulazni podaci za analizu, dobijena je granica površinskog kopa za vek eksploracije od 26 godina, a vrednost neto sadašnje vrednosti iznosi 252.591.906 \$.

**Ključne reči:** površinski kop Severni revir Majdanpek, optimizacija, fazni razvoj kopa, novčani tok, neto sadašnja vrednost, softver Whittle

**UVOD**

U okviru preduzeća Rudnik bakra Majdanpek, koji je deo kompanije Rudarsko topioničarski basen Bor (RTB Bor), posluju dva površinska kopa i to Severni revir i Južni revir. S obzirom da se na površinskom kopu Južni revir vrši raskrivanje ležišta, nosilac proizvodnje rude bakra poslednjih godina je kop Severni revir, sa kapacitetom oko 3,5 miliona tona godišnje. Izgradnjom nove topionice u Boru neophodno je obezbediti sirovinu za njen rad kroz povećanje kapaciteta otkopavanja na površinskim kopovima koji posluju u okviru RTB Bor. U tom cilju izvršena je analiza mogućnosti dugoročnog otkopavanja rude bakra na površinskom kopu Severni revir Majdanpek

za kapacitet od 5 miliona tona godišnje, koja obuhvata:

- 1) optimizaciju površinskog kopa i izbor optimalne konture kopa
- 2) definisanje faza otkopavanja (push-backs)
- 3) optimizaciju dinamike otkopavanja
- 4) ekonomsku analizu u softveru Whittle, koja se zasniva na analizi kretanja diskontovanog novčanog toka tokom eksploracionog perioda, odnosno ostvarene neto sadašnje vrednosti, i koja je pokazatelj postignutih ekonomskih rezultata eksploracije ležišta Severni revir za zadate početne uslove.

\* Institut za rudarstvo i metalurgiju Bor, e-mail: daniel.kržanovic@irmbor.co.rs

\*\* Univerzitet u Beogradu, Tehnički fakultet Bor

\*\*\* Ovaj rad je proistekao iz projekta TR-33038: Usavršavanje tehnologija eksploracije i prerade rude bakra sa monitoringom životne sredine u RTB Bor-Grupu, koji je finansiran sredstvima Ministarstva prosvete, nauke i tehnološkog razvoja Republike Srbije

Tehničko-ekonomska analiza izvršena je za deo ležišta bakra „Severni revir – Majdanpek“ i ležišta polimetaličnih mineralnih sirovina (Zn-Pb-Cu) „Tenka – Severni revir Majdanpek“ u sovveru Whittle.

## TEHNOEKONOMSKI PARAMETRI ZA ANALIZU

Dugoročni razvoj površinskog kopa definisan je na osnovu sledećih polaznih tehnokonomskih parametara [1].

### 1. Rudarska iskorišćenja i osiromašenja

- Osirašenje rude bakra 4,0%,
- Osirašenje olovo-cinkane rude 6,0%,
- Eksplotacioni gubici bakarne rude 4,0%,
- Eksplotacioni gubici PbZn rude 6,0%.

### 2. Flotacijska iskorišćenja:

Ruda Cu:

- Iskorišćenje Cu 82,0%,
- Iskorišćenje Ag 50,0%,
- Iskorišćenje Au 50,0%.

Ruda Pb-Zn:

- Iskorišćenje Zn 60,0%,
- Iskorišćenje Pb 60,0%,
- Iskorišćenje Ag 51,5%,
- Iskorišćenje Au 35,0%,

### 3. Metalurška iskorišćenja:

Koncentrat Cu:

- Iskorišćenje Cu 95,0%,
- Iskorišćenje Ag 90,0%,
- Iskorišćenje Au 90,0%,

Koncentrat Pb-Zn:

- Iskorišćenje Zn 96,5%,
- Iskorišćenje Pb 95,0%,
- Iskorišćenje Ag 90,0%,
- Iskorišćenje Au 90,0%.

### 4. Prodajne cene metala:

- Bakar (Cu) 6.000 US \$/t,
- Srebro (Ag) 800 US \$/kg,

- Zlato (Au) 30.000 US \$/kg,
- Cink (Zn) 1.800 US \$/t,
- Olovo (Pb) 1.800 US \$/t,

### 5. Vrednost metala u koncentratu:

Koncentrat Cu:

- Bakar (6.000 – 600) = 5.400 US \$/t,
- Zlato (30.000 – 150) = 29.850 US \$/kg,
- Srebro (800 – 15) = 785 US \$/kg.

Koncentrat Pb-Zn:

- ❖ Cink (1.800×0,55) = 990 US \$/t,
- ❖ Olovo (1.800×0,55) = 990 US \$/t,
- ❖ Zlato (30.000×0,93) = 27.900 US \$/kg,
- ❖ Srebro (800×0,88) = 700 US \$/kg,
- ❖ Dobit 0,55%.

### 6. Troškovi otkopavanja:

- ❖ Otkopavanje rude i jalovine 2,0 US \$/t iskopa.

### 7. Flotacijski troškovi:

- Flotiranje Cu 4,0 US \$/t rude,
- Flotiranje Pb-Zn 6,0 US \$/t rude.

### 8. Troškovi metalurške prerade:

- Koncentrat Cu: 600 US \$/t koncentrata,
- Koncentrat Pb-Zn: 0,45 %.

### 9. Usvojena diskontna stopa 10%.

## KAPACITETI OTKOPAVANJA I ODLAGANJA

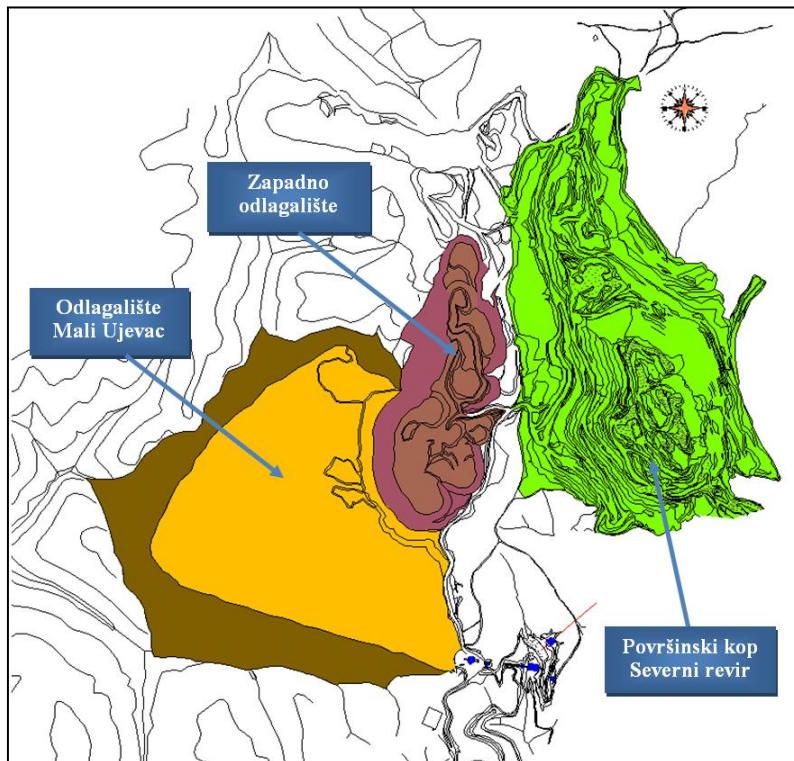
Planirana vrednost kapaciteta otkopavanja rude na godišnjem nivou je sledeća

- u 1. godini 3.000.000 t rude
- od 2. godine do kraja eksplotacionog perioda 5.000.000 t rude.

Kapacitet otkopavanje jalovine ograničen je na 16 miliona tona u prvoj godini eksplotacije. Od druge do četrnaeste godine

kapacitet otkopavanja na jalovini iznosi 14 miliona tona godišnje, a zatim konstantno opada, sem u periodu od osamnaeste do dvadesete godine kada je na nivou od 12÷13 miliona tona (tabela 3).

Na slici 1 prikazana su odlagališta Mali Ujevac i Zapadno odlagalište. Prostorni kapacitet navedenih odlagališta omogućava smeštaj celokupne količine jalovine koja se otkopava u toku eksploatacionog perioda.

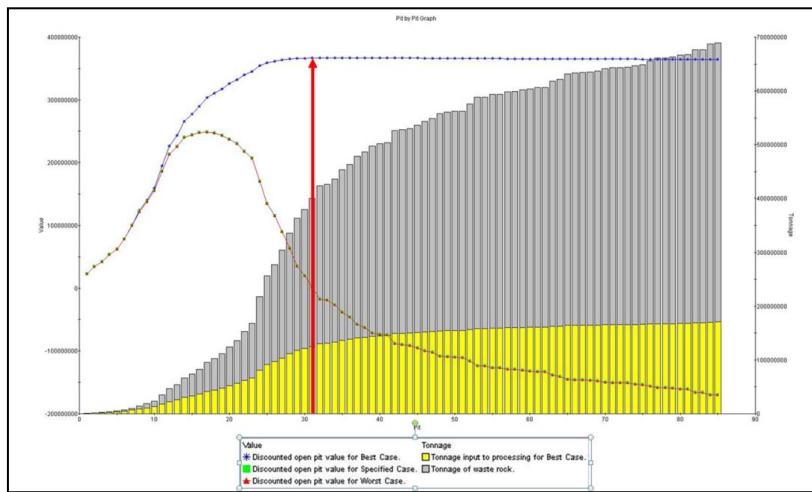


**Sl. 1.** Prikaz lokacija odlagališta površinskog kopa Severni revir

## OPTIMIZACIJA GRANICE POVRŠINSKOG KOPA

Optimalna granica otkopavanja površinskog kopa, za utvrđene tehnico-ekonomski parametre određena je korišćenjem softvera za optimizaciju i strateško planiranje površinskih kopova Whittle [2], [3]. Softver generiše više mogućih optimalnih kontura kopova, primenom faktora prihoda

(Revenue Factor). Dobijeni kopovi (generisano je 85 kopova koji su prikazani u tabeli 1 i na slici 2) dalje se analiziraju i vrši se izbor optimalnog kopa po kriteriju - diskontovane sadašnje vrednosti. Za dalje sagledavanje izabran je kop broj 31 [4].



**Sl. 2.** Grafički prikaz rezultata optimizacije površinskog kopa i izbora optimalne konture

**Tabela 1.** Rezultati optimizacije površinskog kopa i izbor optimalne konture

Kop	Faktor prihoda	Cena metala (C\$)	Ruda	Javlovina	Izkupine	Nevršeni tok best	Nevršeni tok specified	Nevršeni tok worst	Kop	Faktor prihoda	Cena metala (C\$)	Ruda	Javlovina	Izkupine	Nevršeni tok best	Nevršeni tok specified	Nevršeni tok worst
(S)	(S)	(S)	(S)	(S)	(S)	(S dñc)	(S dñc)	(S dñc)	(S)	(S)	(S)	(S)	(S)	(S)	(S dñc)	(S dñc)	(S dñc)
1	0.30	1 800	948 181	203 712	1 171 893	22 584 296	22 584 296	22 584 296	43	1.14	6 840	149 466 138	378 553 793	528 049 931	366 614 915	-89 578 295	
2	0.32	1 920	1 023 349	450 874	207 473	34 312 916	34 312 916	34 312 916	44	1.16	6 960	150 016 049	379 959 771	529 974 805	366 585 844	-91 100 702	
3	0.34	2 040	2 123 188	606 469	275 946	41 789 193	41 789 193	41 789 193	45	1.18	7 080	150 850 043	382 456 957	536 597 000	366 504 709	-94 941 362	
4	0.36	2 160	2 920 255	1 009 247	4 021 729	53 519 206	53 519 206	53 519 206	46	1.20	7 200	151 819 471	391 798 162	543 612 833	366 423 017	-99 707 699	
5	0.38	2 280	3 650 020	1 313 542	4 989 182	62 533 173	62 533 173	62 533 173	47	1.22	7 320	152 791 478	395 913 378	548 710 877	366 360 418	-101 886 755	
6	0.40	2 400	4 902 725	2 181 811	7 084 336	78 708 254	78 708 254	78 708 254	48	1.24	7 440	154 085 441	404 046 312	558 144 753	366 242 849	-108 521 838	
7	0.42	2 520	7 071 398	3 140 216	10 292 122	100 844 033	99 630 269	99 630 269	49	1.26	7 560	154 593 811	403 941 093	560 554 804	366 203 247	-109 166 215	
8	0.44	2 640	9 286 522	5 407 075	14 693 597	123 919 273	123 919 273	123 919 273	50	1.28	7 680	154 781 049	407 179 923	561 940 971	366 188 588	-110 048 394	
9	0.46	2 760	11 067 158	7 048 235	18 474 303	140 301 765	137 641 992	137 641 992	51	1.30	7 800	154 934 095	407 840 052	562 777 944	366 176 200	-110 353 097	
10	0.48	2 880	13 157 839	10 175 045	23 332 808	159 240 909	155 303 894	155 303 894	52	1.32	7 920	156 991 452	419 211 707	576 203 159	365 977 182	-116 630 127	
11	0.50	3 000	17 921 373	16 712 168	34 640 141	194 744 291	186 303 811	186 303 811	53	1.34	8 040	158 440 184	429 791 939	588 239 093	365 812 883	-123 772 663	
12	0.52	3 120	22 711 807	23 883 135	44 594 942	226 403 934	213 021 965	213 021 965	54	1.36	8 160	158 497 574	429 947 801	588 444 375	365 809 317	-123 884 339	
13	0.54	3 240	25 863 252	28 182 396	54 045 648	243 162 544	226 051 272	226 051 272	55	1.38	8 280	159 558 554	434 340 741	593 903 302	365 723 291	-124 459 957	
14	0.56	3 360	30 724 154	31 998 077	68 722 231	266 129 304	240 652 139	240 652 139	56	1.40	8 420	159 592 857	434 537 270	594 133 127	365 719 668	-124 479 454	
15	0.58	3 480	33 477 175	40 271 145	73 749 020	277 057 488	244 277 282	244 277 282	57	1.42	8 520	160 054 057	437 834 259	597 890 316	365 684 818	-128 101 097	
16	0.60	3 600	37 109 213	45 485 293	82 478 206	289 634 625	247 798 051	247 798 051	58	1.44	8 640	160 324 985	439 293 394	599 818 379	365 638 059	-129 382 131	
17	0.62	3 720	41 443 045	53 885 839	101 754 045	303 274 051	248 883 219	248 883 219	59	1.46	8 760	160 579 643	441 490 045	602 069 680	365 603 014	-130 733 799	
18	0.64	3 840	44 205 134	58 944 831	102 653 945	31 018 420	247 430 866	247 430 866	60	1.48	8 880	160 755 533	442 924 454	603 579 992	365 580 228	-131 808 169	
19	0.66	3 960	47 502 142	64 495 312	111 997 199	345 142 269	243 140 799	243 140 799	61	1.50	9 000	161 049 366	443 038 000	604 087 366	365 542 337	-133 029 393	
20	0.68	4 080	52 113 348	71 835 981	123 949 293	325 699 173	237 058 568	237 058 568	62	1.52	9 120	161 059 864	447 077 723	608 136 587	365 541 347	-133 056 955	
21	0.70	4 200	56 271 841	79 412 781	131 684 442	332 193 270	230 051 444	230 051 444	63	1.54	9 240	161 592 536	455 492 298	618 211 233	365 337 633	-138 422 927	
22	0.72	4 320	62 083 245	90 431 004	152 514 249	339 836 590	218 011 798	218 011 798	64	1.56	9 360	163 095 722	458 854 209	621 749 831	365 302 145	-140 311 918	
23	0.74	4 440	66 812 254	101 754 105	161 568 359	354 104 533	207 145 865	207 145 865	65	1.58	9 480	164 216 094	467 639 247	631 856 151	365 154 330	-145 180 524	
24	0.76	4 560	81 051 118	136 434 533	211 487 598	354 419 794	170 358 756	170 358 756	66	1.60	9 600	164 397 954	468 929 719	633 327 873	365 133 144	-145 388 727	
25	0.78	4 680	91 334 045	164 754 105	256 072 025	359 464 452	134 947 260	134 947 260	67	1.62	9 720	164 519 005	469 711 084	634 236 089	365 119 239	-144 339 169	
26	0.80	4 800	88 781 159	180 409 615	277 181 814	361 514 656	115 608 954	115 608 954	68	1.64	9 840	164 640 566	470 502 220	635 142 786	365 105 246	-146 775 402	
27	0.82	4 920	103 400 175	200 320 71	304 382 246	363 547 140	89 619 201	89 619 201	69	1.66	9 960	164 851 493	472 074 991	636 930 494	365 078 343	-147 233 405	
28	0.84	5 040	111 265 895	223 854 432	335 520 207	365 709 853	334 284 591	334 284 591	70	1.68	10 080	165 333 219	476 021 341	641 336 562	365 014 381	-149 475 008	
29	0.86	5 160	117 724 186	246 149 900	363 774 086	365 918 172	34 954 332	34 954 332	71	1.70	10 200	165 542 870	471 091 662	643 434 532	364 983 174	-150 211 976	
30	0.88	5 280	132 780 157	251 865 230	379 841 389	368 333 339	220 018 724	220 018 724	72	1.72	10 320	165 547 264	474 132 427	643 679 693	364 982 590	-150 134 725	
31	0.90	5 400	132 341 338	275 079 007	404 420 394	368 519 292	220 940	220 940	73	1.74	10 440	165 624 374	474 459 431	444 003 812	364 975 915	-152 924 039	
32	0.92	5 520	137 781 020	285 603 437	438 237 053	368 919 137	-16 975 286	-16 975 286	74	1.76	10 560	165 803 749	480 927 794	446 733 543	364 940 593	-152 582 138	
33	0.94	5 640	131 114 938	295 642 942	426 757 539	368 899 137	-18 886 084	-18 886 084	75	1.78	10 680	166 131 945	482 706 428	448 338 373	364 908 592	-153 443 285	
34	0.96	5 760	145 781 035	303 470 552	458 237 050	367 047 835	-26 505 753	-26 505 753	76	1.80	10 800	167 027 893	489 333 471	456 361 369	364 795 419	-156 132 521	
35	0.98	5 880	138 322 733	317 495 007	451 817 740	367 081 144	-38 381 780	-38 381 780	77	1.82	10 940	167 442 255	493 539 673	606 972 926	364 732 933	-158 135 513	
36	1.00	6 000	138 161 280	324 654 235	463 117 518	367 081 291	-45 537 457	-45 537 457	78	1.84	11 120	167 744 540	493 729 187	643 476 334	364 697 624	-159 499 253	
37	1.02	6 120	140 099 315	337 107 231	471 398 544	367 015 651	-57 484 923	-57 484 923	79	1.86	11 240	168 322 555	493 809 283	647 122 844	364 640 649	-160 363 859	
38	1.04	6 240	142 503 976	344 462 024	487 186 640	366 987 239	-62 747 899	-62 747 899	80	1.88	11 360	168 349 852	497 937 026	667 286 873	364 637 998	-160 188 952	
39	1.06	6 360	144 046 208	353 072 457	491 117 463	366 911 454	-71 308 357	-71 308 357	81	1.90	11 480	168 216 976	507 068 333	676 283 171	364 514 182	-165 487 724	
40	1.08	6 480	145 132 209	358 644 572	501 798 401	366 875 490	-79 811 425	-79 811 425	82	1.92	11 600	169 277 495	507 432 162	677 093 657	364 500 058	-165 244 949	
41	1.10	6 600	145 473 922	358 036 674	503 510 594	366 860 081	-74 384 990	-74 384 990	83	1.94	11 880	170 327 443	514 928 107	687 251 550	364 345 855	-169 860 134	
42	1.12	6 720	149 261 428	377 000 077	524 942 195	366 852 022	-88 296 935	-88 296 935	84	1.96	12 000	170 560 005	518 387 985	638 947 990	364 342 172	-170 132 990	

## DEFINISANJE FAZA OTKOPAVANJA (PUSHBACKS)

Nakon određivanja konačne granice otkopavanja, sledeći korak u procesu dizaj-

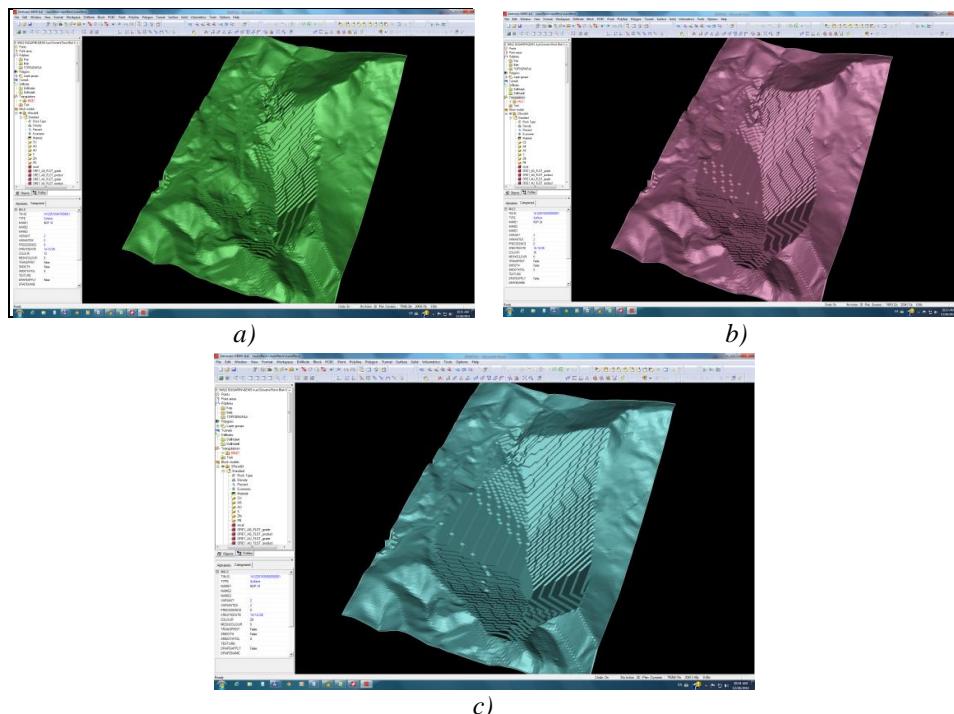
niranja površinskih kopava jeste definisanje faza otkopavanja [5].

Dobijeni rezultati u softveru Whittle prikazani su u tabeli 2.

**Tabela 2. Rezultati definisanja faza otkopavanja**

Osnovni eksploatacioni parametri	Faze otkopavanja (pushbacks)		
	Faza 1 (pushback 1)	Faza 2 (pushback 2)	Faza 3 (pushback 3)
Ukupna količina iskopina, t	46 631 341	170 986 143	183 003 754
Ukupna količina otkrivke, t	23 883 136	112 553 318	138 642 554
Količina rude, t	22 748 205	58 432 825	44 361 200
Granični sadržaj bakra u rudi, % C <sub>u</sub>	0,100	0,100	0,100
Prosečan sadržaj bakra u rudi, % C <sub>u</sub>	0,385	0,291	0,302
Granični sadržaj cinka u rudi, % Z <sub>n</sub>	1,000	1,000	1,000
Prosečan sadržaj cinka u rudi, % Z <sub>n</sub>	1,924	1,658	1,508
Koeficijent otkrivke, t/t	1,050	1,930	3,130

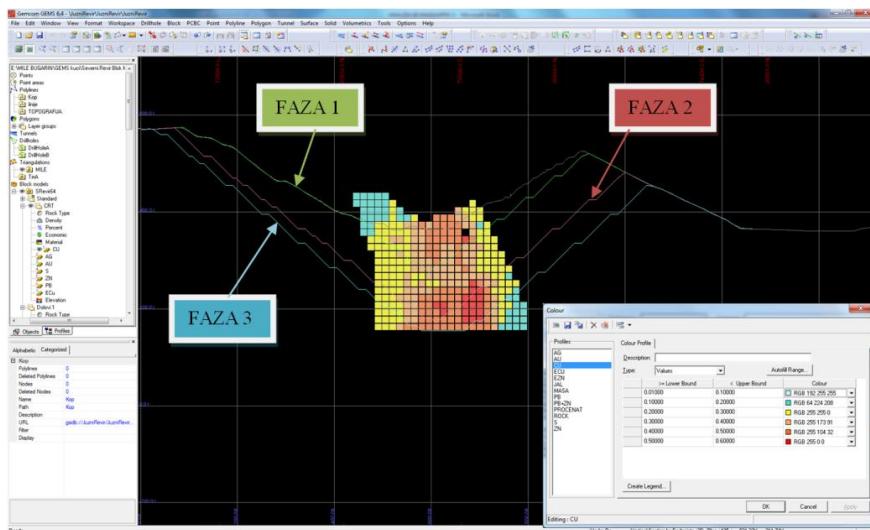
Prikaz završnih kontura Faza razvoja kopova, dobijena u softveru Whittle, dat je na sl. 3.



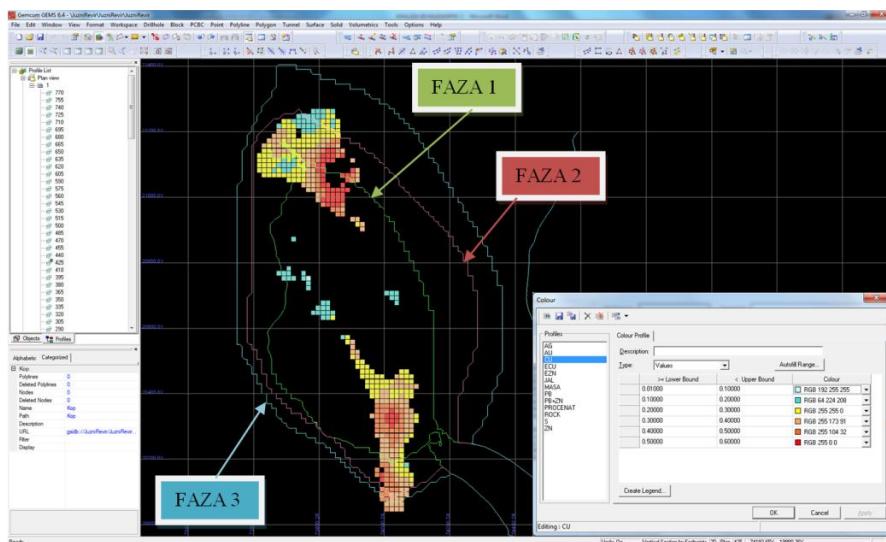
**Sl. 3. Izgled završnih kontura Faza razvoja kopa(3D prikaz)**  
a) faza 1, b) faza 2, c) faza 3

Na slikama 4 i 5 prikazane su Faze otkopavanja u softveru Gemcom Gems, na kojima

se pored granica Faza uočava i blok model sadržaja metala u rudi u ležištu Severni revir.



**Sl. 4.** Poprečni presek kopa sa prikazom Faza razvoja kopa i blok modela sadržaja bakra (koordinate tačaka X=4973341 i Y= 7520652; X=4974575 i Y= 7520652; azimut v=90°)



**Sl. 5.** Prikaz Faza razvoja kopa i blok modela sadržaja bakra u planu (nivo etaže E+425)

## OPTIMIZACIJA DINAMIKE OTKOPAVANJA

Dinamika otkopavanja po godinama eksplotacije dobijena je u softveru Whittle, u modulu New Schedule Graf. Za optimi-

zaciju dinamike otkopavanja softver koristi Milava algoritam, koji može da radi u režimu NPV kada se traži maksimalna neto

sadašnja vrednost (NSV) ili u režimu balansiranja u kome se traži da se maksimalno iskoriste proizvodni kapaciteti na otkopavanju i flotacijskoj pripremi u prvim godinama

eksploatacije. U ovom radu primjenjen je režim balansiranja (Milawa Balanced).

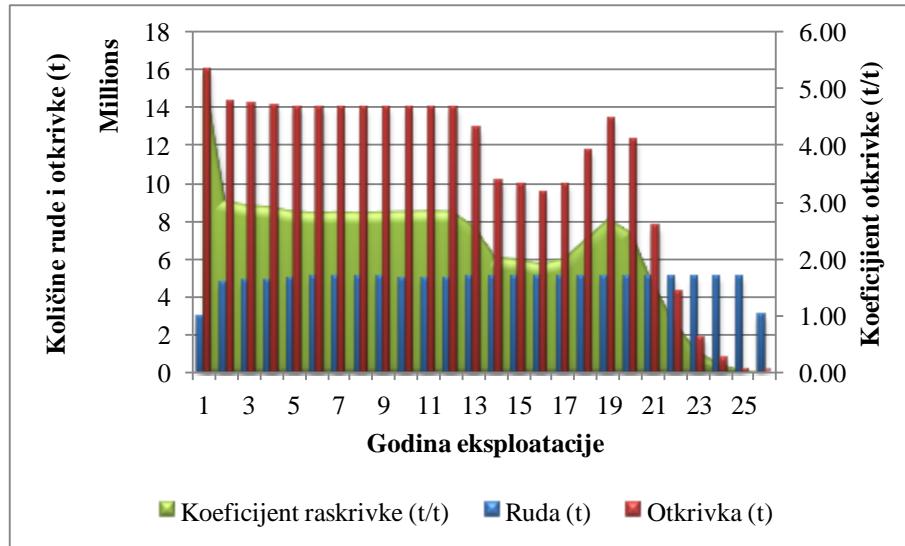
Rezultati optimizacije dinamike otkopavanja prikazani su u tabeli 3.

**Tabela 3. Dinamika otkopavanja po godinama eksploracije sa prikazom novčanog toka**

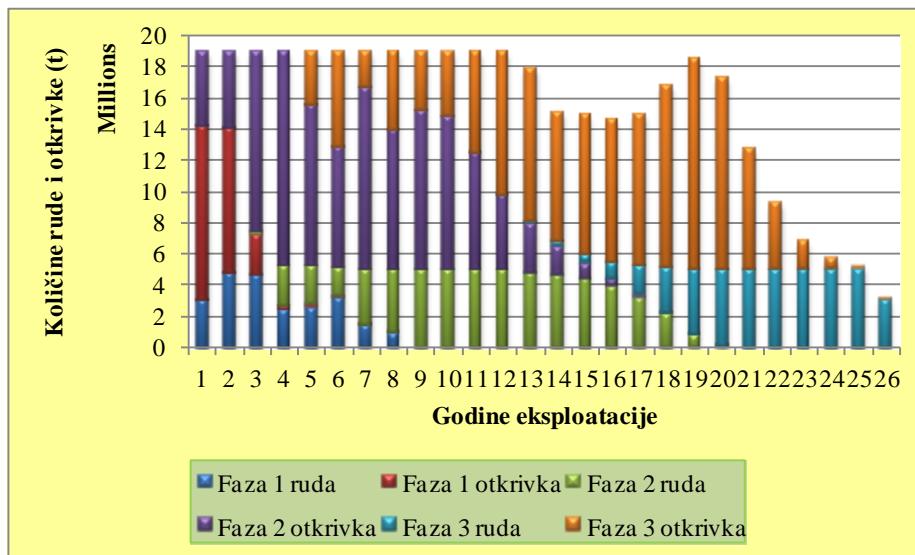
God.	Ruda	Jalovina	Iskopine	Koef. rask.	Novčani tok	Novčani tok disc
	(t)	(t)	(t)	(t/t)	\$	\$
1	2 979 345	16 020 655	19 000 000	5.38	11 246 634	10 224 213
2	4 734 069	14 265 931	19 000 000	3.01	34 996 063	28 922 366
3	4 845 618	14 154 382	19 000 000	2.92	33 451 016	25 132 244
4	4 876 619	14 123 381	19 000 000	2.90	31 150 733	21 276 370
5	4 971 615	14 028 385	19 000 000	2.82	34 912 504	21 677 918
6	4 996 616	14 003 384	19 000 000	2.80	40 871 924	23 071 135
7	4 982 021	14 017 979	19 000 000	2.81	21 689 710	11 130 251
8	4 994 294	14 005 706	19 000 000	2.80	26 008 360	12 133 092
9	4 985 137	14 014 863	19 000 000	2.81	13 143 992	5 574 336
10	4 969 517	14 030 484	19 000 001	2.82	18 102 666	6 979 361
11	4 964 874	14 035 126	19 000 000	2.83	17 222 757	6 036 471
12	4 975 731	14 024 269	19 000 000	2.82	18 713 860	5 962 812
13	5 000 000	12 848 645	17 848 645	2.57	25 731 559	7 453 516
14	5 000 000	10 082 085	15 082 085	2.02	36 509 799	9 614 171
15	4 999 998	9 922 013	14 922 011	1.98	37 432 610	8 961 069
16	5 000 000	9 538 805	14 538 805	1.91	31 437 699	6 841 759
17	5 000 000	9 939 543	14 939 543	1.99	24 695 897	4 885 952
18	4 999 998	11 698 016	16 698 014	2.34	22 904 849	4 119 638
19	5 000 000	13 430 083	18 430 083	2.69	18 038 165	2 949 384
20	5 000 000	12 269 592	17 269 592	2.45	23 636 188	3 513 369
21	5 000 000	7 704 188	12 704 188	1.54	33 055 309	4 466 783
22	5 000 000	4 216 883	9 216 883	0.84	31 765 187	3 902 225
23	5 000 000	1 814 944	6 814 944	0.36	35 382 772	3 951 483
24	5 000 000	715 856	5 715 856	0.14	43 949 792	4 462 029
25	5 000 000	162 320	5 162 320	0.03	57 185 004	5 277 947
26	3 065 906	11 490	3 077 396	0.00	46 774 308	4 072 012
Total	125 341 358	275 079 008	400 420 366	2.19	770 009 357	252 591 906

Na slici 6 dat je prikaz količina rude i jalovine po godinama eksploracije sa pripadajućim koeficijentom otkrivke.

Slika 7 prikazuje promenu količina rude i jalovine po godinama eksploracije i fazama razvoja kopa



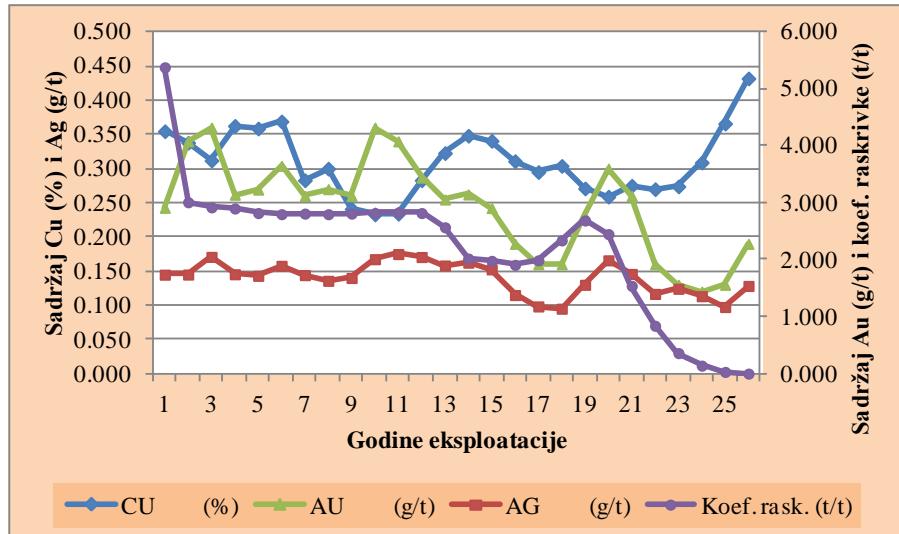
Sl. 6. Količine rude i jalovine po godinama eksploatacije sa pripadajućim koeficijentom otkrivke



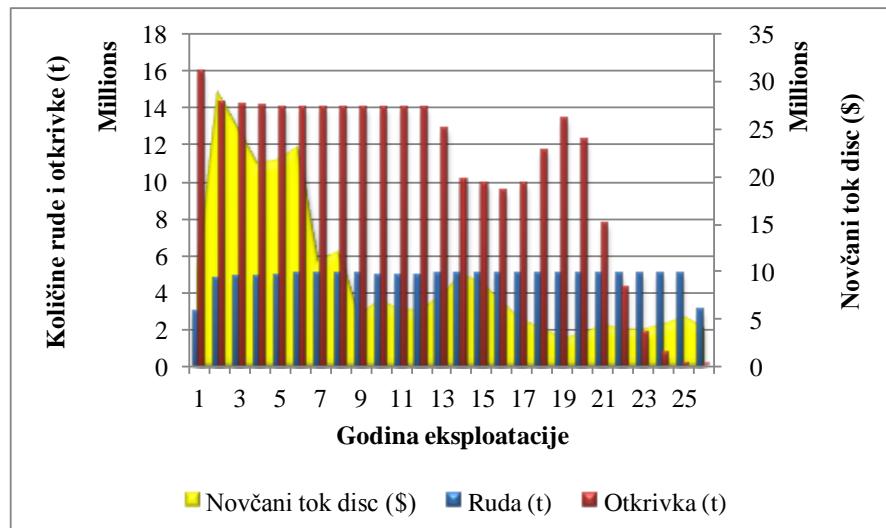
Sl. 7. Količine rude i jalovine po godinama eksploatacije i Fazama razvoja kopa

Promena srednjeg sadržaja bakra, srebra i zlata u rudi bakra i koeficijenta raskrivke po godinama eksploatacije može se očitati sa grafika na slici 8.

Slika 9 prikazuje kretanje diskontovanog novčanog toka i količina rude i jalovine po godinama eksploatacije.



Sl. 8. Promena srednjeg sadržaja bakra, srebra i zlata u rudi bakra i koeficijenta raskrivke po godinama



Sl. 9. Promena diskontovanog novčanog toka, količina rude i jalovine po godinama eksploracije

## ZAKLJUČAK

Na osnovu sprovedene analize zaključuje se sledeće:

- 1) Zadati kapacitet na otkopavanju rude bakra na površinskom kopu Severni revir Majdanpek od 5 miliona tona

godишnje postiže se u drugoj godini eksploracije. U prvoj godini kapacitet je na nivou od 3 miliona tona.

- 2) Vek eksploracije kopa iznosi 26 godina.

- 3) Koeficijent raskrivke u prvoj godini eksploatacije iznosi 5,38 t/t. Od druge do četrnaeste godine ovaj koeficijent ima ima vrednost oko 2,8 t/t, a zatim konstantno opada, sem u periodu od osamnaeste do dvadesete godine kada je na približno na nivou od 2,5 t/t.
- 4) Kretanje novčanog toka je pozitivno tokom celog perioda eksploatacije.
- 5) Ostvaruje se neto sadašnja vrednost u iznosu od **252.591.906 \$** (obračun u softveru Whittle).

## LITERATURA

- [1] Elaborat o rezervama ležišta bakra „Severni revir – Majdanpek“ i ležišta polimetaličnih mineralnih sirovina (Zn-Pb-Cu) „Tenka – Severni revir Majdanpek“, Institut za rudarstvo i metalurgiju Bor, 30.06.2011.
- [2] D. Kržanović, R. Rajković, M. Mikić: The Effect of Open Pit Slope Design on Net Present Value for Long Term Planning, The 46<sup>th</sup> International October Conference on Mining and Metallurgy, Borsko jezero, Serbia, 2014.
- [3] G. Whittle, W. Stange and N. Hanson, Optimising Project Value and Robustness, Project Evaluation Conference, Melbourne, Vic, 19 - 20 June 2007, str. 1-10.
- [4] D. Kržanović, R. Rajković, M. Mikić: Primena softverskih paketa za projektovanje u rudarstvu Gemcom i Whittle u cilju racionalnog i ekonomičnog iskorišćenja ležišta bakra Veliki Kričevlj kod Bora, Srbija, Rudarski radovi, Institut za rudarstvo i metalurgiju Bor, 3/2012, str. 85-90.
- [5] D. Kržanović, R. Rajković, M. Mikić, M. Ljubojević: Efekat faznog razvoja rudarskih radova na maksimizaciju neto sadašnje vrednosti kod dugo-ročnog planiranja površinskih kopova, Mining and Metallurgy Engineering Bor, 4/2014, str. 41-48.

Branislav Rajković\*, Zoran Ilić\*, Daniela Urošević\*

## TAKE UP PULLEY SELECTION OF BELT CONVEYOR FOR THE ORE IN TERMS OF AXLE SIZING

### Abstract

This work gives the methodology of take up pulley axle calculation on the example of belt conveyor for ore T 3505 designed for the needs of Majdanpek open pit with capacity of 800 t/h.

The analysis was made by calculation and represents a universal method for belt conveyor take up pulley axle calculation whose results are indispensable for reliability the check of this important part of belt conveyors.

Also, technical characteristics of all elements of the take up assembly are given, as well as their graphical representation.

**Keywords:** belt conveyor for ore, take up pulley axle calculation, take up assembly

## 1 INTRODUCTION

It is necessary that the conveyor belt is tense for correct operation of belt conveyors by corresponding force during the operation. Belt tensioning is made by take up pulley, while tensioning force itself is mostly obtained via screw take up device for the belt conveyors of shorter length or via counter weight for the belt conveyors of longer length.

Belt conveyor for the ore T 3505 was designed for transportation the small fraction screening product at the Majdanpek open pit from the screening facility to the belt conveyor T 3504[1].

Accordingly, it is a horizontal belt conveyor with a drive pulley on the discharge side of the conveyor and a take up pulley on the loading side of the conveyor. Considering that it is a belt conveyor of shorter length than 50 m, a screw take up device was predicted for obtaining the tensioning force by axial moving of the take up pulley what consequently tightens the belt.

Tensioning force on the take up pulley is a result of the preliminary calculation of the belt conveyor and it is an input value for the sizing of its elements.

## 2 TECHNICAL DESCRIPTION OF TAKE UP ASSEMBLY

The take up assembly of the belt conveyor consists of take up pulley assembly with axle and bearings, screw take up device, snub pulley assembly with axle and bearings, carrying troughing set with rollers, plow cleaner and bearing construction.

Technical characteristics of the belt conveyor itself are as follows:

- capacity: —
- material type: copper ore
- maximum lump size: —
- bulk density: —

\* Mining and Metallurgy Institute Bor, e-mail: branislav.rajkovic@irmbor.co.rs

- transport length:
- lifting of the material on belt:
- side carrying rollers inclination angle:
- belt speed: —
- belt type: 800/4 EP250 7/2
- electric motor power for belt drive:

The take up pulley (mark USF,620,950, 65,YA,RR,15; made by Rulmeca) is placed at the opposite side of the belt conveyor in relation to the drive pulley and it is equipped with the screw take up device with travel of 457,2 mm (mark TUHD-300-18; manufactured by Superior). Bearings of the take up pulley are self-adjusting (mark 22215 EK; manufactured by SKF). The snub pulley is placed in front of the take up pulley (mark USF,320,950,40,YA; manufactured by Rulmeca) with self-adjusting bearings (mark 22209 EK; manufactured by SKF). To prevent material from getting between the belt and the take up pulley the plow cleaner is predicted (mark E 4000 „V“ plough; manufactured by BMS). Within the take up assembly there is also a carrying troughing set (mark A3P/50,800,F22,H160,YA, manufactured by Rulmeca) with three carrying rollers (mark PSV4,30F,133N,323, manufactured by Rulmeca). All the elements of the take up assembly are placed on the bearing

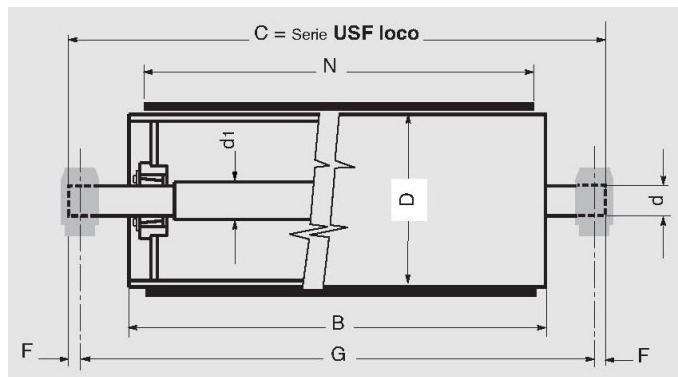
steel construction made by welding from hot rolled steel profiles.

The take up pulley dimensions with rubber lagging are as follows according to Fig. 1:

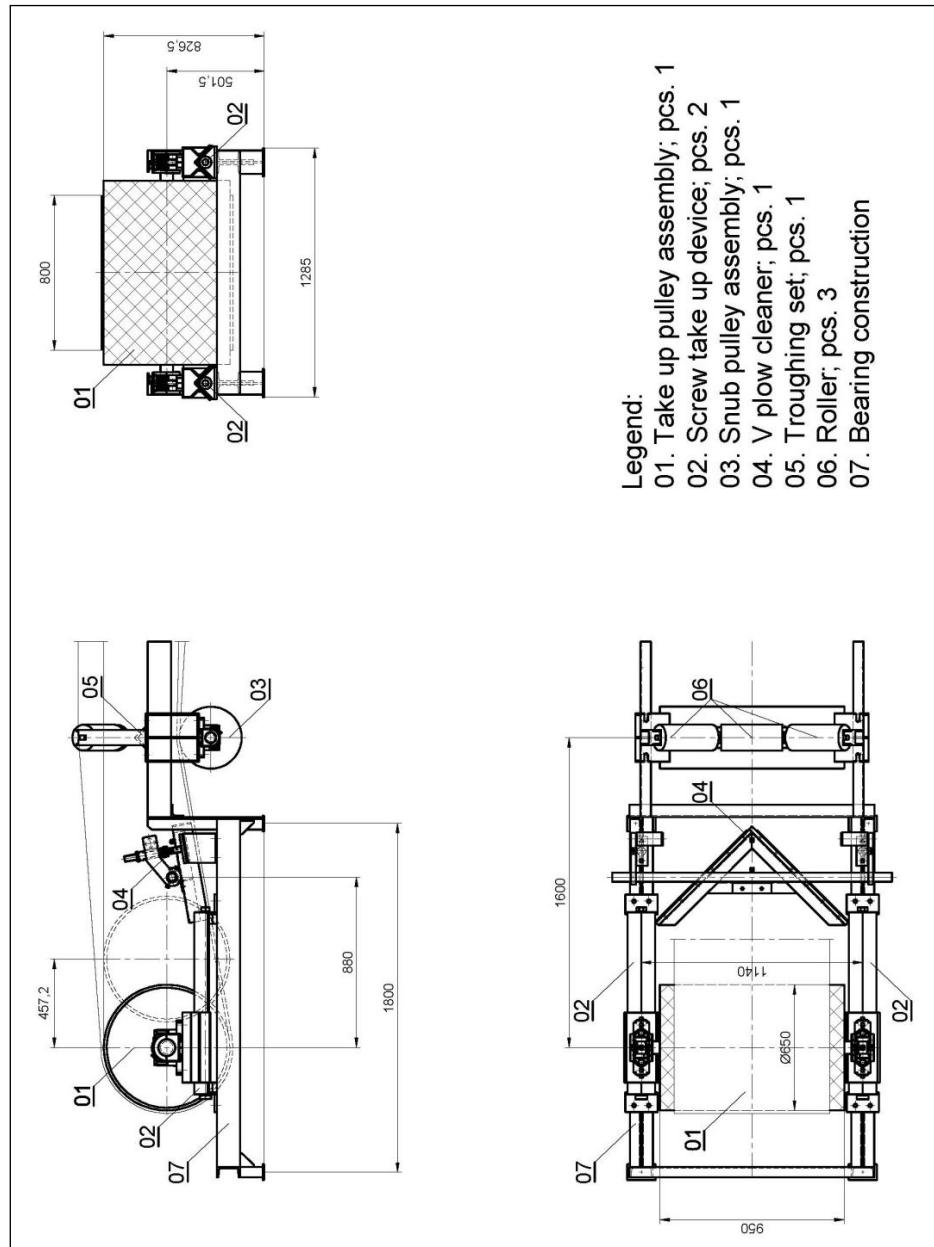
$$\begin{aligned} D &= 650 \text{ mm} \\ B &= 950 \text{ mm} \\ d &= 65 \text{ mm} \\ d_1 &= 70 \text{ mm} \\ G &= 1140 \text{ mm} \\ F &= 35 \text{ mm} \\ C &= 1210 \text{ mm} \end{aligned}$$

According to the catalog data of the Rulmeca manufacturer [2] series USF pulleys with clamping units connection between the axle and hub enables the compression axle locking using a system of screws and tapered sleeves eliminating the play and eccentricity. This locking system is used mostly today having in mind the strength, simplicity of construction, easy assembly and disassembly as well as the maintenance. The advantage compared to the traditional connection between the axle and the hub by key is in the fact that there is module of resistance reduction at traditional connection due to the key groove as well as difficult alignment on the assembly and difficult disassembly of pulleys being long time in exploitation.

The take up assembly of the belt conveyor T 3505 is given in Fig. 2.



**Fig. 1 Take up pulley of belt conveyor T 3505**



**Fig. 2** Take up assembly of belt conveyor T 3505

### 3 CALCULATION OF TAKE UP PULLEY AXLE

#### 3.1 Calculation of take up pulley axle diameter according to the stress limit

1. Calculation of take up pulley axle diameter according to the stress limit has for a purpose of determination the minimum axle diameter considering the load and admissible stress and it is given according to [2].

2. Bending moment

3. Module of resistance

4. Axle diameter

Where is:

—tension force at the pulley

—geometrical parameter

— — admissible stress

for material of the axle steel C40

#### 3.2 Calculation of take up pulley axle according to the axle deflection at hub

1. Calculation of take up pulley axle according to axle deflection at hub has for a purpose the determination of deflection

angle made as a result of axle elastic deformation under load considering allowable deflection and it is given according to [3] and figure 3.

2. Tangent of angle made by the deflected axle and its natural axis before bending, at the take up pulley hub

Where are:

— tension force at the pulley

— geometrical parameter

— geometrical parameter

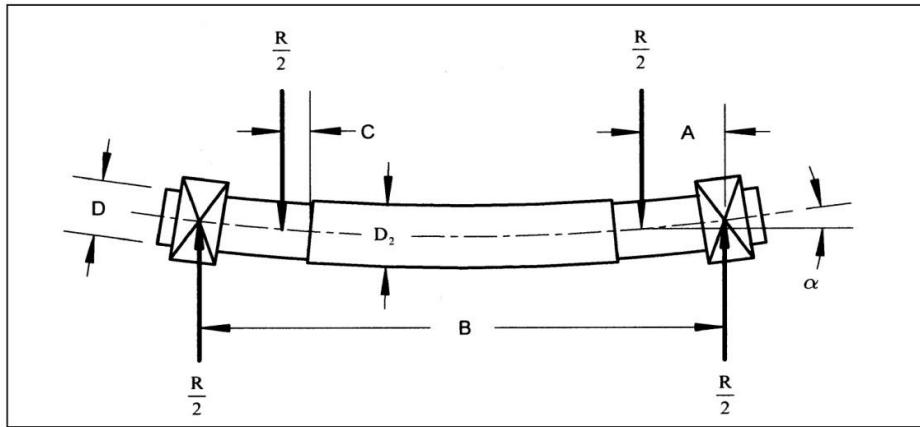
— modules of elasticity of steel

— area moment of inertia for diameter D

— axle diameter at hub

— area moment of inertia for diameter D2

— axle diameter inside the pulley



**Figure 3 Take up pulley axle deflection – geometrical parameters**

#### 4 DISCUSSION OF CALCULATION

The take up pulley axle is symmetrically loaded in bending. Steel C40 (heat treated) was selected as the axle material from the manufacturer's catalog. The axle is calculated according to the stress limit and allowable deflection angle. Calculation of take up pulley axle diameter according to the stress limit indicates that selected axle diameter is larger than required what means that the axle is satisfactory regarding the stress limit. The axle was designed with two different diameters so that its diameter inside the pulley is larger reducing the elastic deformations of axle under load compared to the case in which the axle is designed with constant diameter. Calculation of take up pulley axle according to the axle deflection at hub indicates that the deflection angle of axle is within acceptable limits. Namely, according to data from literature [3], maximum value of this angle amounts 8° while calculated value in this particular case amounts 3.9°. Applying the above formula, it is easily shown that the axle designed with constant diameter of 65 mm would have a deflection angle of 4.7°.

#### CONCLUSION

The results obtained by calculation show that the take up pulley axle is sized correctly by both criteria, i.e. according to the stress limit and according to the allowable deflection.

Take up pulley selection is usually done from the catalog data of the manufacturers. On this occasion, it is often necessary to check how the take up pulley axle is resistant in given operating conditions, so this work may be useful in this sense.

#### REFERENCES

- [1] Detail Design of Relocation of the Crushing Facility from the North Mining District and Construction the New Transportation System No. 3 for Ore of the South Mining District in the Copper Ming Majdanpek - Detail Mechanical Design of the Belt Conveyor for the Small Fraction Screening Product with all Transfer Points; Mining and Metallurgy Institute Bor; Section MEGA; 2013 (in Serbian);

- [2] Catalog of Rulmeca Company: Rollers and Components for Bulk Handling; Rulli Rulmeca S.p.A.; 4<sup>th</sup> Edition; July 2003; pp. 65, 259;
- [3] Catalog CEMA (Conveyors Equipment Manufacturer Association): Belt Conveyors for Bulk Materials“; 6<sup>th</sup> Edition; 2007, p. 227;

Branislav Rajković\*, Zoran Ilić\*, Daniela Urošević\*

## IZBOR ZATEZNOG BUBNJA TRAKASTOG TRANSPORTERA ZA RUDU SA ASPEKTA DIMENZIONISANJA OSOVINE

### Izvod

*U ovom radu je, na primeru trakastog transporterera za rudu T 3505 projektovanog za potrebe površinskog kopa u Majdanpeku sa kapacitetom 800 t/h, data metodologija proračuna osovine zateznog bubenja.*

*Analiza je urađena računskim putem i predstavlja univerzalni metod za proračun osovine zateznih bubenjeva trakastih transporterera čiji su rezultati neophodni za proveru pouzdanosti ovog važnog dela trakastih transporterera.*

*Takođe su date tehničke karakteristike svih elemenata zatezne grupe i njihov grafički prikaz.*

**Ključne reči:** trakasti transporter za rudu, proračun osovine zateznog bubenja, zatezna grupa

### 1. UVOD

Za ispravan rad trakastih transporterera neophodno je da transportna traka u toku rada bude zategnuta odgovarajućom silom. Zatezanje trake ostvaruje se preko zateznog bubenja, a sama sila zatezanja najčešće se ostvaruje, za transporterere manje dužine preko navojnog vretena, a za transporterere veće dužine preko zateznog tega.

Trakasti transporter za rudu T 3505 projektovan je za transport podrešetnog proizvoda rude na površinskom kopu u Majdanpeku od sitare do trakastog transporterera T 3504 [1].

Dakle, radi se o horizontalnom trakastom transporteru sa pogonskim bubenjem na istovarnej strani transporterera i sa zateznim bubenjem na utovarnoj strani transporterera. S obzirom da se radi o transporteru manje dužine od 50 m za ostvarivanje sile zatezanja predvideno je navojno vreteno kojim se aksijalno pomera zatezni bubenj i na taj način zateže traka.

Zatezna sila na zateznom bubenju je rezultat prethodnog proračuna transporterera i predstavlja ulazni podatak za dimenzionisanje njenih elemenata.

### 2. TEHNIČKI OPIS ZATEZNE GRUPE

Zatezna grupa trakastog transporterera sastoji se od sklopa zateznog bubenja sa osovinom i ležajima, uređaja za zatezanje trake sa navojnim vretenom, sklopa otklon-skog bubenja sa osovinom i ležajima, nosećeg sloga sa valjcima, plužnog brisača i noseće konstrukcije.

Tehničke karakteristike samog transporterera su sledeće:

- kapacitet: —
- vrsta materijala: ruda bakra
- krupnoća: —
- nasipna gustina: —

\* Institut za rudarstvo i metalurgiju Bor, e-mail: branislav.rajkovic@irmbor.co.rs

- dužina transporta:
- visina dizanja materijala na traci:
- ugao nagiba bočnih nosećih rolni:
- brzina trake: —
- tip trake: 800/4 EP250 7/2
- snaga elektromotora za pogon trake:

Zatezni bubanj (oznake USF,620,950,65, YA,RR,15; proizvođača Rulmeca) nalazi se na suprotnom kraju transporterja u odnosu na pogonski bubanj i snabdeven je uređajem za zatezanje trake sa navojnim vretenom čiji je hod 457,2 mm (oznake TUHD-300-18; proizvođača Superior). Ležaji zateznog bubenja su samopodesivi (oznake 22215 EK; proizvođača SKF). Ispred zateznog bubenja se nalazi otklonski bubanj (oznake USF,320,950,40,YA; proizvođača Rulmeca) sa samopodesivim ležajima (oznake 22209 EK; proizvođača SKF). Za zaštitu od upadanja materijala između trake i zateznog bubenja predviđen je plužni brisač (oznake E 4000 „V“ plough; proizvođača BMS). U sastav zatezne grupe ulazi i noseći slog (oznake A3P/50,800,F22,H160,YA, proizvođača Rulmeca) sa tri noseća valjka (oznake PSV4,30F,133N,323, proizvođača Rulmeca). Svi elementi zatezne grupe sme-

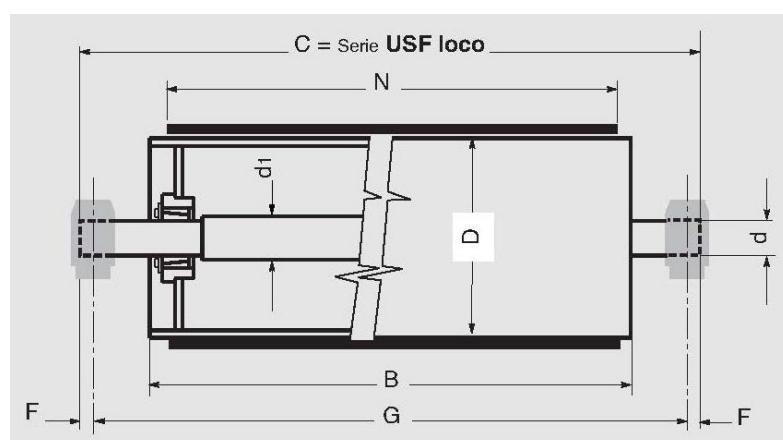
šteni su na noseću čeličnu konstrukciju izradenu zavarivanjem od toplo valjanih čeličnih profila.

Dimenzije zateznog bubenja sa gumenom oblogom su sledeće prema slici 1.:

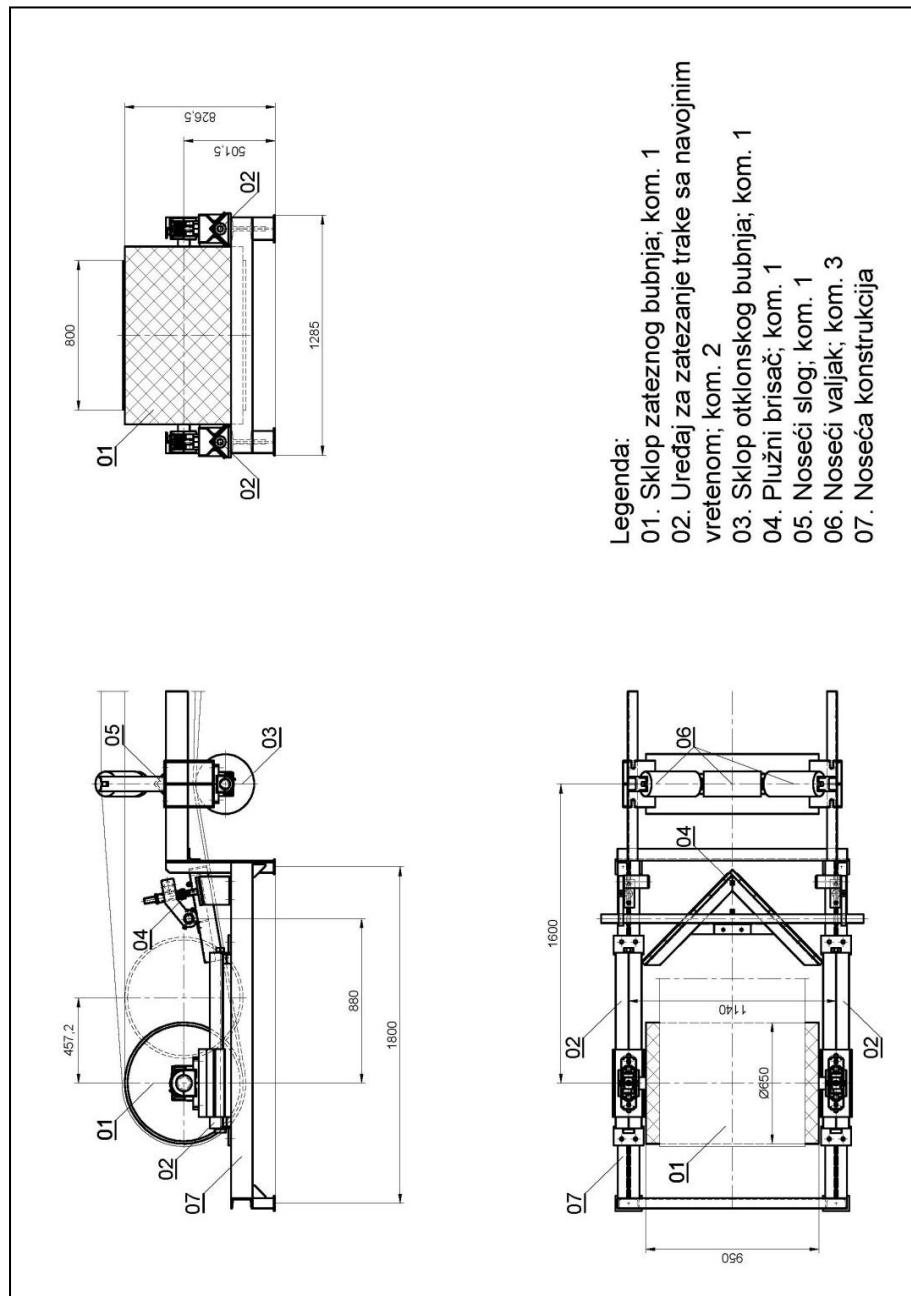
$$\begin{aligned} D &= 650 \text{ mm} \\ B &= 950 \text{ mm} \\ d &= 65 \text{ mm} \\ d_1 &= 70 \text{ mm} \\ G &= 1140 \text{ mm} \\ F &= 35 \text{ mm} \\ C &= 1210 \text{ mm} \end{aligned}$$

Prema kataloškim podacima proizvođača Rulmeca [2] serija USF bubenjeva sa vezom između osovine i glavčine bubenja steznim jedinicama omogućava zabravljinje osovine kompresijom koristeći sistem zavrtnjeva i konusnih rukavaca eliminirajući mrtvi hod i ekscentricitet. Ovaj sistem zabravljinja se danas najčešće koristi imajući u vidu jačinu, jednostavnost konstrukcije, laku montažu i demontažu, kao i održavanje. Prednost u odnosu na tradicionalnu vezu između osovine i glavčine bubenja klinom je što kod tradicionalne veze postoji smanjenje otpornog momenta osovine usled žleba za klin, kao i otežano centriranje pri montaži odnosno otežana demontaža kod bubenjeva koji su duže vreme u eksploataciji.

Prikaz zatezne grupe trakastog transporterja T 3505 dat je na slici 2.



**Sl. 1. Zatezni bubanj trakastog transporterja T 3505**



**Sl. 2.** Zatezna grupa trakastog transporterja T 3505

### **3. PRORAČUN OSOVINE ZATEZNOG BUBNJA**

#### **3.1. Proračun prečnika osovine zateznog bubnja prema dozvoljenom naponu**

1. Proračun prečnika osovine zateznog bubnja prema dozvoljenom naponu ima za cilj određivanje minimalnog prečnika osovine s obzirom na opterećenje i dozvoljeni napon i dat je prema [2].

2. Moment savijanja

—

3. Otporni moment

—

posledica elastične deformacije osovine pod opterećenjem s obzirom na dozvoljenu deformaciju i dat je prema [3] i slici 3.

2. Tangens ugla između deformisane osovine i njene prirodne ose pre savijanja na mestu glavčine zateznog bubnja

—

—

gde su:

4. Prečnik osovine

—  
—

zatezna sila na bubnju

— geo-  
metrijski parametar

geometrijski parametar

— geo-  
metrijski parametar  
— modul elasti-  
nosti za čelik

— moment inercije za prečnik D  
— prečnik  
osovine na glavčini

— moment inercije za prečnik  $D_2$   
— prečnik  
osovine unutar bubnja

gde su:

—zatezna sila na bubnju

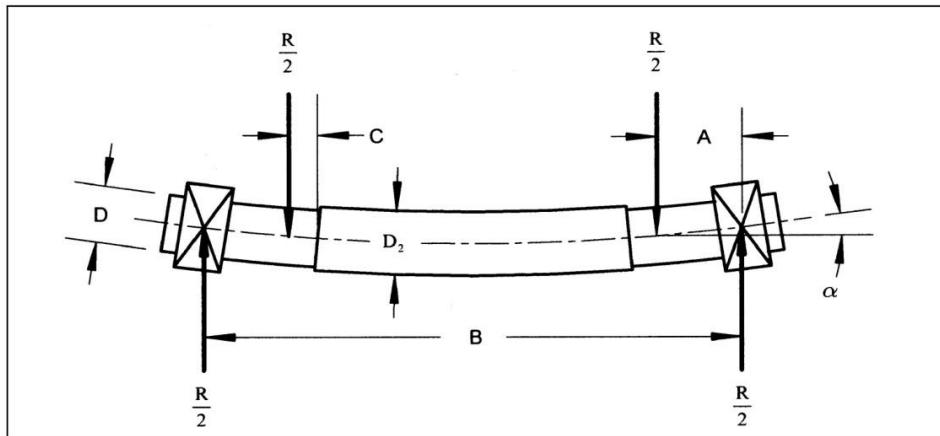
—geometrijski parametar

— — dozvoljeni

napon za materijal osovine čelik C40

#### **3.2. Proračun osovine zateznog bubnja prema nagibu osovine na glavčini**

1. Proračun osovine zateznog bubnja prema nagibu osovine na glavčini ima za cilj određivanje ugla nagiba koji nastaje kao



Sl 3. Deformacija osovine zateznog bubenja-geometrijski parametri

#### 4. DISKUSIJA PRORAČUNA

Osovina zateznog bubenja simetrično je opterećena na savijanje. Iz kataloga proizvođača usvojen je kao materijal osovine čelik C40 (poboljšan). Osovina se proračunava prema dozvoljenom naponu i prema dozvoljenom nagibu. Proračun prečnika osovine prema dozvoljenom naponu pokazuje da je usvojeni prečnik osovine veći od potrebnog što znači da u pogledu dozvoljenog napona osovina zadovoljava. Osovina je izvedena sa dva različita prečnika tako da je njen prečnik unutar bubenja veći čime se smanjuju elastične deformacije osovine pod opterećenjem u odnosu na slučaj kada se osovina izvodi sa konstantnim prečnikom. Proračun osovine prema nagibu osovine na glavčini pokazuje da je nagib osovine u dozvoljenim granicama. Naime, prema podacima iz literature [3] maksimalna vrednost ovog nagiba iznosi  $8'$  dok proračunska vrednost u konkretnom slučaju iznosi  $3,9'$ . Primenom gornje formule lako se pokazuje da bi osovina izvedena sa konstantnim prečnikom od 65 mm imala nagib od  $4,7'$ .

#### ZAKLJUČAK

Proračunom dobijeni rezultati pokazuju da je osovina zateznog bubenja ispravno dimenzionisana po oba kriterijuma tj. i prema dozvoljenom naponu i prema dozvoljenoj deformaciji.

Izbor zateznih bubenja obično se vrši iz kataloških podataka proizvođača. Tom prilikom često je potrebno proveriti kako se ponaša osovina zateznog bubenja u datim radnim uslovima, te ovaj rad može biti koristan doprinos u tom smislu.

#### LITERATURA

- [1] „Tehnički projekat preseljenja drobljiličnog postrojenja sa Severnog revira i izgradnje novog transportnog sistema br. 3 za rуду ležišta Južni Revir u Rudniku bakra Majdanpek-Tehnički mašinski projekat transporter-a za podrešetni proizvod sa svim presipnim mestima”; Institut za rudarstvo i metalurgiju Bor; Odeljenje MEGA; 2013.

- [2] Katalog firme Rulmeca: „Rollers and components for bulk handling”; Rulli Rulmeca S.p.A.; 4. izdanje; jul 2003.; str. 65, 259
- [3] Katalog CEMA (Conveyors Equipment Manufacturer Association): „Belt conveyors for bulk materials“; 6. izdanje; 2007.; str. 227

Milka Vidović\*, Vojin Gordanić\*, Ivana Trajković\*, Sanja Jovanić\*

## HYDROGEOCHEMICAL INVESTIGATION OF GROUND AND SURFACE WATER IN THE NEOGENE - QUATERNARY SEDIMENTS\*\*

### Abstract

*Geochemical investigations in order to identify the mineral deposits, as well as the sources of water supply of rural settlements included in the area of Bela Crkva, between the Nera and the Karaš rivers, draining the Neogene and Quaternary sediments. During the prospecting, water samples were collected from surface water streams, springs, wells, drills, water reservoirs, as well as the samples of stream sediments and rocks. Hydrogeochemical investigations are of significance, where, in the water of Vrsac hills, elevated levels of radionuclides U, Ra and Rn, and other toxic elements were detected with values above maximum allowed concentrations for drinking water. The wells of rural households had increased levels of Fe and Mn, as well as the increased mineralization, conductivity, and nitrogen cycle. The concentration of heavy metals in water wells was increased in the most settlements around Bela Crkva, as well as in Češko Selo, Banatska Subotica, Kuštilj, Jablanka and Karaš river.*

*From the water accumulations formed in the Quaternary sediments southwest from Bela Crkva, samples of water, mud, overbank sediments, and A-horizon were collected. The water samples were determined on: Na, K, Ca, Mg, Fe, Mn, Al, NH<sub>4</sub>, NO<sub>3</sub>, SO<sub>4</sub>, HCO<sub>3</sub>, Cl, F, Ep, Eh, pH value, mineralization, Pb, Cd, Co, Ni, Cr, Cu, Zn, H<sub>2</sub>S, O<sub>2</sub>, CO<sub>2</sub>, U, Ra, Rn, As, Hg, Br. In the solid samples, Au, Ag, Pb, Zn, and other elements, as well as the content of <sup>238</sup>U, <sup>232</sup>Th and <sup>40</sup>K were determined. Test results are presented in tables, diagrams, and hydrogeochemical maps.*

**Keywords:** hydrogeochemistry, prospecting, radioactivity, toxic elements, Neogene and Quaternary sediments.

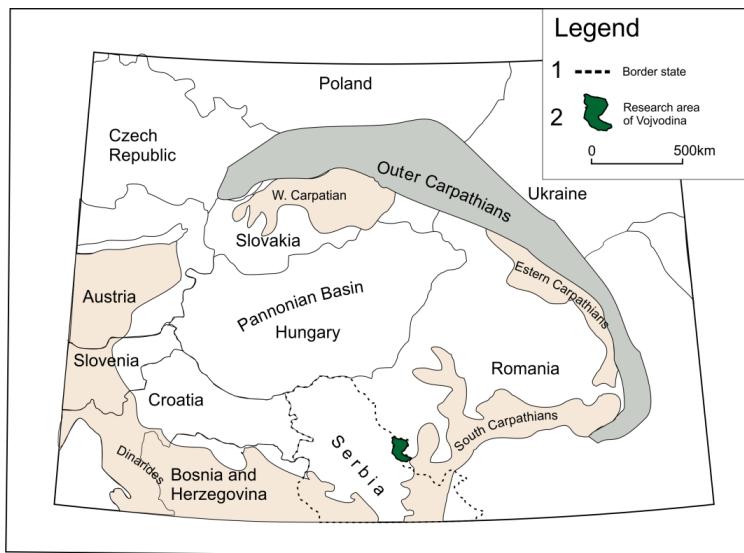
### INTRODUCTION

The presence of uranium deposits in Romania (Čudanovica Dobre), located in the zone of Rešica-Moldava Nova, relatively close to the border with Serbia im-

posed the need for research in Vršac-Bela Crkva region, as a perspective area for discovering uranium deposits and other mineral materials (Figure 1).

\* University of Belgrade, Scientific Institution Institute of Chemistry, Technology and Metallurgy, Department for Ecology and Technoeconomics, Njegoševa 12, Belgrade, e-mail: mivibgd@yahoo.com

\*\* This work was supported by the Ministry of Education, Science and Technological Development of the Republic of Serbia (Project OI 176018: "Geological and Ecotoxicological Research in Identification of Geopathogenic Zones of Toxic Elements in Drinking Water Reservoirs – Analysis of Methods and Procedures for Reduction the Effects of Biogeochemical Anomalies")



**Figure 1** Location of research area of the Pannonian Basin in Serbia

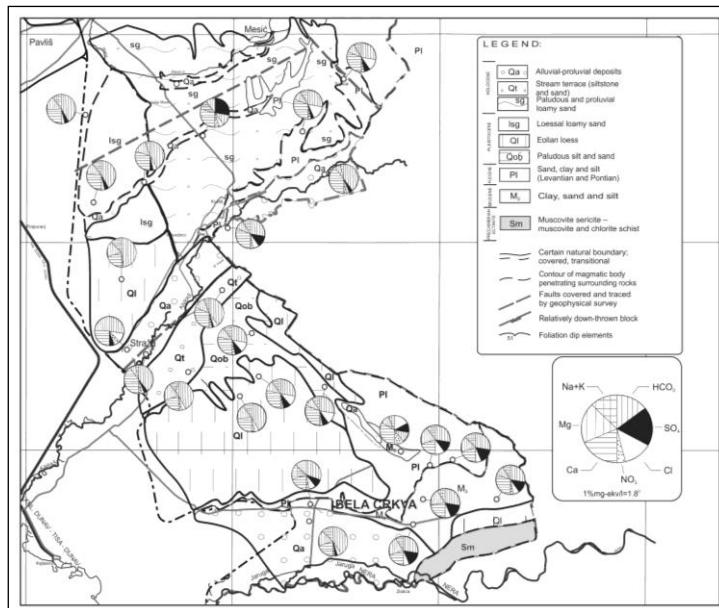
The earliest studies dating back to the 19<sup>th</sup> century (1880-1886) [1], when the first geological map of the Vršac area, scale 1:144000, with explanation was made. The most important data of studied area were gathered during research of oil and gas which were synthesized and then used for creation of book interpreter for the map of Bela Crkva 1:100000 [2, 3]. Researches included numerous geological, hydrogeological, geophysical, geochemical investigations. For the water supplying of Bela Crkva and surrounding rural settlements, in the area of Bela Crkva, the systematic monitoring of chemical elements distribution in different environments of geosphere was carried out, which is of special significance in detecting the natural and anthropogenic influence on living environment, and for defining the ecological status as well [4]. The largest number of data was collected during the regional research of nuclear materials in the area of Vršač hills - Bela Crkva [5], during the preparation of maps geochemical-ecological atlas 1:50000 [6]. The area of Bela Crkva is located in the southeastern Banat and presents the southeast end of the

Pannonian plain. In morphogenic terms, it is divided into three parts: sandstone west of the Bela Crkva, loess plateau and river lake terrace while the lowest parts of terrain are presented as the alluvial plains. An aquifer is formed in them with free level or so called the first aquifer, which is locally exploited through shallow wells for water supply or irrigation.

## METHODOLOGY

Lithogeochemical, metalometric and hydrogeochemical researches of the area of Bela Crkva (Figure 1) were applied. Sampling network was adjusted to the morphological and hydrographic characteristics of the terrain. The surface flows and shallow and deeper aquifers were tested.

In all water samples, contents of U, Eh, pH and Ec were determined. In water with the increased content of uranium, and pH, Eh and Ec changes, the complete chemical analyses were conducted: anion-cation composition, content of microelements and radioactive elements U, Ra and Rn, content of gases O<sub>2</sub>, CO<sub>2</sub>, H<sub>2</sub>S (Figure 2).



**Figure 2** Anion-Cation composition of water samples from the area of Bela Crkva

For determining the metal content in water, Atomic Absorption Spectrophotometry was applied (AAS Perkin Elmer M-306). For other components in water solutions, colorimetric, volumetric, potentiometric and turbidometric methods were used. Uranium was determined using the laser fluorimeter UA of Canadian production of Scintrex company, with fluran as the characteristic reagent. Radium concentrations were measured by radon detector RD-200 EDA, and radon concentrations were measured by radon emanometer ETR-1 Scintrex, Canada.

## RESULTS AND DISCUSSION

The quaternary formations of Pleistocene and Holocene cover about 70% of total area included within regional research of uranium in the area Vršac - Bela Crkva. The terrain is made of Quaternary formations of fluvial and aeolian origin which were deposited at the time when Pannonian Basin became mainland, with rivers, lakes and puddles.

The formations are presented as puddle alevrolites (Qab), aeolian loess (Ql), and loess clays (Figure 2). These sediments were created in continental conditions, and their origin is fluvial and aeolian. The thickness of Pleistocene in the Vršac area is about 30-60 m, and in the northern and western part reaches 100 m. Holocene is developed in morphologically the lowest parts of the terrain (north and south from the Vršac hills) and along the beds of smaller or bigger rivers Nera and Karaš. The sediments have a heterogeneous composition and consist of: proluvial suglines (Sg), debris of river terraces (alevrolites and Qz sand) and alluvial-proluvial creations (bed facies, floods with gravels, sand and alevrolites - Qa).

In hydrogeological terms, the terrain has a complex geological structure in the northern part from Bela Crkva (Vršac hills) the terrain is composed of old rock masses: granites, gneisses, albite-muscovite schists, and on the other side of Bela Crkva area the terrain is composed of a thick strata of the Tertiary and Quaternary sediments. The position of rock masses and the character of

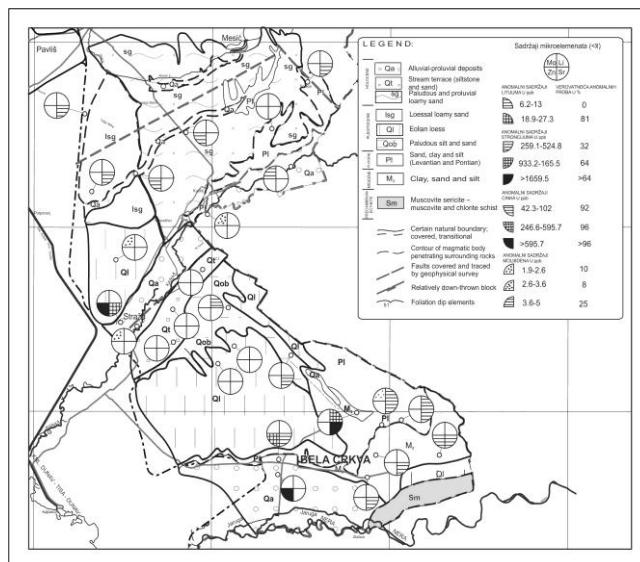
porosity in them caused formation of different types of aquifers in that part of the terrain. In terms of structure, the structural elements are significant which extend in the NE-SW direction, and in that direction, the surface flows that drain this area are developed. In deeper parts of the terrain there are no accumulations of free underground water, so the faults which intersect the terrain do not have higher hydrogeological significance.

The underground water is mainly  $\text{HCO}_3$ -Ca-Mg type, with low mineralization (about 0,4-0,5 g/L), pH neutral and moderately hard; it is contained in an open hydrogeological structure, where there is an intense water exchange, so the contents of certain chemical components are subjected to the time changes. Free aquifer of compact type was formed on the entire expanse of alluvial-lake sediments. This aquifer was developed in the alluvial plain of the rivers Karaš and Nera, then in the sand which is locally contained at different depth [7]. Depth to groundwater is mainly 5-10 m, and on smaller expanse depth varies above and beneath this value. Hydroisopleths of the first aquifer mainly follow the isopleths of the terrain and point to the directions of underground water drainage that is towards the erosive basin of

the rivers Nera and Karaš. In the area of Bela Crkva and wider (Vršac hills) in the phase of hydrogeochemical prospection, the samples of water were collected from surface flows, spring wells and lakes. According to the anioncation composition, water belongs to the hydrocarbonate type (Figure 2).

According to the presence of cations, calcium and magnesium prevail in water, which classifies it as calc-magnesium (Ca-Mg), and magnesium-calcium (Mg-Ca) type of water. Among other cations,  $\text{Na}^+$   $\text{K}$  are present but in considerably smaller quantity. Mineralization varies within the interval of 138 mg/L - 4557 mg/L in Vršac hills. The concentration of hydrogen ions varies from 5.5 to 7.9 so this water can be classified as weakly acidic to slightly alkaline. The redox potential (Eh) was determined in every water sample. On the basis of Eh values, we can conclude that water is mostly located in oxidizing conditions. The Eh values are within the interval from -65 mV to +190 mV.

Contents of microelements vary in the interval for: Mo from 1-14 ppb, =2ppb, Li from 3-60 ppb, =5 ppb, Sr from 30 - 3250 ppb, =300 ppb, Zn from 3 - 3800 ppb, =13 ppb (Figure 3).



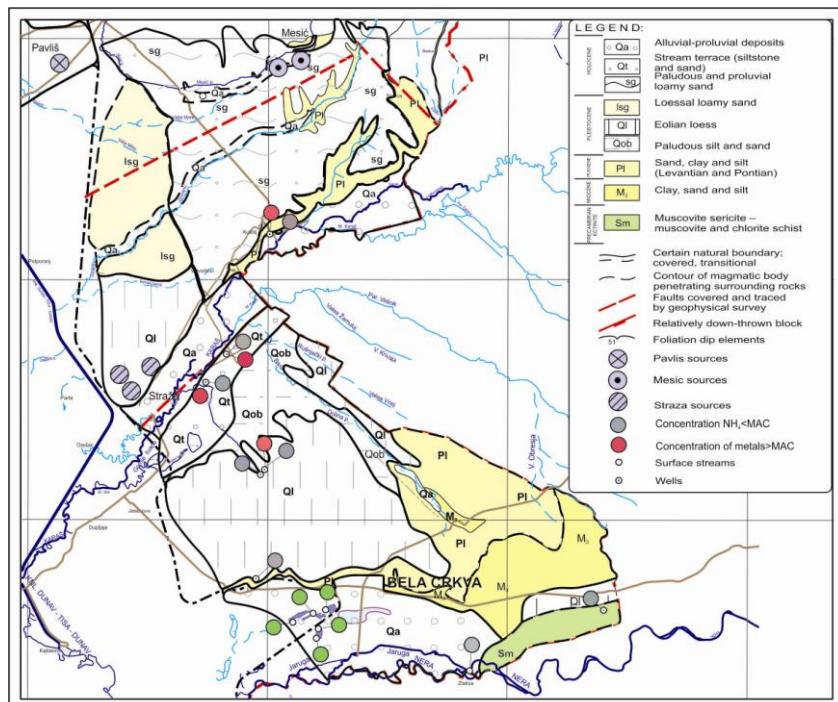
**Figure 3** Hydrogeochemical map of microelements content

The increased contents of Li are caused by the vicinity of granite intrusion in Vršac hills, zone of fine grained gneisses with leptinolites, aplites and strings of pegmatite. Clay materials in the sediments of Bela Crkva, unlike other alkaline elements (Lithium, Rubidium, Cesium) absorb weakly Sr. Since its ion has a large radius, it cannot be absorbed into compact structure of clay minerals with the exception of multistrata structure of monmorionites. The increased content of Sr is related to hydrocarbonate water which probably originate from granite intrusion. Anomalous concentrations of U, Ra and Rn in water can be found in the Vršac hills area.

In the Bela Crkva area, including water accumulations of lakes: Vračarev Gaj, Šaran lake, Bager lake, Veliko lake, the water analysis showed that water has slightly alkaline character. Concentration of ammonium ion, according to maximum allowed concentration (MAC) of dangerous substances in

water [8], has classified this water in the III/IV category and water from the lakes is classified in the I and II category. The nitrogen cycle is intense but content of nitrates does not exceed the MAC value. None of the samples detected hydrogen-sulfide as a product of anaerobic decomposition, which means that there is no process of rotting and decay. This water by its composition is calcium-sulphate, and by mineralization mainly belongs to water of the I category that is the II category [9]. It is important to point out that this water by the content of heavy metals can be classified as water of the I/II category according to the mentioned regulation.

The increased content of ammonia and nitrates gives a bad bacteriological image. In most wells there is an increased content of Fe and Mn which is a characteristic of underground water in this area, so water from certain wells shown in the hydrogeochemical map (Figure 4) cannot be used for drinking [10].



**Figure 4** Geoecological map of chemical content above maximum allowable concentration (MAC)

## CONCLUSION

In the phase of regional semi-detailed and detailed researches in the region of Bela Crkva and Vršac hills, the aquifer level was defined for water supply of rural settlements.

During the hydrogeochemical prospection, in every sample of water from surface flows, spring wells, and borings, complete chemical analyses were performed, which are relevant for researching the mineral materials deposits, and they present a base for the assessment of the influence of geological composition on the living environment. In the area of Bela Crkva, anomalous concentrations of elements in water of rivers Karaš and Nera and other water points are evident and they are a consequence of anthropogenic influence of excessive pollution from which the geoecological maps were done.

Presented results of chemical analyses of water, aquifer type and water quality of selected water points in rural settlements, represent a basis in spatial planning and living environment protection.

## REFERENCES

- [1] J. Halavats, Geological Conditions of Vršac Varoš, Journal Povesnica of free royal varoš Vršac, Pančevo, Kingdom of Yugoslavia, 1886, pp. 219-221;
- [2] B. Aksin, Theoretical Problems of Classification of Oil and Gas Deposits, its Significance with Special Reference to the Deposits of Banat; Special Edition Institute for Geological and Geophysical Researches, Book 15, Belgrade, Yugoslavia, 1967;
- [3] M. Rakić, Interpreter for the Geological Map of Bela Crkva 1:100000, Geological Institute, Belgrade, Yugoslavia, 1978;
- [4] V. Marinković, Lj. Obradović, M. Bugarin, G. Stojanović, The Impact of Polluted Wastewater on Water Quality of the Bor River and Surrounding Groundwater, Mining and Metallurgy Engineering Bor, 3 (2014), 33-36;
- [5] D. Purić, V. Gordanić, Report on Regional Studies of Nuclear Materials in the Area of Vršac Hills - Bela Crkva, Fund of Expert Documentation, Geoinstitute, Belgrade, Yugoslavia, 1981;
- [6] V. Gordanić, D. Jovanović, Geochemical-geoecological Atlas 1:50000, Fund of Expert Documentation, Geoinstitute, Belgrade, Serbia, 2007;
- [7] M. Vidović, V. Gordanić, Hydrogeological-Geochemical Characteristics of Groundwater in East Banat, Pannonian Basin, Serbia, Chapter 5 In: Hydrogeology – A Global Perspective, Edited by Gholam A. Kazemi, Rijeka, Croatia, InTech, 2012, pp. 161-179;
- [8] Regulation on Dangerous Substances in Water, Official Gazette of the Republic of Serbia No. 31/82, Belgrade, Yugoslavia, 1982;
- [9] Regulation on Water Classification, Official Gazette of the Republic of Serbia No. 5/68, 1968;
- [10] Official Gazette SRY 42/98, Belgrade, Yugoslavia, 1998.

Milka Vidović\*, Vojin Gordanić\*, Ivana Trajković\*, Sanja Jovanić\*

## HIDROGEOHEMIJSKA ISPITIVANJA KVALITETA PODZEMNIH I POVRŠINSKIH VODA U NEOGENIM – KVARTARNIM SEDIMENTIMA\*\*

### Izvod

Geološko-geohemija istraživanja u cilju identifikacije ležišta mineralnih sirovina, kao i izvorišta za vodosnabdevanje ruralnih naselja obuhvatila su područje Bele Crkve, između reka Nere i Karaša, koje dreniraju sedimente Neogena i Kvartara. U toku prospekcije, prikupljeni su uzorci voda iz površinskih tokova, izvora, bunara, bušotina, vodenih akumulacija, potočnih sedimenata i uzorci stena. Značajna su hidrogeochemijska ispitivanja, u kojima su u vodama otkriveni povišeni sadržaji radionuklida U, Ra i Rn u području Vršačkih brda, kao i drugih toksičnih elemenata, čije su vrednosti iznad maksimalno dozvoljenih u vodi za piće. U bunarima seoskih domaćinstava povećani su sadržaji Fe, Mn, a povećani su i mineralizacija, provodljivost i azotni ciklus. Koncentracija teških metala u bunarskim vodama je povećana u većini naselja oko Bele Crkve kao i u naseljima Češko selo, Banatska Subotica, Kuštilj, Jablanka kao i reka Karaš.

Od vodenih akumulacija nastalih u kvartarnim sedimentima JZ od Bele Crkve; prikupljeni su uzorci voda muljevitne komponente s dna jezera, overbank sedimenata i A-horizonta. U uzorcima voda određivani su: Na, K, Ca, Mg, Fe, Mn, Al, NH<sub>4</sub>, NO<sub>3</sub>, SO<sub>4</sub>, HCO<sub>3</sub>, Cl, F, Ep, Eh, pH, mineralizacija, Pb, Cd, Co, Ni, Cr, Cu, Zn, H<sub>2</sub>S, O<sub>2</sub>, CO<sub>2</sub>, U, Ra, Rn, As, Hg, Br, u čvrstim uzorcima Au, Ag, Pb, Zn, U i dr. elementi, kao i sadržaji U, Th i <sup>40</sup>K. Rezultati ispitivanja prikazani su: tabelama dijagramima i hidrogeochemijskim kartama.

**Ključne reči:** hidrogeochemija, prospekcija, radioaktivnost, toksični elementi, sedimenti neogena i kvartara

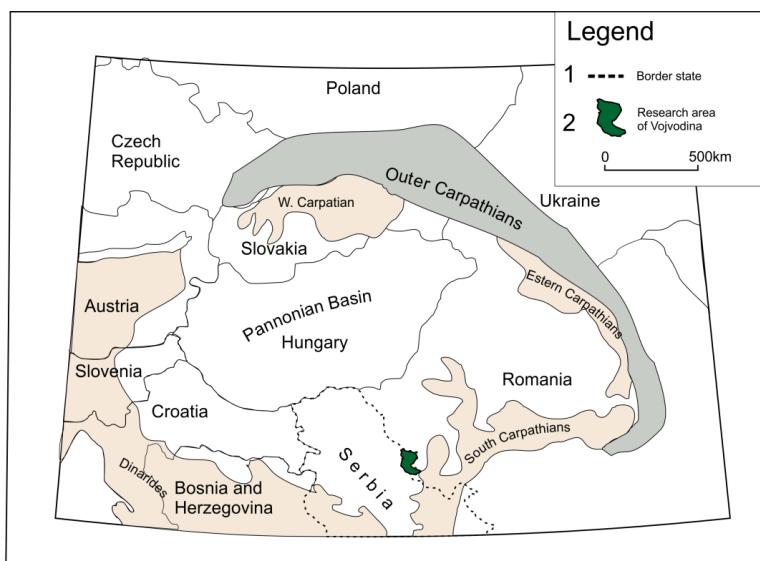
### UVOD

Prisustvo uranskih ležišta u Rumuniji (Čudanovica Dobre), koja se nalaze u zoni Rešica - Moldava Nova, na relativno bliskom rastojanju od granice sa Srbijom,

nametnula su potrebu za istraživanjem regiona Vršac - Bela Crkva, kao perspektivnog područja za otkrivanja ležišta urana i drugih mineralnih sirovina (Slika 1).

\* Univerzitet u Beogradu, Naučna ustanova Institut za hemiju, tehnologiju i metalurgiju, Centar za ekologiju i tehnokonomiku, Njegoševa 12, Beograd, e-mail: mivibgd@yahoo.com

\*\* Ovaj rad je realizovan uz podršku Ministarstva prosvete, nauke i tehnološkog razvoja Republike Srbije (projekat OI 176018: „Geološka i ekotoksikološka istraživanja u identifikaciji geopatogenih zona toksičnih elemenata u akumulacijama vode za piće – istraživanje metoda i postupaka smanjivanja uticaja biogeohemijских anomalija“)



**Sl. 1.** Lokacija istraživanog područja Panonskog basena u Srbiji

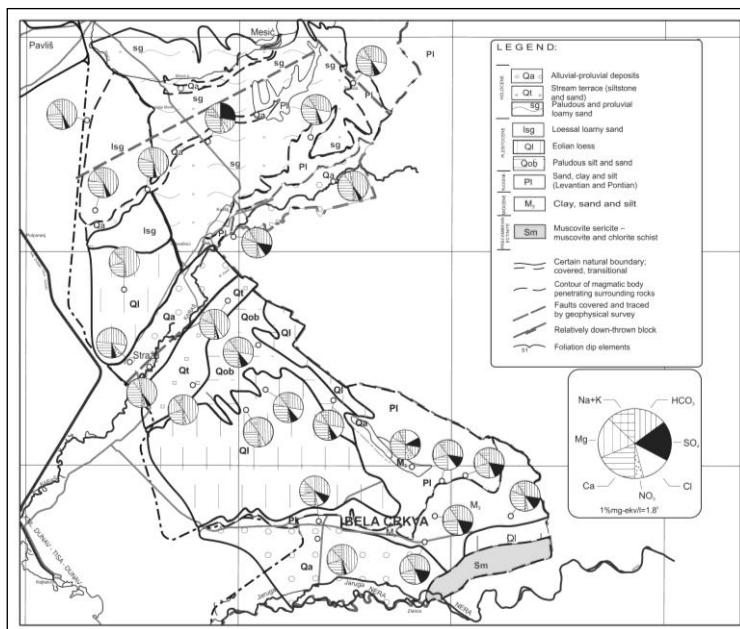
Najranija istraživanja datiraju iz vremena 19. veka (1880-1886. god.), kada je urađena prva geološka karta okoline Vršca u razmeri 1:144000 sa tumačem [1]. Najvažniji podaci o ispitivanom području dobijeni su prilikom istraživanja nafte i gasa, koji su korišćeni za izradu tumača za List Bela Crkva 1:100000 [2, 3]. Istraživanjima su obuhvaćena brojna ispitivanja iz oblasti geologije, hidrogeologije, geofizike, geochemije i dr. Za potrebe vodosnabdevanja Bele Crkve i okolnih ruralnih naselja, u ovom području Bele Crkve izvršeno je sistematsko praćenje distribucije hemijskih elemenata u različitim sredinama geosfere, što je od posebnog značaja za praćenje prirodnog i antropogenog uticaja na životnu sredinu i definisanje ekološkog statusa [4]. Najveći broj podataka prikupljen je za vreme regionalnih istraživanja nuklearnih sirovina na području Vršačkih bregova-Bele Crkve [5], odnosno tokom izrade geohemijskog-ekološkog atlasa 1:50000 [6]. Područje Bele Crkve nalazi se u jugoistočnom Banatu i predstavlja krajnji jugoistočni deo Panonske nizije. U morfogenom smislu podeljeno je na tri celine:

peščaru, zapadno od Bele Crkve, Lesnu zaravan i rečno jezersku terasu, a najniži delovi terena predstavljeni su aluvijalnim ravnima. U njima je formirana izdan sa slobodnim nivoom ili takozvana prva izdan, koja se lokalno eksplatiše preko plitkih kopanih bunara za vodosnabdevanje ili navodnjavanje.

## METODOLOGIJA

Litogeohemijska, metalometrijska i hidrogeohemijska ispitivanja su primenjena u fazi regionalnih istraživanja na području Bele Crkve (Slika 1). Morfološkim i hidrografskim karakteristikama terena prilagođena je mreža uzorkovanja. Ispitivani su površinski tokovi plitke i dublje izdani.

U svim uzorcima voda određeni su sadržaji U i vrednosti Eh, pH i Ep. U voda sa povиšenim sadržajem urana, promenama pH, Eh i Ep urađene su kompletne emijske analize voda, i to: anjonsko-katjonski sastav vode, sadržaj mikro-elenata i radioaktivnih elemenata U, Ra i Rn, sadržaj gasova O<sub>2</sub>, CO<sub>2</sub>, H<sub>2</sub>S (Slika 2).



Sl. 2. Anjonsko-katjonski sastav uzoraka vode sa područja Bele Crkve

Za određivanje sadržaja metala u vodama, primenjena je Atomsko Apsorpciona spektrofotometrija (AAS Perkin Elmer M-306). Za ostale komponente, u vodenim rastvorima korišćene su kolorimetrijske, volumetrijske, potenciometrijske i turbid-metrijske metode. Uran je određivan po-moću laserskog fluorimetra UA firme Scintrex kanadske proizvodnje, sa fluranom kao karakterističnim reagensom. Koncentracije radijuma su merene pomoću radon detek-tora RD-200 EDA, a koncentracije radona merene su emanometrom ETR-1 Scintrex, Kanada.

## REZULTATI I DISKUSIJA

Kvartarne tvorevine Pleistocena i Holocena, zahvataju oko 70% ukupne površine obuhvaćene regionalnim ispitivanjima urana područja Vršac-Bela Crkva. Teren je izgra-den od kvartarnih tvorevin, koje su fluvi-jalnog i eolskog porekla i taložene u vreme kada je Panonski basen postao kopno, sa rekama, jezerima i barama.

Tvorevine su predstavljene barskim alevrolitima (Qab), eolskim lesom (Ql), lesoidnim glinama (Slika 2). Ovi sedimenti su stvoreni u kontinentalnim uslovima, a porekla su fluvijalnog i eolskog. Debljina pleistocena u području Vršca je oko 30-60 m, a u severnom i zapadnom delu dostiže 100 m. Holocen je razvijen u morfološki najnižim delovima terena (severno i južno od Vršačkih brda) kao i duž korita manjih ili većih reka Nere i Karaša.

Sedimenti su heterogenog sastava i sastoje se od: barskih, proluvijalnih suglina (Sg), drobina, rečnih terasa (alevriti i peskovi Qz) i aluvijalno-proluvijalnih tvorevina (facija korita, plavina sa šljunkovima, peskovima i alevrolitima-Qa).

U hidrogeološkom smislu teren je slo-žene geološke grade. U severnom delu od Bele Crkve (Vršačkih brda) izgrađen je od starih stenskih masa – graniti, gnajsevi, albitsko–muskovitski škriljci a sa druge strane područje Bele Crkve debelih naslaga tercijarnih i kvartarnih sedimenata. Položaj stenskih masa i karakter poroznosti u njima

uslovili su da se u tom delu terena formiraju izdani različitog tipa.

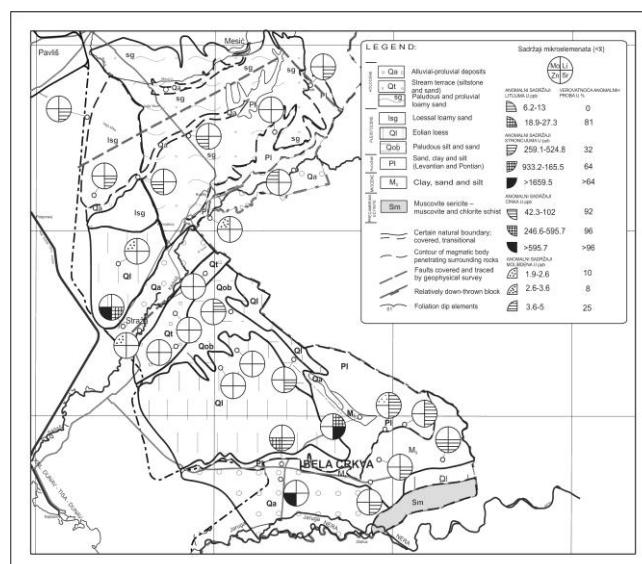
U strukturnom pogledu, značajni su strukturni elementi pravca pružanja SI-JZ, te su u tom smeru razvijeni površinski tokovi koji dreniraju ovo područje. U dubljim delovima terena nema akumulacija slobodnih podzemnih voda, pa ni rasedi koji presecaju teren nemaju veći hidrogeološki značaj.

Podzemne vode su pretežno  $\text{HCO}_3\text{-Ca-Mg}$  tipa, slabomineralizovane (oko 0,4-0,5 g/L), neutralne reakcije i umereno tvrde, koje se nalaze u otvorenoj hidrogeološkoj strukturi, gde se vrši intenzivna vodozamađena, pa su i sadržaji pojedinih hemijskih komponenti podložni promenama u funkciji vremena.

Slobodna izdan zbijenog tipa formirana je na celom prostranstvu aluvijalno-jezerskih sedimenata. Ova izdan je razvijena u aluvijalnoj ravni reke Karaš i Nera, zatim u peskovima koji se lokalno nalaze na različitoj dubini [7]. Dubina do podzemne vode je pretežno 5-10 m, a na manjem prostranstvu dubina varira iznad i ispod ove vrednosti. Hidroizohipse prve izdani uglavnom prate izohipse terena i ukazuju na pravce dreniranja podzemnih voda, odnosno ka erozionom bazisu reke Nera i Karaš.

U području Bele Crkve i šire (Vršačka Brda) u fazi hidrogeohemiske prospekcije, prikupljeni su uzorci voda iz površinskih tokova izvora bunara i jezera. Prema anjonsko-katjonskom sastavu, vode pripadaju hidrokarbonatnom tipu (Slika 2). Po zastupljenosti katjona, u vodama preovlađuju kalcijum i magnezijum, što ih svrstava u kalcijsko-magnezijske (Ca-Mg), magnezijsko-kalcijске (Mg-Ca) tipove voda. Od ostalih katjona i znatno manjoj količini su  $\text{Na}^+$ -K. Mineralizacija se kreće u intervalu (138 mg/L do 4557 mg/L). U Vršačkim brdima koncentracija vodonikovih jona varira od 5,5 - 7,9, pa se ove vode mogu svrstati u grupu slabokiselih do slaboalkalnih voda. Oksidaciono redukciono potencijal (Eh) određivan je u svakom uzorku vode. Na osnovu vrednosti Eh možemo zaključiti da se vode nalaze pretežno u oksidacionim uslovima. Vrednosti Eh, nalaze se u intervalu od -65 mV do +190 mV.

Sadržaji mikroelemenata variraju u intervalu za: Mo od 1-14 ppb, = 2 ppb, Li od 3-60 ppb, = 5 ppb, Sr od 30-3250 ppb, = 300 ppb, Zn od 3 ppb – 3800 ppb, = 13 ppb (Slika 3).



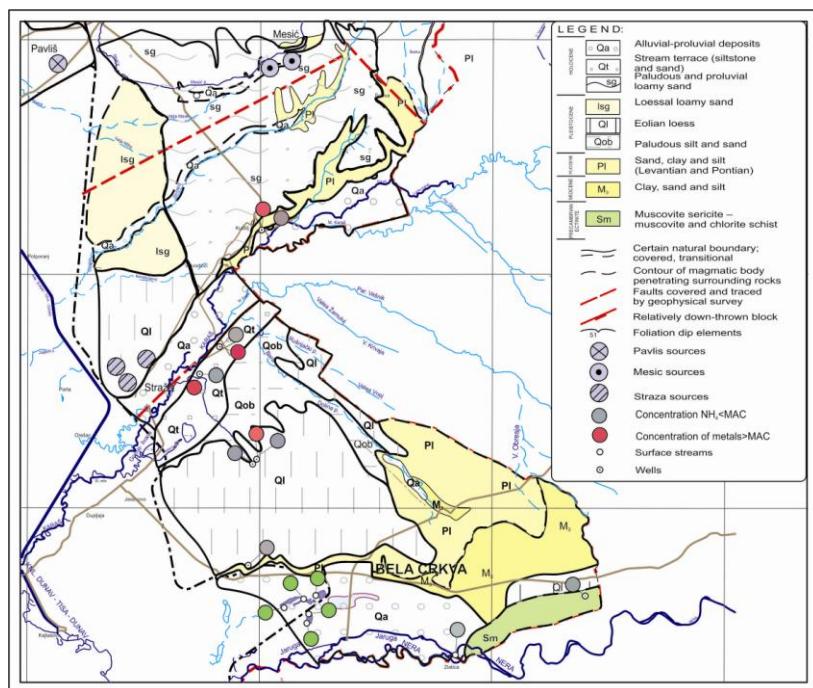
Sl. 3. Hidrogeohemiska karta sadržaja mikroelemenata

Povećani sadržaji Li uslovljeni su blizinom granitske intruzije u Vršačkim brdima, zone sitnozrnih gnajseva sa leptinolitima, aplitima i žicama pegmatita. Glinoviti materijali u sedimentima Bele Crkve, za razliku od drugih alkalnih elemenata (Litijum, Rubidijum, Cezijum) slabo apsorbuju Sr. Kako je njegov ion velikih razmara to ne može biti apsorbovan u zgušnutoj strukturi glinovitih minerala, sa izuzetkom višeslojne strukture monmorionita. Povišeni sadržaji Sr vezani su za hidrokarbonatne vode i verovatno vode poreklo od granitskog intruziva. Anomalne koncentracije U, Ra i Rn u vodama nalaze se u području Vršačkih Brda.

U području Bele Crkve uključujući i vodene akumulacije jezera: Vračarev Gaj, Jezero, Šaransko jezero, Bagersko jezero i Veliko Jezero, analize voda su pokazale da vode imaju slabo alkalan karakter. Koncentracija amonijum jona, prema maksimalno

dovoljenoj količini opasnih materija u vodama [8] svrstava ovu vodu u kategoriju III/IV, a vode iz Jezera u I i II kategoriju. Izražen je azotni ciklus ali sadržaj nitrata ne prelazi maksimalno dozvoljenu vrednost. Ni u jednom uzorku nije detektovan vodonik-sulfid, kao proizvod anaerobnog raspadanja, što znači da nema procesa truljenja i raspadanja. Ove vode su po svom sastavu uglavnom kalcijum-sulfatne, a po mineralizaciji uglavnom pripadaju vodama I odnosno II kategorije [9]. Bitno je istaći da se, i po sadržaju teških metala mogu svrstati u I/II kategoriju voda prema navedenoj uredbi.

Povećani sadržaji amonijaka i nitrita daju lošu bakteriološku sliku. U većini bunara je povećan sadržaj Fe i Mn što je karakteristika podzemnih voda ovog područja, pa se voda iz pojedinih bunara prikazanih na hidrogeohemijskoj karti (Slika 4) ne može koristiti kao voda za piće [10].



**Sl. 4.** Geoekološka karta hemijskih sadržaja preko maksimalno dozvoljene koncentracije (MDK)

## ZAKLJUČAK

U fazi regionalnih, poludetaljnih i detaljnih istraživanja, u region Bele Crkve i Vršačkih brda, definisan je nivo izdani za vodosnabdevanje ruralnih naselja.

U toku hidrogeohemijske prospekcije, u svakom uzorku vode: površinskih tokova, izvora, bunara i bušotina, urađene su hemijske analize od značaja za istraživanje ležišta mineralnih sirovina, a koje čine osnovu u proceni uticaja geološkog sastava na životnu sredinu. U području Bele Crkve, evidentne su anomalne koncentracije elemenata u vodama reke Karaš i Nere i drugih vodopunktova, koje su posledica antropogenog uticaja prekograničnog zagadenja, na osnovu čega su urađene geološke karte.

Prikazani rezultati hemijskih analiza voda, tip izdani i kvalitet voda izabranih vodopunktova u ruralnim naseljima čine osnovu u prostornom planiranju i zaštiti životne sredine.

## LITERATURA

- [1] J. Halavats, Geological conditions of Vršac varoš, Journal Povesnica of Free Royal Varoš Vršac, Pančevo, Kingdom of Yugoslavia, 1886, str. 219-221.
- [2] B. Aksin, Theoretical Problems of Classification of Oil and Gas Deposits, its Significance with Special Reference to the Deposits of Banat; Special Edition Institute for Geological and Geophysical Researches, Book 15, Belgrade, Yugoslavia, 1967.
- [3] M. Rakić, Interpreter for the Geological Map of Bela Crkva 1:100000, Geological Institute, Belgrade, Yugoslavia, 1978.
- [4] V. Marinković, Lj. Obradović, M. Bulgarin, G. Stojanović, Uticaj zagađenih otpadnih voda na kvalitet vode Borske reke i okolnih podzemnih voda, Mining and Metallurgy Engineering Bor, 3 (2014), 37-40.
- [5] D. Purić, V. Gordanić, Report on Regional Studies of Nuclear Materials in the Area of Vršac hills - Bela Crkva, Fund of Expert Documentation, Geo-institute, Belgrade, Yugoslavia, 1981.
- [6] V. Gordanić, D. Jovanović, Geochemical-geoecological Atlas 1:50000, Fund of Expert Documentation, Geo-institute, Belgrade, Serbia, 2007.
- [7] M. Vidović, V. Gordanić, Hydrogeochemical-Geochemical Characteristics of Groundwater in East Banat, Pannonian Basin, Serbia, Chapter 5 In: Hydrogeology – A Global Perspective, Edited by Gholam A. Kazemi, Rijeka, Croatia, InTech, 2012, str. 161-179.
- [8] Regulation on Dangerous Substances in Water, Official Gazette of the Republic of Serbia No. 31/82, Belgrade, Yugoslavia, 1982.
- [9] Regulation on Water Classification, Official Gazette of the Republic of Serbia No. 5/68, 1968.
- [10] Officiale gazette SRJ 42/98, Belgrade, Yugoslavia, 1998.

Vojin Gordanić\*, Milka Vidović\*, Ivana Trajković\*, Saša Rogan\*

## GEOCHEMICAL MAPPING OF RIVERBANK PROFILES IN THE BASIN AREA OF THE RIVER IBAR: ROLE IN ESTABLISHING THE GEOCHEMICAL BASIS FOR THE ASSESSMENT OF ANTHROPOGENIC INFLUENCE ON THE ENVIRONMENT\*\*

### Abstract

*Geochemical mapping of riverbank profiles of the basin area of the river Ibar was performed in the purpose of making regional geochemical map of Serbia 1:1000000. In this area, deposits of lead and zinc are located, and they are characterized by very complex geological composition. Sampling net at chosen locations of riverbank profiles was adjusted to the morphological and hydrographic characteristics of the terrain. At every profile, samples were collected from A-horizon, Ob-overbank sediment and S-active stream sediment, while tracking the changes of lithological members, in accordance to the WEGS methodology (Western European Geological Surveys).*

*The preserved geochemical track in the overbank sediment is of special significance for correlation the results of chemical elements in the surface part of (A-horizon) and active contemporary stream sediment. In the analytical process, beside determining contents of Pb, Zn, Cu, Co, Ni, Cr, Sb, V, Cd and other elements, the radiometric examinations of contents of  $U^{238}$ ,  $Th^{232}$  and  $K^{40}$ , were also conducted as well as the appropriate sedimentological analyses. On the basis of geochemical prospection results, a data base was formed which represents a foundation for estimation of anthropogenic influence on the living environment of rural settlements in the basin area of the river Ibar. In accordance to the geological-structural and morphological characteristics of the terrain, the results are applicable in the research of mineral raw materials, in agriculture, forestry, geomedicine, etc.*

**Keywords:** overbank, strim sediments, A-horizotn, geochemical mapping, riverbank profile

### INTRODUCTION

The overbank sediment (material deposited in the alluvial plain outside of the drainage canal) is usually used in the processes of making regional geochemical maps [1]. Studies in Great Britain showed a “close link“ between the mine contamination and contents of metals in the contemporary overbank sediments [2,3]. Application of OB-overbank sediment as a medium suitable for making geochemical atlas of Western

Europe and defining the anthropogenic influence on the living environment was supported by Bolviken et al. [4]. For making a regional geochemical map of Serbia 1:1000000 [5], the overbank sediment was used, and for researches basin areas from 60-600 km<sup>2</sup> were used. The significance of overbank sediment in defining the ecological status and making regional geochemical map of Serbia is shown at locations of

\* University of Belgrade, Scientific Institution Institute of Chemistry, Technology and Metallurgy, Department for Ecology and Technoeconomics, Njegoševa 12, Belgrade, e-mail: trajkovicivana@yahoo.com

\*\* This work was supported by the Ministry of Education, Science and Technological Development of the Republic of Serbia (Project OI 176018: “Geological and Ecotoxicological Research in Identification of Geopathogenic Zones of Toxic Elements in Drinking Water Reservoirs – Analysis of Methods and Procedures for Reduction the effects of Biogeochemical Anomalies“).

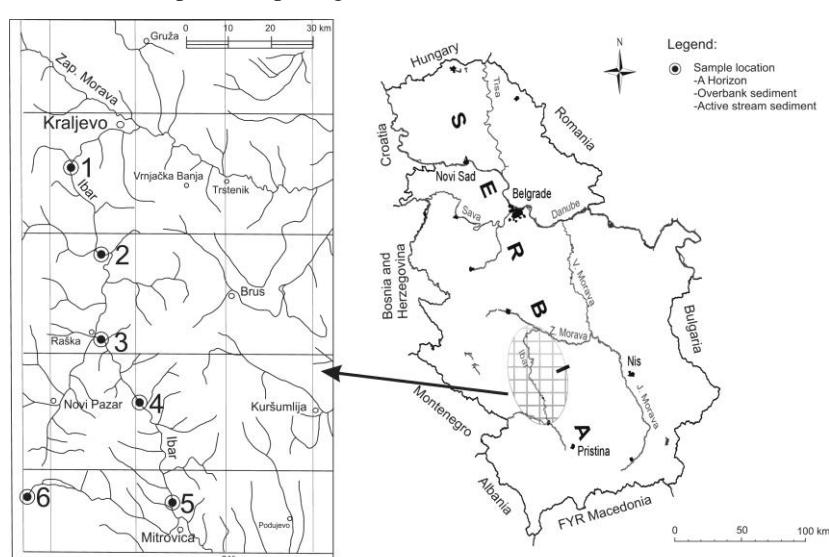
riverbank profiles (A-horizon, OB-overbank sediment and S-stream sediment) [6,7,8]. Since the riverbank sediments are used, beside in the process of making regional geochemical map, also in defining the anthropogenic influence on the living environment, the WEST methodology (Western European Geological Surveys) is usually used in researches. Due to these reasons, the basin area of the river Ibar was selected, where deposits of lead and zinc were located, which are characterized by very complex geological composition. Geochemical mapping the riverbank profiles of the river Ibar basin, included the part of the Vardar zone area and inner Dinarides. Two complexes stand out: the Volcanic zone of Kopaonik and the area of mountain Rogozna.

The volcanic zone of Kopaonik is located on the both sides of the river Ibar, in length of about 60 km and width of 35 km (direction of extending (NNW – SSE), including the area from the mouth in West Morava in the north till Leposavić in the south. It continues onto volcanogenic complex of the mines of Pb and Zn “Trepča”. Volcanic activity took place in three phases: preplutonic phase - dalto-andesites, followed by larger occurrences of volcanic breccias, tuffs and tuffites; sinplutonic phase-grano-

diorites, quartzmonzonites and quartzdiorites with occurrences of volcanic breccias, tuffs and tuffites and postplutonic phase - basalts and andesite basalts. Volcanics and pyroclastites of Rogozna are different from Kopaonik's by younger postplutonic phases of volcanic activity. Among larger structural forms, the structural zone of Studenica is of relevance, whose system of ruptures goes along with the flow of the river Studenica (tributary of Ibar), and it is difficult to follow it in the Ibar ultramaphite complex.

## MATERIALS AND METHODS

The basin area of the river Ibar with its tributaries – rivers Ribnica, Lopatnica, Studenica, Raška, Ljudska, Jošanica, Drenska, Kozareva, Vidrenjak, covers the area of about 7000 km<sup>2</sup>. In the phase of regional geochemical prospection, mapping of riverbank profiles of alluvial plains and river valleys in the part of southern and central Serbia was conducted. Sampling net was adjusted to the morphological and hydrographic characteristics of the terrain, in accordance to the map scale 1:1000000 (Figure 1).



**Figure 1** Geochemical map with the sample locations

According to the WEGS recommendation, at selected locations (shown in Figure 1), samples were collected from:

- A – horizon, at depth up to 20 cm close to surface, which is polluted by the human impact, weight 5kg;
- Subsurface material “overbank sediment” sampled at depth of 1 - 1,5 m, in accordance to the lithological changes of deposited sediments, weight 5-15 kg;
- Contemporary active stream sediment, weight 5 kg, for correlation with the results from overbank sediments, formed in the preindustrial era.

The samples were dried at temperature of 80 °C and sieved through sieves dimensions up to 2 mm; 0.5-2 mm; 0.5–0.18 mm; 0.18–0.125 mm. For fractions smaller than 0.125 mm, laboratory tests were conducted. Chemical analyses methods that were applied are: Atomic Absorption Spectrophotometry (AAS) and Inducted Coupled Plasma-Atomic-Emission Spectrophotometry (ICP-AES). Samples were prepared by open digestion with mineral acids: with “aqua regia” (mixture HCl:NO<sub>3</sub>= 3:1) for: Ag, Au, Bi, Cd, Co, Cu, Mo, Ni, Pb, Sb, V and Zn; with “modified aqua regia” for: P and S; and separation with HF, NH<sub>3</sub> and HClO<sub>4</sub> for: B, Ba, Be, Cr, Cs, Li, Rb and Sr.

The international geochemical standards of granite G-1 and diabase W-1 were used in the analytical process, and the samples were also checked in the other laboratories as well. In all samples sedimentological, spectrochemical, radiometric and partially mineralogical researches were performed. In collected samples with low content of U (< 50 ppm), contents of total U, <sup>232</sup>Th and <sup>40</sup>K

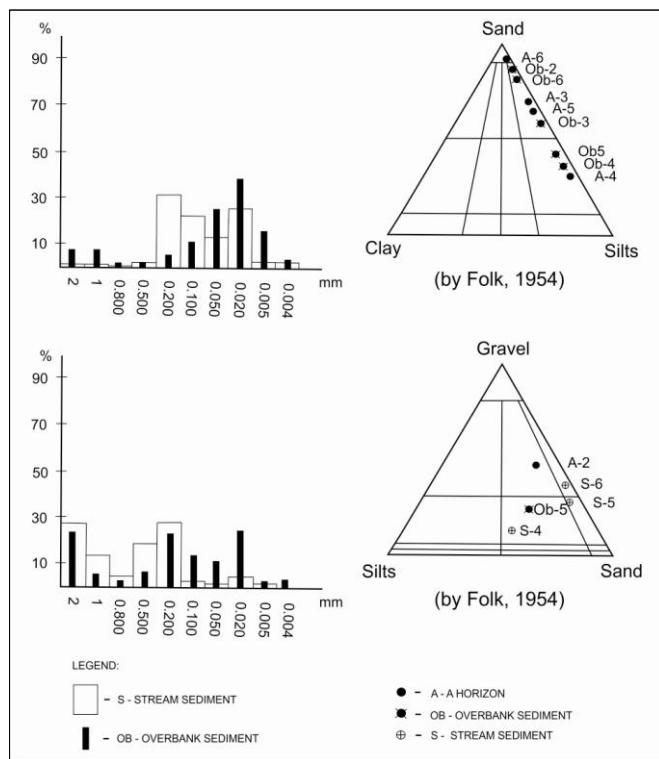
were determined. Measurements were conducted using a scintillation detector 4” x 4” of Bikron company with crystal made of NaI with multiplicative analyzer (MCA; 4096 channels) type “ORTEC-7500”. The analyses are based on the measurements of high energy radiations (0-3 meV). For calibration of the spectrum and calculation of natural radionuclides concentration, the standards of uranium ore (U) and thorium (Th) were used, “New Bruncwick Laboratory” (USAEC), NBL No. 103 0.005%, NBL No. 107 0.10% Th. Potassium chloride was used (r.a.) as the standard for potassium.

## RESULTS AND DISCUSSION

In accordance to the geological characteristics of the terrain in the riverbank profile, the geochemical track of elements which reflect the composition of the spring material which is deposited in the fluvial plain of the basin area of the river Ibar, is preserved. On the basis of the results of granulometric examinations the collected sediments of deposit of selected locations were determined according to classification of Folk, 1954 [9] (Figure 2):

- A - horizon as: sandy alevrite, alevrite sand, sand, alevrite sandy gravel;
- OB - overbank sediment as: sandy alevrite, alevrite sand, gravelly alevrite sand, sand;
- S - stream sediment as: gravelly alevrite sand, gravelly sand, sandy gravel, coarse-grained sand, gravel.

The geochemical track of riverbank profiles at selected locations: 1, 2, 3, 4, 5, 6 is shown in Table 1 and sampling places are presented in a geochemical map (Figure 1).

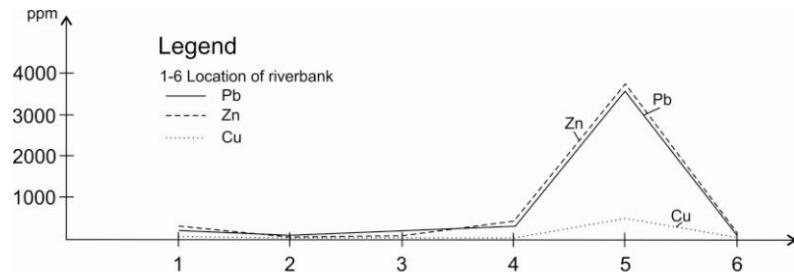


**Figure 2** Histogram-fraction distribution in profile of the river Ibar and Folk classification [9]

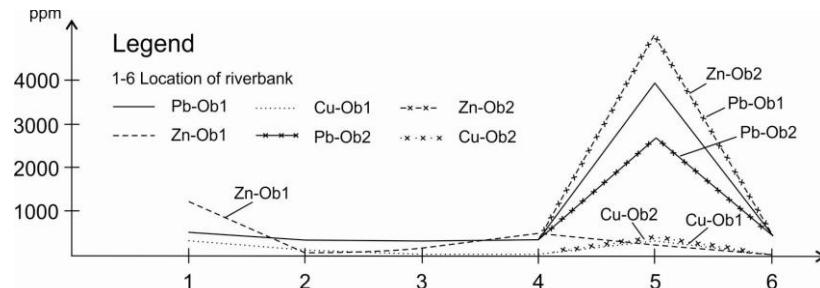
**Table 1** Contents of elements in the riverbank profiles from the spring part of the river Ibar (location 6) till the mouth in the West Morava (location 1)

River Ibar	Pb, ppm	Zn, ppm	Cu, ppm	Cd, ppm	As, ppm	Fe, ppm	Uu, ppm
Location 1	A	173	276	32	0.9	-	-
	OB	190	1333	28	3.3	-	-
	S	127	1220	27	3.6	-	-
Location 2	A	85	65	35	1.2	13.9	31400
	OB	95	78	35	1.3	9.8	35700
	S	90	81	35	1.3	11.6	42800
Location 3	A	110	81	35	0.9	8.8	22500
	OB	110	25	35	0.6	11.5	18700
	S	60	72	35	1.2	8.2	25000
Location 4	A	210	311	68	1	3.5	70525
	OB	390	392	61	2	7.8	72540
	S	530	712	100	4	17.4	76895
Location 5	A	3500	3710	345	26	78.8	150150
	OB	4000	297	491	11	36.3	241800
	OB	3070	4995	542	26	112	108875
Location 6	S	700	1703	79	13	7.5	80145
	A	85	99	68	1	10.1	59020
	OB	35	101	47	□ 1	7.0	45045
	S	100	88	44	1.0	3.2	34250
							3.2

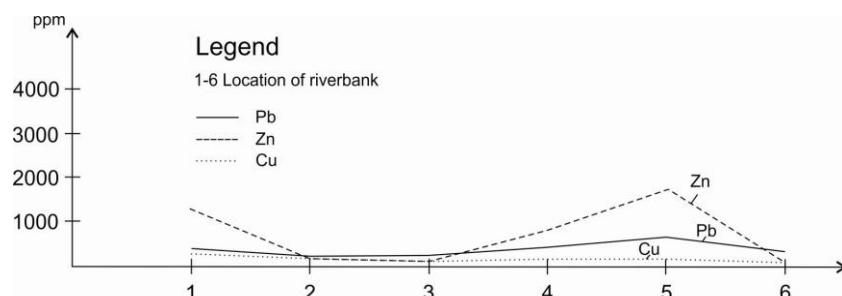
The results of contents variations of Pb, Zn, Cu, Cd, As are shown in diagrams for every riverbank profile per locations



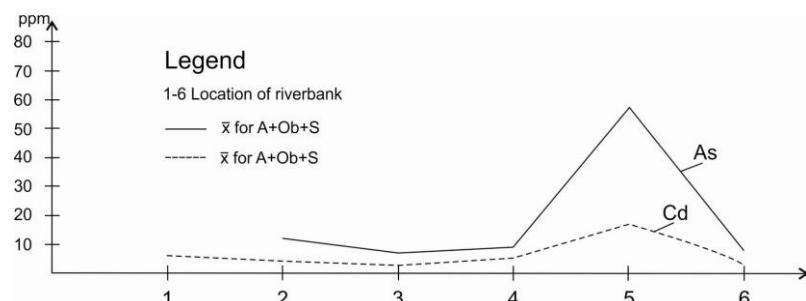
**Figure 3** Content variations of Pb, Zn and Cu in A-horizon at locations of the river Ibar



**Figure 4** Content variations of Pb, Zn and Cu in OB-overbank sediments of the river Ibar



**Figure 5** Content variations of Pb, Zn and Cu in S-stream sediments of the river Ibar



**Figure 6** Content variations of As and Cd in the riverbank profiles of the river Ibar

Anomaly concentrations of Pb, Zn, Cu, Cd, As and Fe are of twofold origin: from rocks in which there is a fom of high values (Table 2) and elements which origi-

nate from ore (ore halda, old mining works), metallurgy processes, agrochemical compounds rich in metals, material for filling the roads, wastewater and other.

**Table 2** Average contrast among the metal contents in the zone without ores and in the peripheral ore

Main metals	(A) Content in magmatic rocks, ppm	(B) Content in the ores that are being processed, ppm	Contrast ratio (B/A)
Lead, Pb	16 <sup>a</sup>	50000 <sup>b</sup>	3000
Zinc, Zn	80 <sup>a</sup>	80000 <sup>b</sup>	1000
Copper, Cu	70 <sup>a</sup>	10000 <sup>b</sup>	140
Chrome, Cr	2000 <sup>c</sup>	250000 <sup>b</sup>	125
Nickel, Ni	160 <sup>d</sup>	15000 <sup>b</sup>	95

<sup>a</sup> [10]

<sup>b</sup> Data for Pb, Zn, Cu [11]

<sup>c</sup> Medium content in ultrabasic rocks [12]

<sup>d</sup> Medium content in gabbro [13]

Contrasts in the metal contents between the secondary geochemical anomalies and normal fom depend on many factors: contrast between ore and surrounding rock, relative mobility of elements in scattering environment, concentration dilution by sterile material. For different types of mineral deposits, the primary contrast varies in wide limits (Table 2). The primary contrast is more sustained by immobile elements (Pb) than mobile elements (Zn, Cu and U), which are subjected to leaching, whose level is determined by decay intensity, velocity of water movement, pH value and many other factors which influence on the form of scattering. In water, contrast is also in the function of mobility [13]. The most mobile elements show the biggest contrast. Mobile elements which deposit at relatively small changes of chemical and biological conditions show the most severe contrast in hydromorphic anomalies of soil and sediments [14].

In the prospected area of the river Ibar basin, the main rocks of high fom values are located. The most distinctive is a group of ultrabasic rocks (peridotites, serpentinites) with high contents of Cr, Ni, Co and Mg, then a group of basic rocks (gabbro, basalts and diabase) with high contents of Fe, Ti and Cu. In granite, granodiorites, quartz diorites and diorite Cu, Ag, Au, Zn, Cd, Hg,

Ge, Sn, Pb, As, Sb, Bi, Nb, Ta, S, Se, Te, Mo, W, U, Fe, Co and Ni are concentrated. Content of lead in magmatic rocks is changeable and depends on the character of these rocks. In the basic rocks, content of Pb is low and it rises with the acidity of magmatic rocks. So the content of Pb in granites is five times higher than the content in gabbro. Distribution of Zn in rocks of different composition is partially similar to the distribution of Fe, beginning from the basic magmatic rocks percentage of Zn rises and in granodiorites achieves the highest values. According to the level of concentration, a distinct connection of Cu with basic rocks can be observed in some magmatic rocks. The connection of As with certain magmatic rocks refers to the medium acid rocks which have an increased content of that metal. For the influence of chemical composition of riverbank profiles in the basin area of the river Ibar, beside geological composition, the area of northern part of Kosovska Mitrovica is of special significance including the mines of Pb and Zn: Crnac, Belo brdo (pit excavation) and Koporiš surface excavation, flotation in Leposavić and me-tallurgy complex which includes the chemical industry of Zn and the Factory of batteries. Anthropogenic influence is the strongest at location of

riverbank profile 5 in which there are extremely high concentrations of Pb, Zn, Cu, As and Cd (Figures 3-6) and Fe in A-horizon, OB-overbank sediment and S-stream sediment and it is located down

stream from Kosovska Mitrovica. The highest content of  $^{238}\text{U}$ ,  $^{232}\text{Th}$ ,  $^{40}\text{K}$  i  $^{226}\text{Ra}$  are found in the stream sediments at location 5, downstream from Kosovska Mitrovica (Table 3).

**Table 3** *Contents of natural radionuclides  $^{238}\text{U}$ ,  $^{232}\text{Th}$ ,  $^{40}\text{K}$ ,  $^{226}\text{Ra}$  in the riverbank profiles from the spring part of the river Ibar (location 6) till the mouth in the West Morava (location 1)*

River Ibar		$^{238}\text{U}$ , ppm	$^{232}\text{Th}$ , ppm	$^{40}\text{K}$ , %	$^{226}\text{Ra}$ , ppm	Th/U
<b>Location 1</b>	<b>A</b>	2.68	6.65	1.25	0.000090	2.48
	<b>OB</b>	2.09	8.32	1.42	0.000071	3.98
	<b>S</b>	2.45	7.89	1.53	0.000083	3.22
<b>Location 2</b>	<b>A</b>	0.43	0.89	0.13	0.000015	2.05
	<b>OB</b>	1.89	7.60	1.15	0.000064	4.03
	<b>S</b>	2.48	7.43	1.23	0.000084	3.00
<b>Location 3</b>	<b>A</b>	2.28	7.75	1.50	0.000077	3.40
	<b>OB</b>	2.10	8.34	1.47	0.000071	3.97
	<b>S</b>	2.16	6.14	1.18	0.000073	2.84
<b>Location 4</b>	<b>A</b>	1.70	6.31	1.33	0.0000574	3.71
	<b>OB</b>	1.53	5.09	1.24	0.0000516	3.33
	<b>S</b>	2.26	6.54	1.39	0.0000763	2.89
<b>Location 5</b>	<b>A</b>	2.15	3.65	1.08	0.0000726	1.70
	<b>OB</b>	2.61	2.95	0.70	0.0000881	1.13
	<b>OB</b>	1.52	3.58	0.68	0.0000513	2.36
<b>Location 6</b>	<b>S</b>	6.27	18.30	2.70	0.0002117	2.92
	<b>A</b>	1.14	5.51	1.36	0.0000476	3.91
	<b>OB</b>	1.31	5.32	1.19	0.0000442	4.06
	<b>S</b>	1.13	3.53	1.26	0.0000381	3.12

The origin of anomalous concentrations of  $^{238}\text{U}$ ,  $^{232}\text{Th}$ ,  $^{40}\text{K}$ ,  $^{226}\text{Ra}$  can be associated with a fluvial transport of radioactive elements from Kosovo area by the river Sitnica, which flows into the river Ibar, upstream from location 5 (Figure 1). The presence of lead and zinc mines in the immediate vicinity (upstream of location 5) requires further research, but in the regional perception of the ecological status of the region, an analysis of content the chemical elements in the riverbank profile is evident and significant. Sampling methodology provides representative data in a regional sense and it is important in the selection of geopathogenic zones of influence the natural radionuclides [15] and other toxic elements.

## CONCLUSION

Geochemical mapping of riverbank profiles which includes: A-horizon, OB-over-

bank sediment and S-stream sediment, is of significance for proper determination of scattering halos, formed depending on geological composition or anthropogenic influence. The applied sampling methodology of riverbank profiles and analytical methods are of special relevance in researching the mineral raw materials and making regional, semidetail and detail geochemical maps. Correlation of contents the chemical elements in the main rocks and defined anthropogenic influence in the riverbank profile, define the state in the living environment. By making geochemical maps in different environments of the geosphere, a data base was formed for defining the state of the living environment in the preindustrial and postindustrial period, and also monitoring was established. The research results are multipurpose, especially for marking the area of biogeochemical endemia, making of

geomedicine maps, researching the mineral raw materials and the other study multidisciplinary researches.

## REFERENCES

- [1] R. T. Ottesen, J. Bogen, B. Bølviken, T. Volden, Overbank sediment: A Representative Sample Medium for Regional Geochemical Mapping, *Journal of Geochemical Exploration*, 32 (1989), 257-277.
- [2] M. G. Macklin, Metal Contamination of Soils and Sediments: A Geographical Perspective. In: Newson, M.D. (Ed.), *Managing the Human Impact on the Natural Environment: Patterns and Processes*, London, Belhaven Press, 1992, 172-195.
- [3] M. G. Macklin, J. Ridgway, D. G. Passmore, B.T. Rumsby, The Use of Overbank Sediment for Geochemical Mapping and Contamination Assessment: Results from Selected English and Welsh Floodplains, *Applied Geochemistry* 9 (1994), 689-700.
- [4] B. Bølviken, J. Bogen, A. Demetriadis, W. De Vos, J. Ebbing, R. Hindel, R.T. Ottesen, R. Salminen, O. Schermann, R. Swennen. Final Report of the Working Group on Regional Geochemical Mapping 1986-1993. Forum of European Geological Surveys (foregs), Geological Survey of Norway Open File Report, 1993, No. 93-092.
- [5] V. Gordanić, D. Milovanović, M. Vidović, S. Rogan, I. Trajković, Geochemical Map of Eastern Serbia in 1:1000000 and Application in Defining the Ecological Status of Selected Areas, Proceedings of the 17th Meeting of the Association of European Geological Societies – MAEGS 17, Serbian Geological Society, Belgrade, Serbia, 2011, 187-191.
- [6] V. Gordanić, A. Ćirić, D. Jovanović, The Use Overbank Sediments Data for Geochemical Mapping and Contamination Assessment: Results from Selected Floodplains of Serbia, Goldschmidt Conference Abstracts “Goldschmidt 2007”, Cologne, Germany, *Geochimica et Cosmochimica Acta*, 71 (2007), 15, 1, A346.
- [7] V. Gordanić, A. Ćirić, D. Jovanović, Regional Geochemical Mapping – Ecological Significance. Goldschmidt Conference Abstracts “Goldschmidt 2008”, Vancouver, Canada, *Geochimica et Cosmochimica Acta*, 72 (2008), 12, A321.
- [8] V. Gordanić, V. Spasić-Jokić, Geochemical indicators in identification of geopathogenic zones of natural radioactivity. MD-Medical Data, 5 (2013), 2, 121-124.
- [9] R. L. Folk, The distinction between grain size and mineral composition in sedimentary rock nomenclature. *Journal of Geology* 62 (1954), 4, 344-359.
- [10] J. Green, Geochemical Table of the Elements for 1959, *Geological Society of America Bulletin* 70 (1959), 1127-1184.
- [11] M. Fleischer, The Abundance and Distribution of the Chemical Elements in the Earth Crust, *Journal of Chemical Education*, 31 (1954), 9, 446-455;
- [12] A. P. Vinogradov, Regularity of Distribution of Chemical Elements in the Earth Crust. *Geochemistry*, 1(1956) 1-43.
- [13] R. Marković, J. Stevanović, M. Gvozdenović, J. M. Jakšić, Treatment of Waste Sulfuric Acid Copper Electrolyte, *Mining and Metallurgy Engineering Bor*, 3 (2014), 141-152.
- [14] L. Zupunski, V. Spasic-Jokic, V. Gordanic, Chapter IX: Low Dose Exposure to Radionuclides in Soil, In: Gerada, J.G. (Ed.), *Radionuclides: Sources, Properties and Hazards*, New York, Nova Science Publishers, Inc., 2012, 151-170.
- [15] V. Spasic-Jokic, Lj. Zupunski, Z. Mitrovic, B. Vujicic, I. Zupunski, Lj. Jankovic-Mandic, V. Gordanic, Environmental Risk of Natural Radiation Sources, 2011 IEEE International Workshop on Medical Measurements and Applications Proceedings (MeMeA), Bari, Italia, 2011, 638-641.

Vojin Gordanić\*, Milka Vidović\*, Ivana Trajković\*, Saša Rogan\*

## GEOHEMIJSKO KARTIRANJE OBALSKIH PROFILA U SLIVNOM PODRUČJU REKE IBAR: ULOGA U USPOSTAVLJANJU GEOHEMIJSKE OSNOVE ZA PROCENU ANTROPOGENOG UTICAJA NA ŽIVOTNU SREDINU\*\*

### Izvod

*Kartiranje obalskih profila u slivnom području reke Ibar vršeno je u cilju izrade geochemijske karte Srbije 1:1000000. U ovom području se nalaze ležišta olova i cinka, a karakteriše ga veoma složen geološki sastav. Mreža uzorkovanja na izabranim lokacijama obalskih profila prilagođena je morfološkim i hidrografskim karakteristikama terena. Na svakom profilu prikupljeni su uzorci iz A-horizonta, overbank sedimenta i aktivnog strim sedimenta, prateći promene litoloških članova, u skladu sa metodologijom WEGS (Western European Geological Surveys).*

*Sačuvani geochemijski zapis u overbank sedimentu je od posebnog značaja za korelaciju rezultata hemijskih elemenata u površinskom delu (A-horizont) i aktivnog savremenog strim sedimenta. U analitičkom postupku, pored određivanja sadržaja Pb, Zn, Cu, Co, Ni, Cr, Sb, V, Cd i drugih elemenata, vršena su radiometrijska ispitivanja sadržaja  $U^{238}$ ,  $Th^{232}$  i  $K^{40}$ , kao i odgovarajuće sedimentološke analize. Na bazi rezultata geochemijske prospekcije formirana je baza podataka koja čini osnovu za procenu antropogenog uticaja na životnu sredinu ruralnih naselja u slivnom području reke Ibar. U skladu sa geološko-strukturalnim i morfološkim karakteristikama terena, rezultati su primenjivi u istraživanju mineralnih sirovina, u poljoprivredi, šumarstvu, geomedicini i sl.*

**Ključne reči:** overbank, strim sedimenti, A-horizont, geochemijsko kartiranje, obalski profil

### UVOD

Overbank sediment (materijal deponovan u aluvijalnoj ravnici izvan drenažnog kanala) se obično koristi prilikom izrade regionalnih geochemijskih karata [1]. Proučavanjima u Velikoj Britaniji pokazano je da postoji „tesna veza“ između rudničke kontaminacije i sadržaja metala u savremenim overbank sedimentima [2,3]. Prime nu OB-overbank sedimenta kao sredine

pogodne za izradu geochemijskog atlasa zapadne Evrope i definisanje antropogenog uticaja na životnu sredinu, zastupali su Bolviken i autori [4]. Prilikom izrade regionalne geochemijske karte 1:1000000 Srbije [5], korišćen je overbank sediment, a za istraživanja su korišćene slivne površine od 60-600 km<sup>2</sup>. Značaj overbank sedimenta u definisanju ekološkog statusa i izradi

\* Univerzitet u Beogradu, Naučna ustanova Institut za hemiju, tehnologiju i metalurgiju, Centar za ekologiju i tehnokonomiku, Njegoševa 12, Beograd, e-mail: trajkoviciana@yahoo.com

\*\* Ovaj rad je realizovan uz podršku Ministarstva prosvete, nauke i tehnološkog razvoja Republike Srbije (projekat OI 176018: „Geološka i ekotoksikološka istraživanja u identifikaciji geopatogenih zona toksičnih elemenata u akumulacijama vode za piće– istraživanje metoda i postupaka smanjivanja uticaja biogeohemijskih anomalija“)

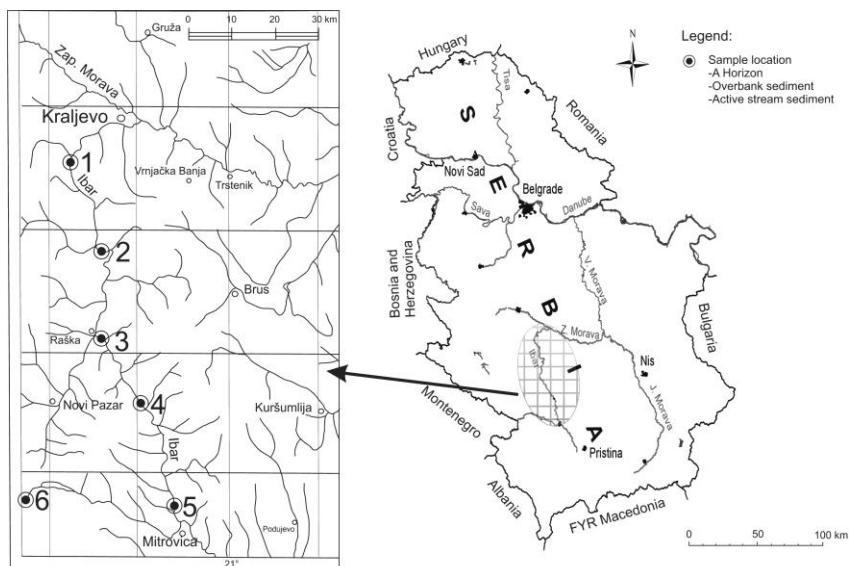
regionalne geochemijske karte Srbije prikazan je na lokacijama obalskih profila (A-horizonta, OB-overbank sedimenta i S-strim sedimenta) [6, 7, 8]. Pošto overbank sedimenti pored izrade geochemijske karte služe za definisanje stanja antropogenog uticaja na životnu sredinu, u istraživanjima se obično primenjuje metodologija WEGS (Western European Geological Surveys). Iz tih razloga izabrano je slivno područje reke Ibar u kome se nalaze ležišta olova i cinka, i koje karakteriše veoma složen geološki sastav. Geohemijsko kartiranje obalskih profila sliva reke Ibar, obuhvatilo je deo područja vardarske zone i unutrašnjih dinarida. Izdvajaju se dva kompleksa: Vulkanska zona Kopaonika i područje planine Rogozne.

Vulkanska zona Kopaonika nalazi se sa obe strane reke Ibar, u dužini oko 60 km i širine 35 km (pravca pružanja SSZ-JJ), zahvatajući prostor od ušća u zapadnu Moravu na severu do Leposavića na jugu. Ona se nastavlja na vulkanogeni kompleks rudnika Pb i Zn „Trepča“, a prošla je kroz tri faze vulkanske aktivnosti: predplutonsku fazu (dalto-andeziti, praćeni većim poj-

vama vulkanskih breča, tufova i tufita), sinplutonsku (granodioriti, kvarcmonconiti i kvarcdioriti sa pojavama vulkanskih breča, tufova i tufita) i postplutonsku fazu (bazalti i andezit bazalti). Vulkaniti i piroklastiti Rogozne se razlikuju od kopaoničkih samo mlađim postplikativnim fazama vulkanske aktivnosti. Od većih strukturnih formi, od značaja je strukturalna zona Studenice čiji sistem razloma ide tokom reke Studenice (pritoke Ibra), a u ibarskom ultramafitskom kompleksu se teško prati.

## MATERIJALI I METODE

Slivno područje reke Ibar sa svojim prijekama – rekama Ribnica, Lopatnica, Studenica, Raška, Ljudska, Jošanica, Drenská, Kozareva, Vidrenjak, obuhvata površinu od oko 7000 km<sup>2</sup>. U fazi regionalne geochemijske prospekcije, izvršeno je kartiranje obalskih profila aluvijalnih ravnica, rečnih dolina dela južne i centralne Srbije. Mreža uzorkovanja prilagođena je morfološkim i hidrografskim karakteristikama terena, u skladu sa razmerom karte 1:1000000 (Slika 1).



**Sl. 1. Geochemijska karta sa lokacijama uzorkovanja**

Prema preporuci WEGS-a (Zapadno-Evropske Geohemijske Asocijacije), na izabranim lokacijama (prikazanim na Slici 1), prikupljeni su uzorci iz:

- A - horizonta, na dubini do 20 cm bližu površine, koji je zagađen uticajem čoveka, a težina uzorka je iznosila 5 kg;
- OB - pod površinskim materijal „overbank sediment“ uzorkovan na dubini 1-1,5 m, u skladu sa litološkim promenama deponovanih sedimenata, pri čemu je težina uzorka iznosila 5-15 kg;
- S - savremeni aktivni strim sediment, koji je uzorkovan radi korelacije sa rezultatima iz obalskih profila formiranih u preindustrijskom dobu a težina uzorka je iznosila 5 kg .

Uzorci su sušeni na temperaturi od 80°C i prosejani na sitima dimenzije do 2 mm; od 2-0,5 mm; 0,5-0,18 mm; 0,18-0,125 mm. Od frakcija manjih od 0,125 mm izvršena su laboratorijska ispitivanja. Od metoda hemijske analize, primenjene su: atomsko apsorpciona spektrofotometrija (AAS) i ICP-AES (Indukovano spregnuta plazma-atomsko-emisiona spektrofotometrija). Uzorci su pripremani otvorenom digestijom sa mineralnim kiselinama: sa „carskom vodom“ (smeša HCl:HNO<sub>3</sub>= 3:1) za: Ag, Au, Bi, Cd, Co, Cu, Mo, Ni, Pb, Sb, V i Zn; sa „modifikovanom carskom vodom“ za: P i S i razlaganjem sa HF, NH<sub>3</sub>, HClO<sub>4</sub> za: B, Ba, Be, Cr, Cs, Li, Rb i Sr.

U analitičkom postupku korišćeni su međunarodni geohemijski standardi granita G-1 i dijabaza W-1, a uzorci su i proveravani u nekoliko laboratorija. U svim uzorcima vršena su sedimentološka, spektrohemiska, radiometrijska i delimično mineraloška ispitivanja. U prikupljenim uzorcima sa niskim sadržajem U (< 50 ppm), određeni

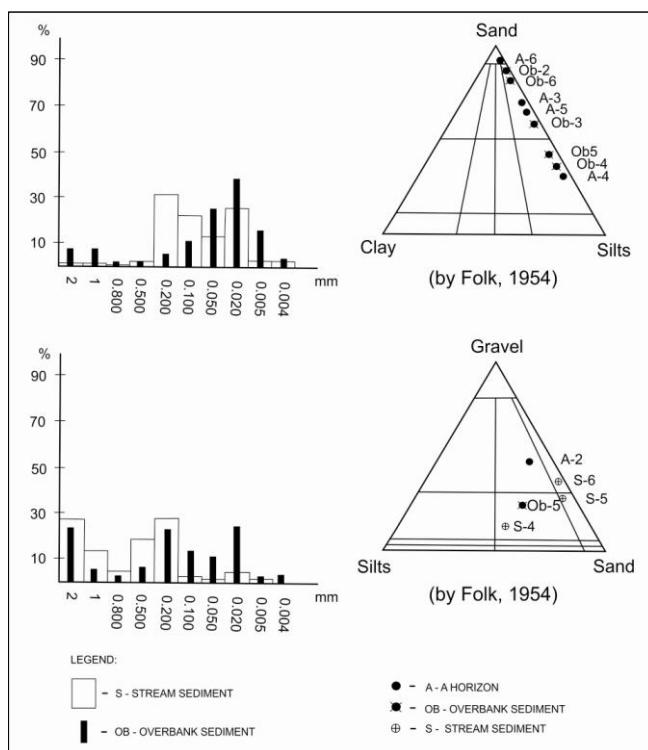
su sadržaji ukupnog U, <sup>232</sup>Th i <sup>40</sup>K. Merenja su izvršena pomoću scintilacionog detektora 4" x 4", firme Bikron sa kristalom od NaI sa multiplikativnim analizatorom (MCA; 4096 kanala) tipa „ORTEC-7500“. Analize se zasnivaju na merenju zračenja visokih energija (0-3 meV). Za kalibraciju spektra i proračun koncentracije prirodnih radioelementa, korišćeni su standardi rude urana U i torijuma Th, „New Bruncwick Laboratorija“ (USAEC), NBL. No. 103 0,005% U i NBL. No. 107 0,10% Th. Kao standard kalijuma, upotrebljen je kalijum-hlorid (r.a.).

## REZULTATI I DISKUSIJA

U skladu sa geološkim karakteristikama terena u obalskom profilu, sačuvan je geohemijski zapis elemenata koji odstičavaju sastav izvorišnog materijala, a koji je deponovan u fluvijalnoj ravni slivnog područja reke Ibar. Na osnovu rezultata granulometrijskih i hemijskih ispitivanja, prikupljeni sedimenti depozita izabranih lokacija determinisani su prema klasifikaciji Folk-1954 (Slika 2):

- A – horizont kao: peskoviti alevrit, alevritski pesak, pesak, alevritsko peskoviti šljunak;
- OB – overbank sediment kao: peskoviti alevrit, alevritski pesak, šljunkoviti alevritski pesak, pesak;
- S – strim sediment kao: šljunkovito alevritski pesak, šljunkoviti pesak, peskoviti šljunak, krupnozrni pesak, šljunak.

Geohemijski zapis obalskih profila na izabranim lokacijama: 1, 2, 3, 4, 5, 6 prikazan je u Tabeli 1, a mesta uzorkovanja su predstavljena na geohemijskoj karti (Slika 1).

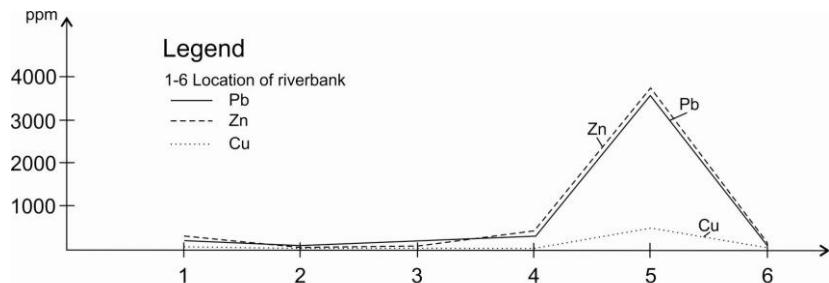


Sl. 2. Histogram distribucija frakcija u profilu reke Ibar i klasifikacija po Folku [9]

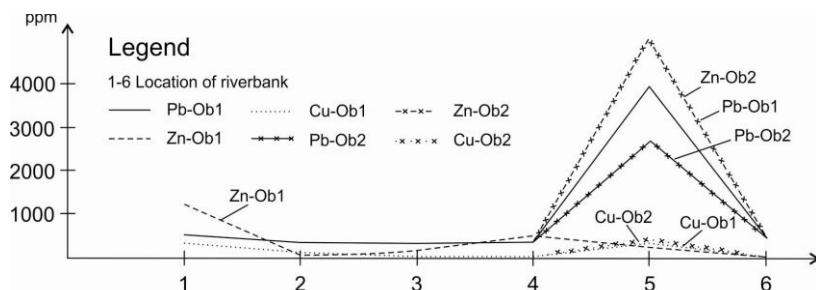
**Tabela 1.** Sadržaj elemenata u obalskim profilima od izvorišnog dela reke Ibar (lokacija 6) od ušća u Zapadnu Moravu (lokacija 1).

Reka Ibar	Pb, ppm	Zn, ppm	Cu, ppm	Cd, ppm	As, ppm	Fe, ppm	Uu, ppm
Lokacija 1	A 173	276	32	0.9	-	-	-
	OB 190	1333	28	3.3	-	-	-
	S 127	1220	27	3.6	-	-	-
Lokacija 2	A 85	65	35	1.2	13.9	31400	4.6
	OB 95	78	35	1.3	9.8	35700	4.8
	S 90	81	35	1.3	11.6	42800	4.0
Lokacija 3	A 110	81	35	0.9	8.8	22500	5.6
	OB 110	25	35	0.6	11.5	18700	9.8
	S 60	72	35	1.2	8.2	25000	18.2
Lokacija 4	A 210	311	68	1	3.5	70525	3.5
	OB 390	392	61	2	7.8	72540	3.5
	S 530	712	100	4	17.4	76895	3.2
Lokacija 5	A 3500	3710	345	26	78.8	150150	0.4
	OB 4000	297	491	11	36.3	241800	-
	OB 3070	4995	542	26	112	108875	4.2
Lokacija 6	S 700	1703	79	13	7.5	80145	7.7
	A 85	99	68	1	10.1	59020	3.0
	OB 35	101	47	1	7.0	45045	6.7
	S 100	88	44	1.0	3.2	34250	3.2

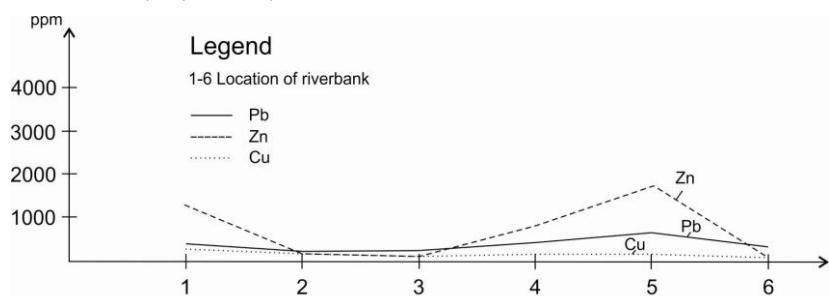
Rezultati varijacije sadržaja Pb, Zn, Cu, Cd, As prikazani su na dijagramima za svaki obalski profil po lokacijama za A - horizont, OB - overbank sedimenta i S - strim sedimenta (Slike 3-6).



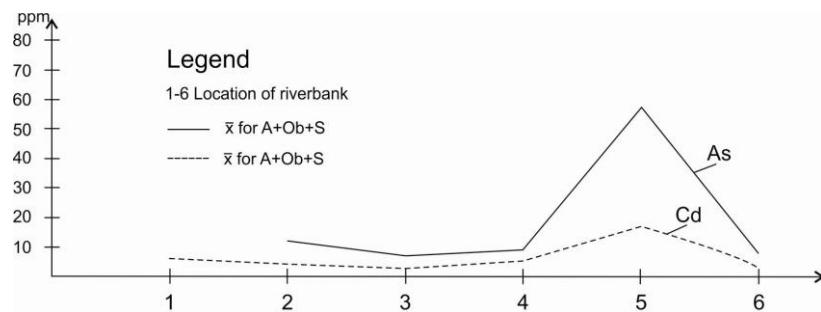
Sl. 3. Varijacije sadržaja Pb, Zn i Cu u A-horizontu na lokacijama reke Ibar



Sl. 4. Varijacije sadržaja Pb, Zn i Cu u OB-overbank sedimentima reke Ibar



Sl. 5. Varijacije sadržaja Pb, Zn i Cu u S-strim sedimentima reke Ibar



Sl. 6. Varijacije sadržaja As i Cd u obalskim profilima reke Ibar

Anomalne koncentracije Pb, Zn, Cu, Cd, As i Fe su dvojakog porekla: iz stena u kojima je fon visokih vrednosti (Tabela 2) i elemenata koji potiču od rude (rudničke

halde, stari rudarski radovi), metalurški procesi, agrohemijnska jedinjenja bogata metalima, materijal za nasipanje puteva, otpadne vode i dr.

**Tabela 2.** Prosečan kontrast između sadržaja metala u neorudnjenoj zoni i u perifernoj rudi

Glavni metali	(A) Sadržaj u magmatskim stenama (ppm)	(B) Sadržaj u rudama koje se obrađuju (ppm)	Kontrast odnos B/A
Olovo, Pb	16 <sup>a</sup>	50000 <sup>b</sup>	3000
Cink, Zn	80 <sup>a</sup>	80000 <sup>b</sup>	1000
Bakar, Cu	70 <sup>a</sup>	10000 <sup>b</sup>	140
Hrom, Cr	2000 <sup>c</sup>	250000 <sup>b</sup>	125
Nikl, Ni	160 <sup>d</sup>	15000 <sup>b</sup>	95

<sup>a</sup> [10]

<sup>b</sup> Rezultati za Pb, Zn, Cu [11]

<sup>c</sup> Prosečna vrednost u ultrabajnim stenama [12]

<sup>d</sup> Prosečna vrednost u gabru [13]

Kontrasti u sadržajima metala između sekundarnih geohemijiskih anomalija i normalnog fona je u zavisnosti od mnogih faktora: kontrasta između rude i okolne stene, relativne mobilnosti elemenata u sredini rasejavanja, razblaženjem koncentracije sterilnim materijalom. Za različite tipove mineralnih ležišta, primarni kontrast varira u širokim granicama (Tabela 2). Primarni kontrast više održavaju imobilni elementi (Pb) nego mobilni elementi (Zn, Cu i U), koji su podložni izluživanju, čiji je stepen određen intenzitetom raspadanja, brzinom kretanja vode, veličinom pH vrednosti i mnogim drugim faktorima koji utiču na oblik rasejavanja [13]. U vodi je kontrast takođe u funkciji mobilnosti. Najveći kontrast pokazuju najmobilniji elementi. Mobilni elementi koji se talože kod relativno malih promena hemijskih i bioloških uslova pokazuju najošttriji kontrast u hidromorfnim anomalijama zemljista i sedimenata [14].

U prospektovanom području sliva reke Ibar nalaze se matične stene visokih vrednosti fona. Najizrazitija je grupa ultrabajčnih stena (peridotiti, serpentiniti) sa visokim sadržajem Cr, Ni, Co i Mg, zatim grupa bazičnih stena (gabro, bazalti i dijabazi) sa visokim sadržajem Fe, Ti i Cu.

U granitu, granodioritu, kvarcdioritu i dioritu su koncentrisani: Cu, Ag, Au, Zn, Cd, Hg, Ge, Sn, Pb, As, Sb, Bi, Nb, Ta, S, Se, Te, Mo, W, U, Fe, Co i Ni. Sadržaj olova u magmatskim stenama je promenljiv i zavisi od karaktera tih stena. U bazičnim stenama, sadržaj Pb je nizak i raste sa kiselosću magmatskih stena. Tako je sadržaj Pb u granitima pet puta veći od sadržaja u gabru. Raspodela Zn u stenama različitog sastava delimično je slična raspodeli Fe, počev od bazičnih magmatskih stena udeo Zn raste i u granodioritima dostiže najveće vrednosti. Prema stepenu koncentracije u pojedinim magmatskim stenama zapaža se izrazita povezanost Cu sa bazičnim stenama. Povezanost As sa određenim magmatskim stenama odnosi se na srednje kisele stene, koje imaju povećan sadržaj tog metala. Na uticaj hemijskog sastava obalskih profila u slivnom području reke Ibar, pored geološkog sastava, od posebnog značaja je područje severnog dela Kosovske Mitrovice u kome se nalaze rudnici Pb i Zn: Crnac, Belo brdo (jamski kop) i Koporiš (površinski kop), zatim flotacija u Leposaviću i metalurški kompleksi koji obuhvata hemijsku industriju Zn i fabriku akumulatora. Antropogeni uticaj najizraženiji je na lokaciju obalskog

profila 5 u kome su izuzetno visoke koncentracije Pb, Zn, Cu, As i Cd (Slike 3-6) i Fe u A-horizontu, OB-overbank sedimentu i S-strim sedimentu a koji se nalaze nizvodno od

Kosovske Mitrovice. Najveći sadržaji  $^{238}\text{U}$ ,  $^{232}\text{Th}$ ,  $^{40}\text{K}$  i  $^{226}\text{Ra}$  nalaze se u strim sedimentu na lokaciji 5 nizvodno od Kosovske Mitrovice (Tabela 3).

**Tabela 3.** Uticaj prirodnih radionuklida  $^{238}\text{U}$ ,  $^{232}\text{Th}$ ,  $^{40}\text{K}$ ,  $^{226}\text{Ra}$  u obalskim profilima od izvorišnog dela reke Ibar (lokacija 6) od ušća u Zapadnu Moravu (lokacija 1)

Reka Ibar		$^{238}\text{U}$ , ppm	$^{232}\text{Th}$ , ppm	$^{40}\text{K}$ , %	$^{226}\text{Ra}$ , ppm	Th/U
Lokacija 1	A	2.68	6.65	1.25	0.000090	2.48
	OB	2.09	8.32	1.42	0.000071	3.98
	S	2.45	7.89	1.53	0.000083	3.22
Lokacija 2	A	0.43	0.89	0.13	0.000015	2.05
	OB	1.89	7.60	1.15	0.000064	4.03
	S	2.48	7.43	1.23	0.000084	3.00
Lokacija 3	A	2.28	7.75	1.50	0.000077	3.40
	OB	2.10	8.34	1.47	0.000071	3.97
	S	2.16	6.14	1.18	0.000073	2.84
Lokacija 4	A	1.70	6.31	1.33	0.0000574	3.71
	OB	1.53	5.09	1.24	0.0000516	3.33
	S	2.26	6.54	1.39	0.0000763	2.89
Lokacija 5	A	2.15	3.65	1.08	0.0000726	1.70
	OB	2.61	2.95	0.70	0.0000881	1.13
	OB	1.52	3.58	0.68	0.0000513	2.36
	S	6.27	18.30	2.70	0.0002117	2.92
Lokacija 6	A	1.14	5.51	1.36	0.0000476	3.91
	OB	1.31	5.32	1.19	0.0000442	4.06
	S	1.13	3.53	1.26	0.0000381	3.12

Poreklo anomalnih koncentracija  $^{238}\text{U}$ ,  $^{232}\text{Th}$ ,  $^{40}\text{K}$ ,  $^{226}\text{Ra}$  može se povezati sa fluvijalnim transportom radioaktivnih elemenata sa područja Kosova rekom Sitnicom, koja se uliva u reku Ibar uzvodno od lokacije 5 (videti sliku 1). Prisustvo rudnika olova i cinka u neposrednoj blizini (uzvodno od lokacije 5) zahteva detaljnija istraživanja, ali u regionalnom sagledavanju ekološkog statusa regiona evidentna je i značajna analiza rezultata sadržaja hemijskih elemenata u obalskim profilima. Metodologija uzorkovanja obezbeđuje reprezentativne podatke u regionalnom smislu i značajna je u izdvajanju geopatogenih zona uticaja prirodnih radionuklida [15] i drugih toksičnih elemenata.

## ZAKLJUČAK

Geohemijsko kartiranje obalskih profila koga čine: A-horizont, OB-overbank sediment i S-strim sediment, od značaja je za

pravilnu determinaciju oreola rasejavanja, formiranih u zavisnosti od geološkog sastava ili antropogenog uticaja. Primjenjena metodologija uzorkovanja obalskih profila i analitičke metode su od posebnog značaja u istraživanju mineralnih sirovina i izradi regionalnih, poludetaljnih i detaljnih geochemijskih karata. Korelacija sadržaja hemijskih elemenata u matičnim stenama i antropogeni uticaj definisan u obalskom profilu definišu stanje u životnoj sredini. Izradom geochemijskih karata u različitim sredinama geofsere, formira se osnova za praćenje definisanja stanja životne sredine u preindustrijskom i postindustrijskom periodu i uspostavljanje monitoringa. Rezultati istraživanja su višenamenskog karaktera, naročito za evidentiranje područja biogeohemijske endemije, izrade geomedicinskih karata, istraživanje mineralnih sirovina i druga studijska multidisciplinarna istraživanja.

## LITERATURA

- [1] R. T. Ottesen, J. Bogen, B. Bølviken, T. Volden, Overbank Sediment: A Representative Sample Medium for Regional Geochemical Mapping, *Journal of Geochemical Exploration*, 32 (1989), 257-277.
- [2] M. G. Macklin, Metal Contamination of Soils and Sediments: A Geographical Perspective. In: Newson, M. D. (Ed.), *Managing the Human Impact on the Natural Environment: Patterns and Processes*, London, Belhaven Press, 1992, 172-195.
- [3] M. G. Macklin, J. Ridgway, D. G. Passmore, B. T. Rumsby, The use of Overbank Sediment for Geochemical Mapping and Contamination Assessment: Results from Selected English and Welsh Floodplains, *Applied Geochemistry* 9 (1994), 689-700.
- [4] B. Bølviken, J. Bogen, A. Demetriadis, W. De Vos, J. Ebbing, R. Hindel, R.T. Ottesen, R. Salminen, O. Schermann, R. Swennen, Final Report of the Working Group on Regional Geochemical Mapping 1986-1993. Forum of European Geological Surveys (foregs), *Geological Survey of Norway Open File Report*, 1993, No. 93-092.
- [5] V. Gordanić, D. Milovanović, M. Vidović, S. Rogan, I. Trajković, Geochemical map of Eastern Serbia in 1:1000000 and Application in Defining the Ecological Status of Selected Areas, Proceedings of the 17<sup>th</sup> meeting of the Association of European Geological Societies – MAEGS 17, Serbian Geological Society, Belgrade, Serbia, 2011, 187-191.
- [6] V. Gordanić, A. Ćirić, D. Jovanović, The use Overbank Sediments data for Geochemical Mapping and Contamination Assessment: Results from Selected Floodplains of Serbia, Goldschmidt Conference Abstracts „Goldschmidt 2007“, Cologne, Germany, *Geochimica et Cosmochimica Acta*, 71 (2007), 15, 1, A346.
- [7] V. Gordanić, A. Ćirić, D. Jovanović, Regional Geochemical Mapping – Ecological Significance, Goldschmidt Conference Abstracts „Goldschmidt 2008“, Vancouver, Canada, *Geochimica et Cosmochimica Acta*, 72 (2008), 12, A321.
- [8] V. Gordanić, V. Spasić-Jokić, Geochemical Indicators in Identification of Geopathogenic Zones of Natural Radioactivity. MD - Medical Data, 5 (2013), 2, 121-124.
- [9] R. L. Folk, The Distinction Between Grain Size and Mineral Composition in Sedimentary Rock Nomenclature. *Journal of Geology* 62 (1954), 4, 344-359.
- [10] J. Green, Geochemical Table of the Elements for 1959, *Geological Society of America Bulletin* 70 (1959), 1127-1184.
- [11] M. Fleischer, The Abundance and Distribution of the Chemical Elements in the Earth's Crust, *Journal of Chemical Education*, 31 (1954), 9, 446-455.
- [12] A. P. Vinogradov, Regularity of Distribution of Chemical Elements in the Earth's Crust, *Geochemistry*, 1 (1956), 1-43.
- [13] R. Marković, J. Stevanović, M. Gvozdenović, J. M. Jakšić, Treatment of Waste Sulfuric Acid Copper Electrolyte, *Mining and Metallurgy Engineering Bor*, 3 (2014), 141-152.
- [14] L. Zupunski, V. Spasic-Jokic, V. Gordanic, Chapter IX: Low Dose Exposure to Radionuclides in Soil, In: Gerada, J. G. (Ed.), *Radionuclides: Sources, Properties and Hazards*, New York, Nova Science Publishers, Inc., 2012, 151-170.
- [15] V. Spasic-Jokic, Lj. Zupunski, Z. Mitrovic, B. Vujicic, I. Zupunski, Lj. Jankovic-Mandic, V. Gordanic, Environmental Risk of Natural Radiation Sources, 2011 IEEE International Workshop on Medical Measurements and Applications Proceedings (MeMeA), Bari, Italija, 2011, 638-641.

Biserka Trumić\*, Aleksandra Ivanović\*, Vojka Gardić\*

## SEGREGATION OF IMPURITIES IN PLATINUM AND PLATINUM-BASED ALLOYS\*\*

### Abstract

This work presents the research results of formation the equilibrium and non-equilibrium segregations of impurities both in pure platinum and platinum alloys. It is shown that segregations strengthen in the case when impurities, absorbed on the surface of crystals, have the same sign or similar values of range deviations regarding to the pure platinum. Equilibrium of segregations occurs as the diffusion result of impurities to the grain boundaries with creation of concentration gradient.

Non-equilibrium segregation of impurities occupies the area size of ten micrometers and is generated in the process of metal crystallization or in solid solution as the result of interaction the impurities with vacancies with formation a pair of vacancy-interstitial atom.

Segregation of impurities in the platinum alloys is conditioned by the nature of impurities, their concentration, distribution in the volume of metal, interaction with the basic and alloying components as well as the temperature - time factor.

The groups of impurities were observed in the form of foreign inclusions along with the equilibrium and non-equilibrium segregation of impurities in the platinum alloys.

**Keywords:** impurities, equilibrium and non-equilibrium segregation, platinum, platinum alloys

## INTRODUCTION

The presence of chemical elements - impurities in the platinum metals and alloys is related to the composition of the starting mineral raw materials as well as the technological processes for their preparation, processing and exploitation in the industrial conditions [1-3].

The presence of impurities in the platinum metals and alloys has a major impact on their physical and mechanical properties. Due to this reason, the purity of platinum metals and alloys is one of their key characteristics [4-6].

Depending on the content and distribution of impurities in metal, their interaction also changes. With increasing the content of

impurities, a probability of brittle fracture of metals during heating increases. However, technological and exploitation properties of platinum metals and alloys can be significantly modified in the presence of very small amounts of impurities (within hundredths and thousandths of percent). The risk of brittle fracture is so much higher if the increase of content of impurities does not occur in the entire volume of metal, but only in some of its parts [7,8].

Local concentration of impurities in the inter-crystal zone or boundaries within the crystal can be several times higher than the average concentrations in a volume of metal. Such local accumulation of impurities in

\* Mining and Metallurgy Institute Bor, Zeleni bulevar 33, Bor, Serbia

\*\* This work is the results of the Project TR 34029 "Development the Technologies for Production the Pd Catalyst – Catcher for Reduction the Losses of Platinum in High Temperature Catalysis Processes", funded by the Ministry of Education, Science and Technological Development of the Republic of Serbia, in the period from 2011 to 2015.

the metal can be the result of equilibrium or non-equilibrium segregation, as well as the presence of foreign inclusions [9].

Equilibrium segregation of impurities as a rule occupies the area of one to ten nanometers, although in most cases the enrichment of impurities is limited by a monolayer segregation of atoms equal to or slightly greater than the inter-granular zone width 2-3 atomic layers [10]. Equilibrium segregation occurs as a result of diffusion of impurities to the grain boundaries with formation of a concentration gradient.

Non-equilibrium segregation of impurities takes, as a rule, the area of ten microme-

ters and is generated in the process of metal crystallization or in solid solution as a result of the interaction the impurities with vacancies with formation the pair of vacancy-interstitial atom.

## EXPERIMENTAL TECHNIQUE

Platinum, rhodium and palladium for production the alloys are obtained as a by-product within the production of electrolytic copper of RTB, Serbia. The required purity is achieved by the additional refining. Composition of tested alloys is listed in Table 1.

**Table 1** Content of alloying elements in tested samples (mass %)

Alloy	Rh (mass%)	Pd (mass%)	Ir (mass%)	Au (mass%)
PtRh7	7	-	-	-
PtRh25	25	-	-	-
PtIr4	-	-	4	-
PtRh20Pd10Ir0,1Au0,1	20	10	0.1	0.1

Melting of samples was carried out in the medium-frequency induction furnace. Annealing of samples was carried out in the electric furnace type LP08.

To test the mechanical properties of samples at high temperatures, a universal apparatus for tension testing of materials at high temperature, manufacturer Karl Frank, type 81221.

Chemical analysis of the materials for samples was performed in the atomic absorption spectrophotometer.

## RESULTS AND DISCUSSION

Equilibrium segregation of impurities increases linearly with increasing time and temperature warming, with great absorption thereof. The most common is for systems with low solubility of impurities in the crystal lattice of metal-base, as well as in large differences in atomic diameters of impurities and base. In literature is known a dependence of inter-granular zone enriched with

impurities from the solubility limit thereof in solid solution. For many studied phase systems, based on Fe, Ni and Cu, the enriched space with impurities is as large as limit of their solubility is lower. With decrease of solubility limit of the impurities to  $1 \times 10^{-3}$  % (at.), their concentration in the inter-crystal zone of metal-base may reach 10% (at.), i.e. it can be 10,000 times higher than the volume of alloys [11-15].

Based on the results of solubility of impurities in platinum, it can be assumed that practically insoluble or slightly soluble impurities like Ba, P, As, Si, Bi and Pb show a high tendency to the formation of equilibrium segregations, while, for example, Fe, Ni, Cu, Ag, Mg Zn, Al, and Sb form with platinum a steady stream of solid solutions.

Equilibrium segregation of impurities leads to decrease in strain energy of the crystal lattice in the zone of their existence, while reducing the Gibbs energy of inter-granular limits [16-22].

The impurities that accumulate at the grain boundaries can react with each other and lead to an increase or decrease in segregation of this or any other element. In the first case, with the same sign of the atomic range of disagreement between the two particles in relation to the metal – base, the inter-crystalline zone will be more enriched with atoms of impurity atoms that has a larger range of disagreement. In the latter case, at different sign of atomic disagreement and equal concentrations of two impurities there is formation of complex atoms of these impurities and equilibrium segregation is weak.

Segregation is stronger in the case that impurities that are adsorbed on the surface

of crystals have the same sign and similar values of the range of discrepancies.

In this way, it can be expected that in cases where the removal of impurities from the alloy is very difficult, their harmful effect can be minimized by introduction less harmful impurity or impurities with the opposite sign of the discrepancy range.

On the basis of the atomic diameter of platinum that is 0.139 nm, it is possible to form a range of deviations of the atomic diameters of impurities.

Size range of deviations ( $\Delta r$ ) of the atomic diameters of platinum and impurities, in the case where diameter of platinum is higher (+  $\Delta r$ ) or less (- $\Delta r$ ) in relation to the diameters of impurities, is given in Table 2.

**Table 2** Size range of deviations ( $\Delta r$ ) for impurities

Element	$\Delta r, \text{nm}$	Element	$\Delta r, \text{nm}$
Zn	+0.006	As	+0.014
Si	-0.021	Sn	-0.012
P	-0.021	Mg	-0.021
Cu	+0.011	Zr	-0.020
Fe	+0.015	Sb	+0.012
Cr	+0.014	Pb	-0.036
Co	+0.014	Y	-0.039
Ni	+0.014	Bi	-0.016
Al	-0.004	Ca	-0.058
Ag	-0.005	Ba	-0.078
Ti	-0.007	K	-0.088

On the basis of the values shown in Table 1, it can be concluded that Zr decreases the equilibrium segregation and negative impact of impurities, such as Si and P in tested platinum alloys. Bismuth can somewhat neutralize the negative impact and accumulation of impurities such as Fe, Cu, Cr, Co, As and Ni.

Also, the presence of Ca, Ba and K in platinum alloys can be neutralized with different impurities with the sign of deviation range, such as Zn, Cu, As, Cr, Co, Ni, Mg.

The most severe is the form of presence the impurities with the approximate values

of deviation range, and of the same sign, for example, Al and Ag, as one pair and Sb and Zn as the second pair. In these cases, the probability of equilibrium segregation of each pair of impurities increases as well as their negative impact on the technological and exploitation properties of platinum alloys.

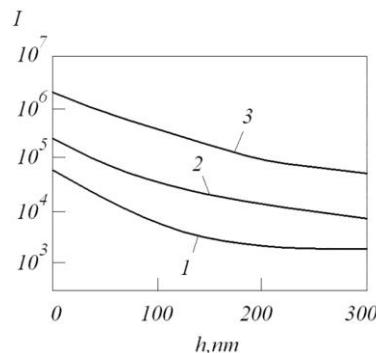
However, in practical terms, it is difficult to predict and even harder to manage the equilibrium segregation of impurities in platinum alloys.

In real terms of formation the equilibrium segregation, ten of impurities can take

part, and that process may depend heavily on their mutual effects, the effect with the metal - base and alloying element with simultaneous temperature dependence - the time factor

The question of formation the non-equilibrium segregations of impurities in solid solution with formation the pair of vacancy - interstitial atom is not sufficiently clarified. It is believed that during cooling the heated metal in the crystal lattice, a large number of vacancies occurs which diffuse to the grain boundaries in a pair with atom

impurities. At the grain boundary, the pair of vacancy - interstitial atoms bump into each other to form an accumulation of atom impurities. At slower cooling of heated metal, the probability of development is more likely for the process and the area of non-equilibrium segregation of impurities becomes significant. If the higher the temperature of metal during cooling, the more significant is formation the pair of vacancy - interstitial atom, which segregate to the grain boundaries, increasing the non-equilibrium segregation of impurities, as shown in Figure 1.



**Figure 1** Profile of Al distribution along the thickness of sample composition PtRh20Pd10Ir0,1Au0,1 in non-annealed condition (1), after annealing in the air at 1,400°C, 50 h, away from the border (2) and at the grain boundaries (3) ( $j = 100 \mu\text{A}/\text{cm}^2$ ,  $P_{\text{O}_2} = 10^{-3} \text{ Pa}$ , I-size of the output secondary ions)

Segregation of aluminum was observed during the study of secondary ions on microanalyzer, the investigated alloys using mass spectrometric method (concentration of impurities was  $10^{-3}$  to  $10^{-5}\%$ ). Based on the value of output of secondary ions (I), it can be concluded that with distance from the sample surface of non-annealed alloy, the Al concentration decreases. After annealing the platinum alloy at 1,400°C for 50 h in the air, the concentration of Al in the surface layers of sample, in the grain boundaries, is twice as higher than that of the grain.

Comparatively with equilibrium and non-equilibrium segregation of impurities in the platinum alloys, the groups of impurities were observed in the form of foreign inclusions. In these inclusions, the impurities are, as a rule, in the form of solid compounds, usually in the form of oxides. Oxide parti-

cles get into the alloy, for example, in the process of melting in ceramic pots or arise in the form of silicate inclusions in the warming process. The size of these inclusions reaches a hundredth of micrometer.

Based on numerous experiments, the possibility of formation of these inclusions was confirmed in the platinum alloys. The investigation of the alloy PtRh20Pd10Ir0,1 Au0,1 by the electron probe (after creeping at 1,400°C, at load of 5 MPa) has studied the foreign inclusions arranged along grain boundaries and within grains.

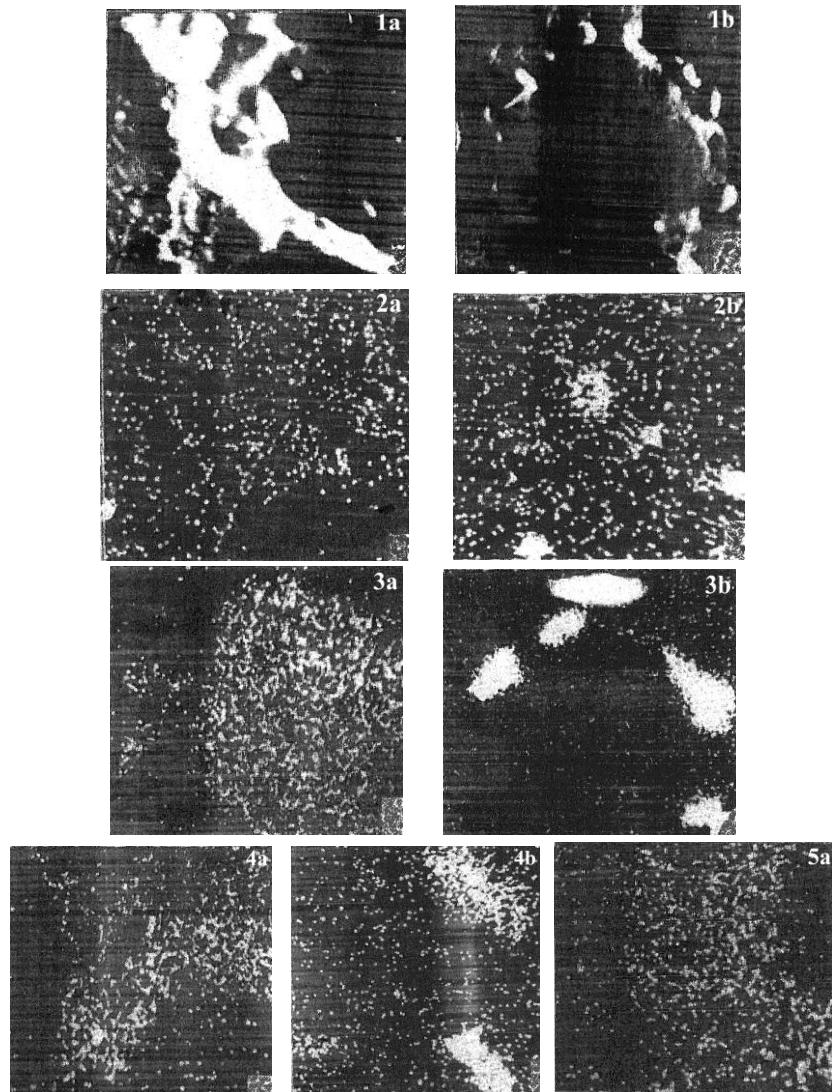
Along the grain boundaries, the inclusions reach the size of 40-50 microns and contain Si and Ti. Large inclusions of copper were discovered inside the grain. Small number of inclusions (up to 10 microns) based on Al and Si occur both in the grain boundaries and within the grains themselves.

The number of small inclusions containing Mg, Zn, Ni and Cr is negligible. The inclusions of complex composition, type of Al-Fe-Ti, Si-Cr-Sn and Pb-Sn, are also present.

Impurities such as Al, Mg, Si, and Fe, present in platinum alloys, after heating in the air ( $1400^{\circ}\text{C}$ , 50 h), are found primarily in the oxide form, while after annealing in vacuum ( $1400^{\circ}\text{C}$ , 2 h) are registered in elemental form.

By investigation the alloy of composition PtRh20Pd10Ir0,1Au0,1 it was shown that foreign inclusions contain a tenth of the percentage of S, C, P and Pb and other harmful impurities [23].

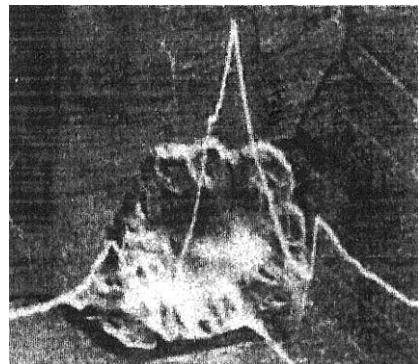
Figure 2 gives the standard view of the area of the sample composition PtRh20Pd10Ir0,1Au0,1 with inclusions of impurities both on the grain boundaries and within the grains in characteristic radiation.



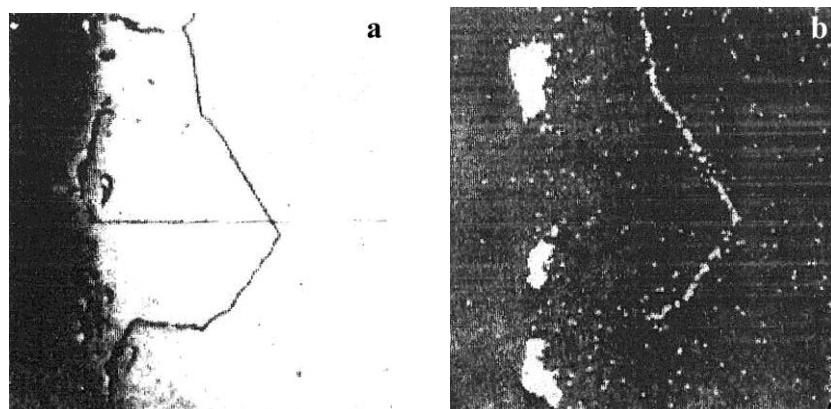
**Figure 2** Standard view the area of the sample composition PtRh20Pd10Ir0,1Au0,1 with inclusions of impurities with the secondary electrons (1a) and (1b), at the characteristic X-ray radiation FeKa (2a), AlKa (3a), BiKa (4a), SnKa (5a), SiKa (2b), TiKa (3b), CaKa (4b); Magnification: a) 800x, b) 400x

It is obvious that, in the area where the inclusions enriched with Fe, Al, Si, Ca, Ti, Bi and Pb are present, the local concentration of impurities ranges from 5-40%.

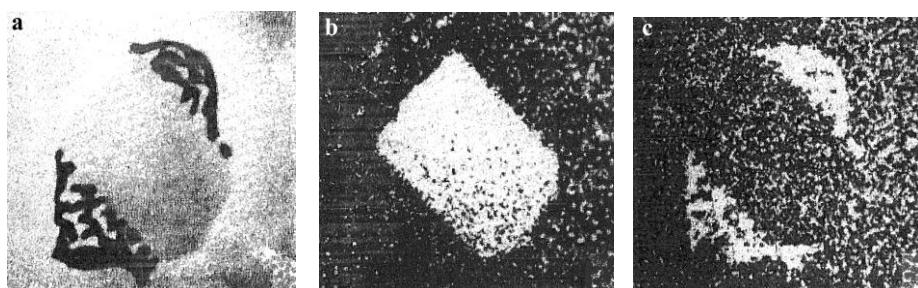
Also, it is noticed the probability of presence in different ways resulting inclusions enriched with Si, Ca, Al, Ag, As and Pb (Figures 3-6).



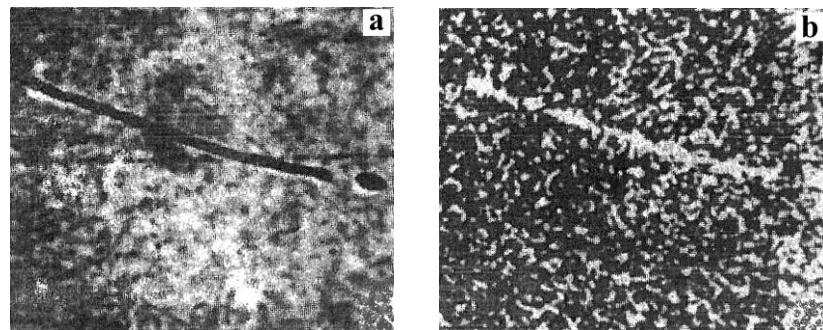
**Figure 3** Standard view the area of the sample composition with PtRh7 inclusions and line distribution of Si in it at K<sub>α</sub> radiation



**Figure 4** Area of destruction the sample PtRh25 with inclusions, with content of Ag with the secondary electrons (a) and in X-ray separation of AgK<sub>α</sub> (b) (Magnification 360x)



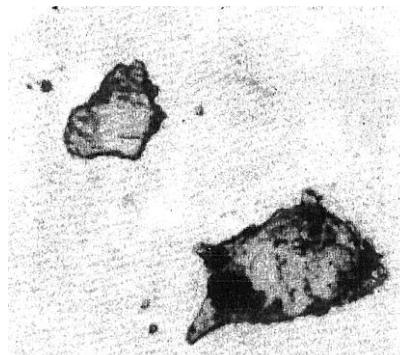
**Figure 5** View a part of platinum sample with the inclusion of secondary electrons (a) and in the X-ray PbK<sub>α</sub> separation (b) and AsK<sub>α</sub> (c), (Magnification 720x)



**Figure 6** View a part of alloy sample PtIr4 with the inclusions containing Pb, with secondary electrons (a) and in the X-ray PbKa separation (b) (magnification 850x)

In most cases, the foreign inclusions in the platinum alloy can be seen under the

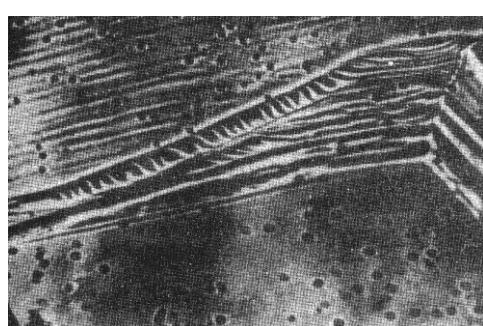
normal light microscope, as shown in Figure 7.



**Figure 7** Inclusion in the alloy PtRh20Pd10Ir0,1Au0,1 seen under the light microscope

In investigation the microstructure of pure platinum after creeping at 1350°C, at stress of 13 MPa for 10 min as shown

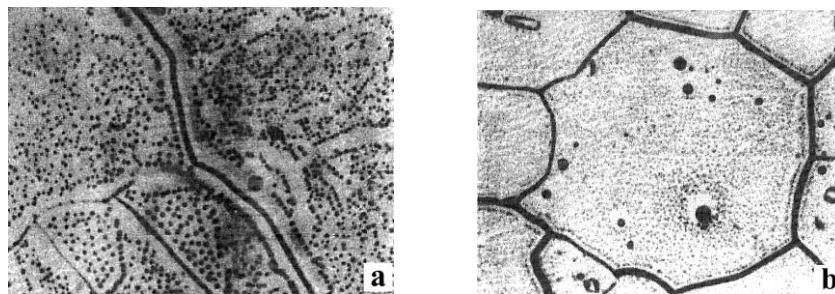
in Figure 8, the characteristic glassy separations could be observed.



**Figure 8** Microstructure of pure platinum after creeping at 1350°C, at stress of 13 MPa for 10 min (magnification 300x)

Similar separations were the subject of research the alloy PtIr4, where it was observed that at temperature higher than 1300°C, the sample surface is

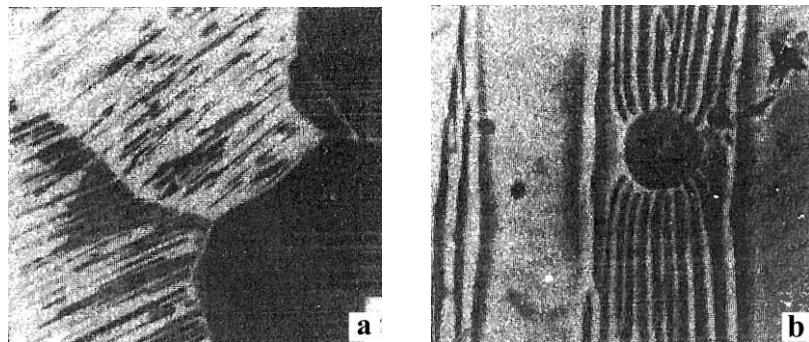
covered with many small droplets of liquid, which gradually pour forming a large transparent drops, as shown in Figure 9.



**Figure 9** Surface of the alloy PtIr4 with formation of silicate drops after annealing at 1400°C:  
a) 4 h, magnification 500x; b) 300 h, magnification 100x

The limits and sub-limits occur at the same time as the zone of separation and further removal of liquid. The separated

liquid makes it difficult sliding over the plane (111) within the grain, as shown in Figure 10.



**Figure 10** Lines of sliding within the grain formed on platinum surface at heating in the air:  
a) up to 1300°C, magnification 200x; b) over 1300°C, magnification 500x

If the rate of metal heating up to 1300°C is rather large, making slipping lines is unlikely. Only in the exceptional uncontrolled cases on the surface of platinum, a small amount of slipping lines of liquid phase, as shown in Figure 10 b, can be observed inside the grain at the same time.

The absence of slipping lines in the presence of liquids (droplets) on the metal surface is associated with it, that all drops are

united in a thin film of liquid which prevents the formation of a layer of adsorbed oxygen, and thus the creation of slip lines. Hardened drops of liquid did not react with hydrochloric or nitric acid, but they are excellent diluted in fluorohydrochloric acid. Microanalysis of hardened drops showed the presence of 8% Si; 10% Al; 10% Ca; 0.1% Ni; 0.1% Fe; 0.1% Mn, and 0.1% Mg. In addition to these elements, Pb and Na were present.

Spectral analysis showed that platinum heating for a period of 800 h results into a gradual reduction of content of impurities such as Si, Fe, Ni, Ca and Mg. Formation of liquid silicate phase is associated with reduction in creeping resistance of platinum and its alloys at content of some of these impurities, as the intermediate layer of molten silicates on the planes grain boundaries probably accelerates sliding.

## CONCLUSION

Based on the previous results of research, it can be concluded the following:

In real conditions of formation the equilibrium segregation, ten of impurities can take part and the process is very depend on their mutual effects, the effect with the metal - base and alloying elements with simultaneous dependence temperature - time factor.

If the higher metal temperature in cooling, therefore, the creation of a pair vacancy-interstitial atom is much more important that diffuses to the grain boundaries, increasing the non-equilibrium segregation of impurities.

Along with the equilibrium and non-equilibrium segregation of impurities in the platinum alloys, the groups of impurities were observed in the form of foreign inclusions. In these inclusions, the impurities are in the form of solid compounds, usually in oxide form. Oxide particles enter the alloy in the melting process in ceramic pots or arise in the form of silicate inclusions in the heating process. The size of these inclusions reaches a hundredth part of a micrometer.

The impurities such as Al, Mg, Si, and Fe, present in the platinum alloys, after heating in the air (1400°C, 50 h), are in the oxide form, whereas after annealing in vacuum (1400°C, 2 h) are registered in the elemental form.

The investigation the alloy of composition PtRh20Pd10Ir0,1Au0,1 has shown that foreign inclusions contain a tenth of the percentage of S, C, P and Pb, and other harmful impurities.

Segregation of impurities in the platinum alloys is conditioned by the nature of impurities, their concentration, distribution in the volume of metal, interaction with the basic and alloying components as well as the temperature - time factor. It is possible to expect that as the result of interaction of harmful impurities with the platinum metals that enter the composition of the alloy, the reductions of a high-temperature resistance of the alloy and increase the possibility of brittle fracture at high temperatures are formed.

## REFERENCES

- [1] H. Gavin, Platinum Met. Rev. 54 (2010) 166.
- [2] E. Preston, Platinum Met. Rev. 4 (1960) 48.
- [3] D. F. Lupton, J. Merker, B. Fischer, R. Völk, 24<sup>th</sup> International Precious Metals Conference, Williamsburg, Virginia, USA, 1–14 June 2000.
- [4] Y. Ning, Z. Yang, H. Zhao, Platinum Met. Rev. 4 (1996) 80.
- [5] N. Yuantao, Y. Zhengfen, Platinum Met. Rev. 43 (1999) 62.
- [6] B. Trumić, D. Stanković, V. Trujić, J. Min. Metall., Sect. B 45 (1) B (2009) 79 – 87.
- [7] B. Wu, G. Liu, , Platinum Met. Rev. 41 (1997) 81.
- [8] M. Funabikia, T. Yamadaa, K. Kayanoa, Catal. Today 10 (1991) 33.
- [9] T. Biggs, S.S. Taylor, E. Van der Lin-gen, Platinum Met. Rev. 49 (2005) 2.
- [10] John C. Wright, Platinum Metals Rev., 2002, 46 (2), 66.
- [11] T. Biggs, M. B. Cortie, M. J. Witcomb, L. A. Cornish, Platinum Metals Rev., 2003, 47, (4), 142.
- [12] T. Biggs, M.J. Witcomb, L.A. Cornish, Materials Science and Engineering A273–275 (1999) 204.
- [13] F. Xiao, F. Zhao, D. Mei, Z. Mo, B. Zeng, Biosens. Bioelectron. 24 (2009) 3481.

- [14] K. T. Jacob, S. Priya, and Y. Waseda, Metall. Mater. Trans. A 29A (1998) 1545.
- [15] G. Dereli, T. Cagin, M. Uludogan, M. Tomak, Philos. Mag. Lett. 75 (4) (1997) 209.
- [16] P. Battaini, Platinum Met. Rev. 55 (2011) 74.
- [17] J. Luyten, J. De Keyzer, P. Wollants, C. Creemers, Calphad 33 (2009) 370.
- [18] B. Trumic, L. Gomidželović, S. Marjanović, V. Krstić, A. Ivanović, S. Dimitrijević, Pt - Materials Testing, 55 (2013) 38.
- [19] Ритвин, Е. И., Медовој, Л.А.: Влијание физико-химическој следи на жаропрочност мераллических материјала, Москва, Наука, 1974
- [20] Савицкиј, Е. М., Полјакова В. П., Горина, Н. Б., Рошан, Н. Р.: Металоведение платиновых металлов, Москва, Металургија, 1975.
- [21] Захаров, М. В., Захаров, А. М.: Жаропрочные сплавы, Москва, Металургија, 1983.
- [22] Ритвин, Е. И.: Жаропрочност платиновых сплавоажв, Москва, Металургија, 1987.
- [23] B. Trumić, L. Gomidželović, M. Bugarin, Mining and Metallurgy Engineering Bor, 1/2015, p. 141-148.

Biserka Trumić\*, Aleksandra Ivanović\*, Vojka Gardić\*

## SEGREGACIJA NEČISTOĆA U PLATINI I LEGURAMA NA BAZI PLATINE\*\*

### Izvod

*U radu su predstavljeni rezultati ispitivanja nastanka ravnotežnih i neravnotežnih segregacija nečistoća kako u čistoj, tako i u legurama platine. Pokazano je da segregacije jačaju u slučaju kada nečistoće, apsorbovane na površini kristala imaju isti znak ili pak slične vrednosti opsega odstupanja u odnosu na čistu platinu. Ravnotežna segregacija javlja se kao rezultat difuzije nečistoća ka granicama zrna uz stvaranje koncentracionog gradijenta.*

*Neravnotežna segregacija nečistoća zauzima oblast veličine desetak mikrometara i nastaje u procesu kristalizacije metala ili u čvrstom rastvoru kao rezultat uzajamnog dejstva nečistoća s vakancijama uz obrazovanje para vakancija-intersticijski atom.*

*Segregacija nečistoća u platinskim legurama uslovljena je prirodnom nečistoća, njihovom koncentracijom, raspodelom u zapremini metala, uzajamnim dejstvom sa osnovnim i legirnim komponentama, kao i temperaturno - vremenskim faktorom.*

*Uporedno sa ravnotežnom i neravnotežnom segregacijom nečistoća u platinskim legurama primećene su skupine nečistoća u obliku stranih uključaka.*

**Ključne reči:** nečistoća, ravnotežna i neravnotežna segregacija, platina, legure platine

## UVOD

Prisustvo hemijskih elemenata-nečistoća u platinskim metalima i legurama povezano je sa sastavom polaznih rudnih sirovina kao i sa tehnološkim operacijama njihovog dobijanja, prerade i eksploatacije u industrijskim uslovima [1-3].

Prisustvo nečistoća u platinskim metalima i legurama ima veliki uticaj na njihova fizička i mehanička svojstva. Iz tog razloga, čistoća platinskih metala i legura jedna je od njihovih ključnih karakteristika [4-6].

U zavisnosti od sadržaja i rasporeda nečistoća u metalu menja se i njihovo međusobno dejstvo. Sa povećanjem sadržaja nečistoća verovatnoća krtog preloma metala

pri zagrevanju raste. Međutim, tehnološka i eksploataciona svojstva platinskih metala i legura mogu se bitno izmeniti u prisustvu veoma malih količina nečistoća (u granicama stotih i hiljaditih delova procenata). Opasnost od krtog preloma je utoliko veća, ukoliko do povećanja sadržaja nečistoća ne dolazi u celoj zapremini metala, već samo u pojedinim njegovim delovima [7,8].

Lokalna koncentracija nečistoća u međukristalnoj zoni ili granicama unutar kristala može biti i nekoliko puta viša od srednje koncentracije u zapremini metala. Takvo lokalno nagomilavanje nečistoća u metalu može biti rezultat ravnotežne ili

\* Institut za rudarstvo i metalurgiju Bor, Zeleni bulevar 33, Bor, Srbija

\*\* Ovaj rad je nastao kao rezultat projekta TR 34029 , "Razvoj tehnologije proizvodnje Pd katalizatora-hvatača za smanjenje gubitaka platine u visoko temperaturnim procesima katalize", finansiran od strane Ministarstva prosvete, nauke i tehnološkog razvoja Republike Srbije, u periodu 2011.-2015.

neravnotežne segregacije, kao i prisustva stranih uključaka [9].

Ravnotežna segregacija nečistoća zauzima po pravilu područje od jednog do desetak nanometara, premda u većini slučajeva obogaćenje nečistoćama ograničeno je monoslojnom segregacijom atoma jednakom ili neznatno većom od međukristalne zone širine 2–3 atomska sloja [10]. Ravnotežna segregacija javlja se kao rezultat difuzije nečistoća ka granicama zrna uz stvaranje koncentracionog gradijenta.

Neravnotežna segregacija nečistoća zauzima, po pravilu, oblast veličine desetak

mikrometara i nastaje u procesu kristalizacije metala ili u čvrstom rastvoru kao rezultat uzajamnog dejstva nečistoća s vakancijama uz obrazovanje para vakancija-intersticijski atom.

## EKSPERIMENTALNA TEHNIKA

Platina, rodijum i paladijum za izradu legura su dobijeni kao sporedan proizvod u okviru proizvodnje elektrolitičkog bakra RTB, Srbija. Dodatnom rafinacijom postignuta je neophodna čistoća. Sastav ispitivanih legura je naveden u tabeli 1.

**Tabela 1.** Sadržaj legirnih elemenata u ispitivanim uzorcima (maseni %)

Legura	Rh (mas.%)	Pd (mas.%)	Ir (mas.%)	Au (mas.%)
PtRh7	7	-	-	-
PtRh25	25	-	-	-
PtIr4	-	-	4	-
PtRh20Pd10Ir0,1Au0,1	20	10	0,1	0,1

Topljenje uzorka vršeno je u srednjefrekventnoj indukcionoj peći. Žarenje uzorka vršeno je u elektrotopornoj peći tipa LP08.

Za ispitivanje mehaničkih karakteristika uzorka na visokim temperaturama korišćen je univerzalni aparat za ispitivanje materijala zatezanjem na viskoim temperaturama, proizvođača Karl Frank, tip 81221.

Hemijska analiza materijala za uzorke izvršena je na atomskom apsorpcionom spektrofotometru.

## REZULTATI I DISKUSIJA

Ravnotežna segregacija nečistoća linearno raste sa povećanjem vremena i temperatupe zagrevanja, uz veliku apsorbenciju istih. Najzastupljenija je kod sistema s malom rastvorljivošću nečistoća u kristalnoj rešetki metala-osnove, kao i pri velikim razlikama u atomskim prečnicima nečistoća i osnove. U literaturi poznata je zavisnost veličine međukristalne zone obogaćene nečistoćama od granice rastvorljivosti istih u čvrstom

rastvoru. Za mnoge proučavane fazne sisteme na bazi Fe, Ni i Cu prostor obogaćen nečistoćama je utoliko veći, ukoliko je manja granica njihove rastvorljivosti. Sa smanjenjem granice rastvorljivosti nečistoća do  $1 \times 10^{-3}$  % (at.), njihova koncentracija u međukristalnoj zoni metala-osnove može dostići 10% (at.), tj. može 10.000 puta biti veća u odnosu na zapreminu legure [11-15].

Na osnovu rezultata rastvorljivosti nečistoća u platini, može se prepostaviti da praktično nerastvorne ili malo rastvorne nečistoće poput Ba, P, As, Si, Bi i Pb pokazuju veliku sklonost ka obrazovanju ravnotežnih segregacija, dok na primer Fe, Ni, Cu, Ag, Mg, Zn, Al i Sb obrazuju s platinom neprekidan niz čvrstih rastvora.

Ravnotežna segregacija nečistoća dovodi do smanjenja energije deformacije kristalne rešetke u zoni njihovog postojanja, uz istovremeno smanjenje Gibsove energije međuzrnnih granica [16-22].

Nečistoće koje se nagomilavaju na granicama zrna mogu međusobno reagovati i dovesti do porasta ili smanjenja segregacije

tog ili nekog drugog elementa. U prvom slučaju, pri istom znaku atomskog opsega neslaganja dvaju primesa u odnosu na metal - osnovu, međukristalna zona biće obogaćenija atomima one nečistoće koja ima veći opseg neslaganja. U drugom slučaju, pri različitom znaku atomskog neslaganja i jednakim koncentracijama dvaju primesa dolazi do obrazovanja kompleksnih atoma tih nečistoća i ravnotežna segregacija slabih.

Segregacija jača u slučaju kada nečistoće koje se apsorbuju na površini kristala imaju isti znak i slične vrednosti opsega odstupanja.

**Tabela 2.** Veličina opsega odstupanja ( $\Delta r$ ) za nečistoće

Element	$\Delta r, \text{nm}$	Element	$\Delta r, \text{nm}$
Zn	+0,006	As	+0,014
Si	-0,021	Sn	-0,012
P	-0,021	Mg	-0,021
Cu	+0,011	Zr	-0,020
Fe	+0,015	Sb	+0,012
Cr	+0,014	Pb	-0,036
Co	+0,014	Y	-0,039
Ni	+0,014	Bi	-0,016
Al	-0,004	Ca	-0,058
Ag	-0,005	Ba	-0,078
Ti	-0,007	K	-0,088

Na osnovu vrednosti prikazanih u tabeli 1 može se zaključiti da Zr smanjuje ravnotežnu segregaciju i negativan uticaj nečistoća, kao što su Si, i P u ispitivanim platin-skim legurama. Bismut donekle može neutralizovati negativan uticaj i nagomilavanje nečistoća poput Fe, Cu,Cr, Co, As i Ni.

Takođe, prisustvo Ca, Ba i K u platin-skim legurama može biti neutralizovano nečistoćama s različitim znakom opsega odstupanja, poput Zn, Cu, As, Cr, Co, Ni, Mg.

Najteži je oblik prisustva nečistoća s približnim vrednostima opsega odstupanja, a istog znaka, na primer Al i Ag, kao jedan par i Sb i Zn kao drugi par. U tim slučajevima, raste verovatnoća ravnotežne segregacije

Na taj način može se očekivati da u slučajevima kada je odstranjivanje štetnih primesa iz legure veoma otežano, njihov štetni uticaj može biti sведен na minimum i uvođenjem manje štetne nečistoće ili nečistoće sa suprotnim znakom opsega odstupanja.

Na osnovu atomskog prečnika platine koji iznosi 0,139 nm, moguće je formirati niz opsega odstupanja atomskih prečnika nečistoća.

Veličina opsega odstupanja ( $\Delta r$ ) atomskih prečnika platine i nečistoća, u slučaju kada je prečnik platine veći (+ $\Delta r$ ) ili manji (- $\Delta r$ ) u onosu na prečnike nečistoća dat je u tabeli 2.

svakog para nečistoća kao i njihov negativan uticaj na tehnološke i eksploatacione osobine platinских legura.

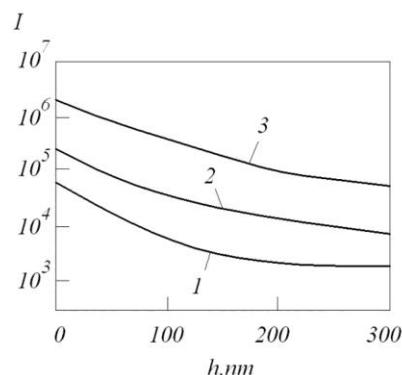
Međutim, u praktičnim uslovima teško je prognozirati a još teže upravljati procesom ravnotežne segregacije nečistoća u platin-skim legurama.

U realnim uslovima u nastajanju ravnotežne segregacije može uzeti učešće desetak nečistoća i taj proces može jako zavisiti od njihovog međusobnog dejstva, dejstva s metalom - osnovom i legirnim elementima uz istovremenu zavisnost temperaturno - vremenskog faktora.

Pitanje nastanka neravnotežnih segregacija nečistoća u čvrstom rastvoru uz

obrazovanje para vakancija - intersticijski atom nije dovoljno razjašnjeno. Smatra se da pri hlađenju zagrejanog metala u kristalnoj rešetki nastaje veliki broj vakancija koje difunduju ka granicama zrna u paru s atomom nečistoća. Na granici zrna par vakancija - intersticijski atom međusobno se sudaraju pri čemu nastaje nagomilavanja atoma nečistoća. Pri sporijem hlađenju

zagrejanog metala veća je verovatnoća odvijanja procesa i oblast neravnotežne segregacije nečistoća postaje značajna. Ukoliko je viša temperatura metala pri hlađenju, utoliko je više i značajnije stvaranje para vakancija - intersticijski atom koji difunduje ka granicama zrna, pojačavajući neravnotežnu segregaciju nečistoća, kako je prikazano na slici 1.



**Sl. 1.** Profil raspodele Al po debljini uzorka sastava PtRh20Pd10Ir0,1Au0,1 u nežarenom stanju (1), posle žarenja na vazduhu na 1.400°C, 50 h, dalje od granice (2) i na granicama zrna (3) ( $j = 100 \mu\text{A}/\text{cm}^2$ ,  $PO_2=10^{-3} \text{ Pa}$ ,  $I$  - veličina izlaznih sekundarnih jona)

Segregacija aluminijuma bila je zapažena pri istraživanju sekundarnih jona, na mikroanalizatoru, ispitivane legure metodom mase spektrometrije (koncentracija nečistoća iznosila je  $10^{-3}$  do  $10^{-5}\%$ ). Na osnovu vrednosti izlaznih sekundarnih jona ( $I$ ) može se zaključiti da sa udaljavanjem od površine uzorka neodžarene legure koncentracija Al se smanjuje. Nakon žarenja platske legure na 1.400°C u trajanju od 50 h na vazduhu, koncentracija Al u površinskim slojevima uzorka, u granicama zrna, duplo je veća u odnosu na samo zrno.

Uporedno sa ravnotežnom i neravnotežnom segregacijom nečistoća u platskim legurama primećene su skupine nečistoća u obliku stranih uključaka. U tim uključcima nečistoće se nalaze, po pravilu, u obliku čvrstih jedinjenja, najčešće u obliku oksida. Čestice oksida dospevaju u leguru, na primer, u procesu topljenja u keramičkim loncima ili nastaju u vidu silikatnih uključaka u procesu zagrevanja. Veličina tih uključaka dostiže stoti deo mikrometra.

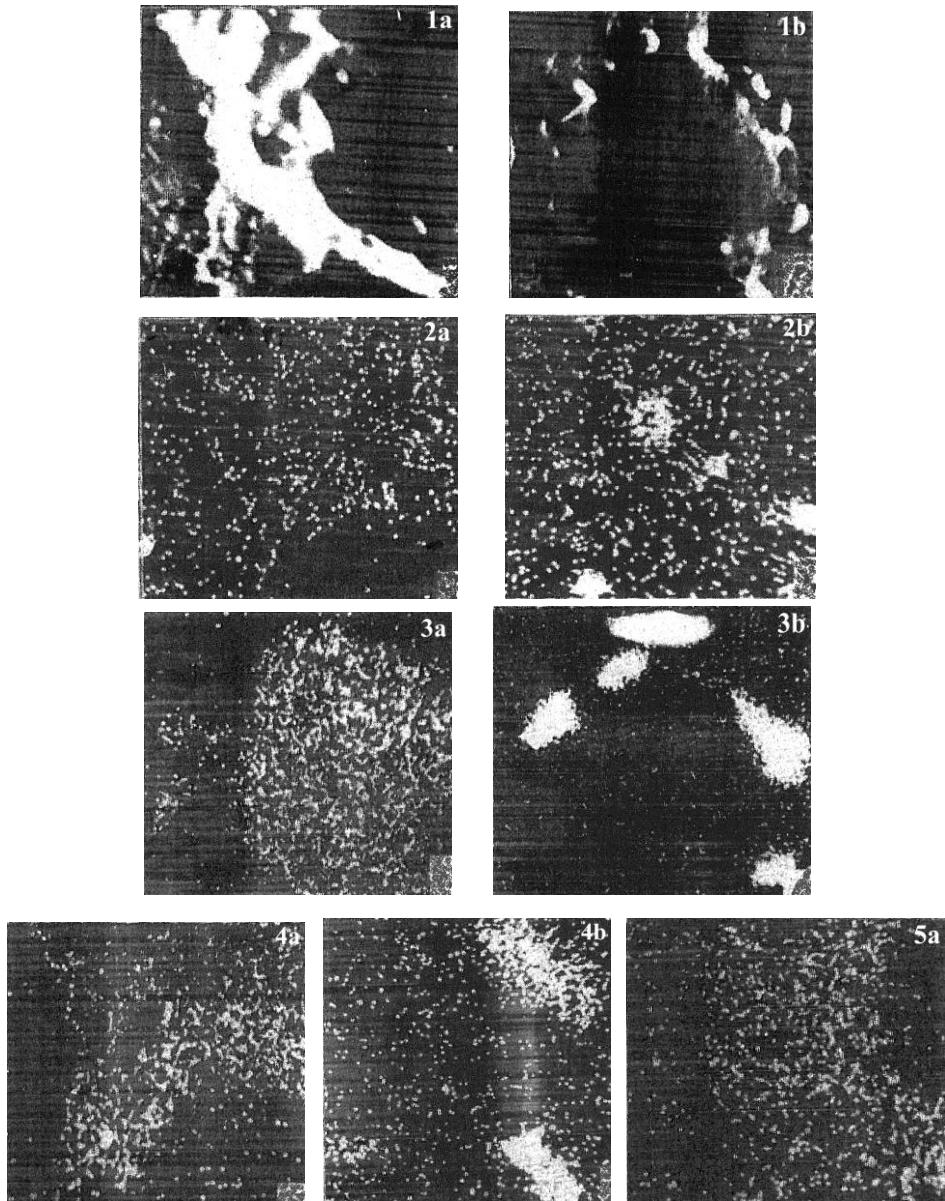
Na osnovu brojnih eksperimenata potvrđena je mogućnost obrazovanja tih uključaka u platskim legurama. Istraživanjem legure PtRh20Pd10Ir0,1Au0,1 elektronskom sondom (nakon puzanja na 1.400°C, pri opterećenju od 5 MPa) proučavani su strani uključci raspoređeni po granicama zrna i u samim zrnima.

Po granicama zrna uključci dostižu veličinu 40–50  $\mu\text{m}$  i sadrže Si i Ti. Veliki uključci bakra otkriveni su unutar zrna. Mali uključci (veličine do 10  $\mu\text{m}$ ) na bazi Al i Si javljaju se kako u granicama zrna tako i unutar samih zrna. Neznatan je broj malih uključaka koji sadrže Mg, Zn, Ni i Cr. Prisutni su takođe i uključci složenog sastava tipa Al-Fe-Ti, Si-Cr-Sn i Pb-Sn.

Nečistoće poput Al, Mg, Si i Fe, prisutne u platskim legurama, nakon zagrevanja na vazduhu (1.400°C, 50 h), nalaze se prvenstveno u oksidnom obliku, dok se nakon žarenja u vakuumu (1.400°C, 2 h) registruju u elementarnom stanju.

Ispitivanjem legure sastava PtRh20Pd10Ir0,1Au0,1 pokazano je da strani uključci sadrže deseti deo procenta S, C, P i Pb i drugih štetnih nečistoća [23].

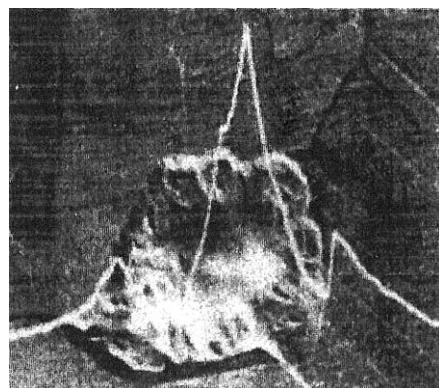
Na slici 2. dat je standardni prikaz područja uzorka sastava PtRh20Pd10Ir0,1Au0,1 sa uključcima nečistoća kako po granicama zrna, tako i unutar zrna, pri karakterističnom rentgenskom zračenju.



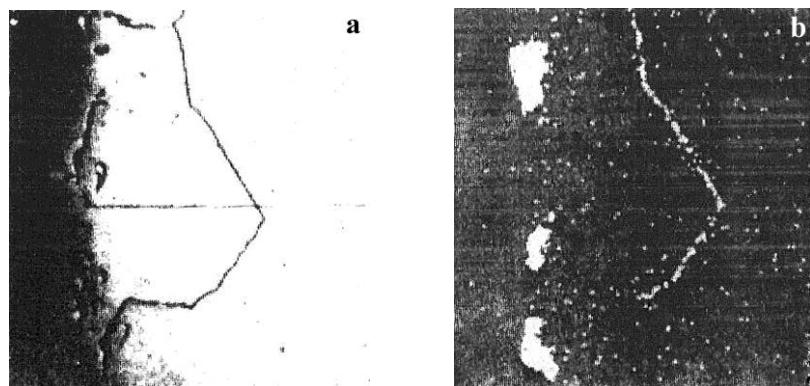
Sl. 2. Standardni prikaz područja uzorka sastava PtRh20Pd10Ir0,1Au0,1 sa uključcima nečistoća sa sekundarnim elektronima (1a) i (1b), pri karakterističnom rentgenskom zračenju FeKa(2a), AlKa(3a), BiKa(4a), SnKa(5a), SiKa(2b), TiKa(3b), CaKa(4b); Uvećanje: a) 800x, b) 400x

Očigledno je da, u području gde su prisutni uključci obogaćeni Fe, Al, Si, Ca, Ti, Bi i Pb lokalna koncentracija nečistoća kreće se od 5–40%.

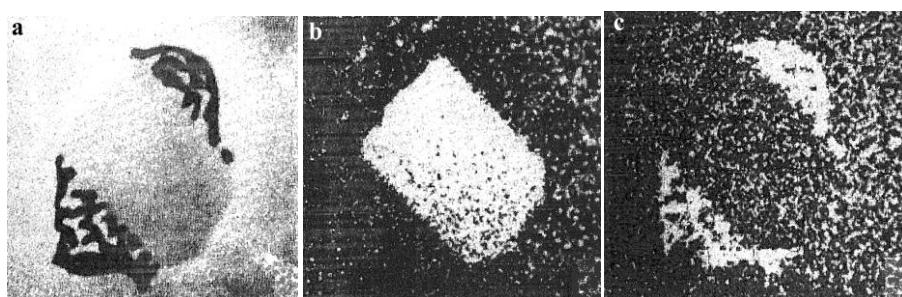
Takođe, zapažena je mogućnost prisustva, na različite načine nastale uključke obogaćene Si, Ca, Al, Ag, As i Pb. (slika 3-6 ).



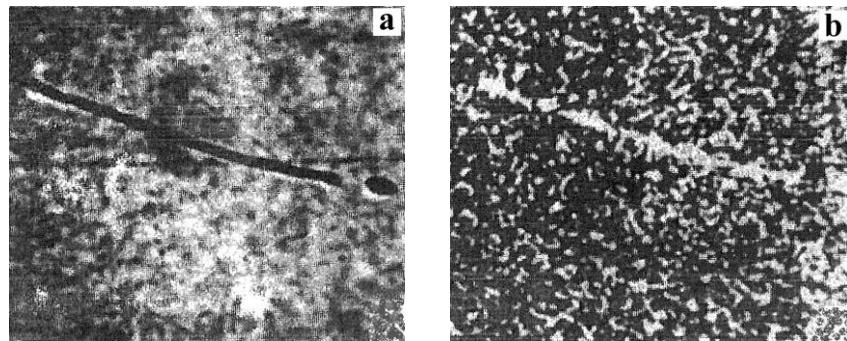
**Sl. 3.** Standardni prikaz područja uzorka sastava PtRh7 sa uključcima i linijskog rasporeda Si u njemu pri Ka zračenju



**Sl. 4.** Oblast razaranja uzorka PtRh25 s uključcima, sa sadržajem Ag sa sekundarnim elektronima (a) i pri rentgenskom izdvajaju AgKa (b) (uvećanje 360x)

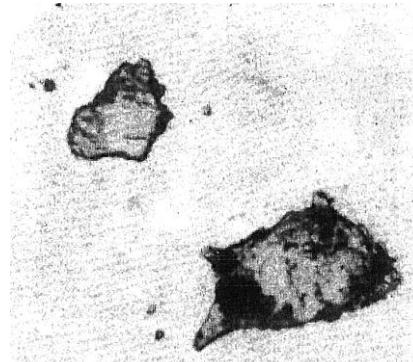


**Sl. 5.** Prikaz dela uzorka platine sa uključivanjem sekundarnih elektrona  
a) pri rentgenskom izdvajaju PbKa (b) i AsKa (c), (Uvećanje 720x)



**Sl. 6.** Prikaz dela uzorka legure PtIr4 sa uključcima koji sadrže Pb, sa sekundarnim elektronima (a) i pri rentgenskom izdvajaju PbKa (b) (uvećanje 850x)

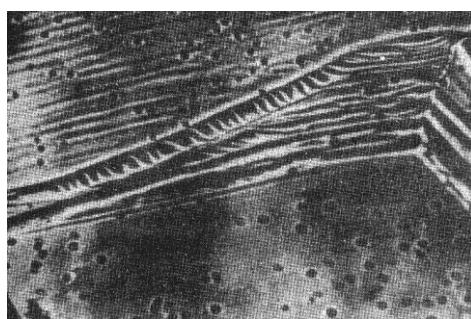
U većini slučajeva strani uključci u platinskim legurama mogu se videti pod običnim svetlosnim mikroskopom, kako je prikazano na slici 7.



**Sl. 7.** Uključak u leguri PtRh20Pd10Ir0.1Au0.1 posmatran pod svetlosnim mikroskopom

Pri ispitivanju mikrostrukture čiste platine nakon puzanja na  $1.350^{\circ}\text{C}$ , pri naprezanju od 13 MPa u trajanju od

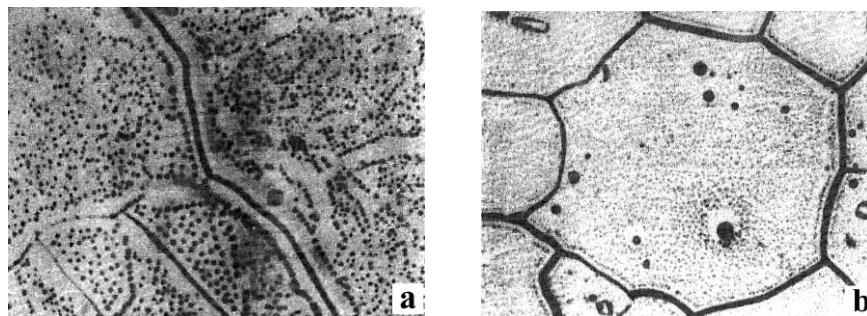
10 min, kako je prikazano na slici 8., mogla su se primetiti karakteristična staklasta izdvajanja.



**Sl. 8.** Mikrostruktura čiste platine nakon puzanja na  $1.350^{\circ}\text{C}$ , pri naprezanju od 13 MPa, u trajanju od 10 min (uvećanje 300x)

Slična izdvajanja bila su predmet istraživanja legure PtIr4, gde je primenjeno da na temperaturi višoj od 1.300°C površina uzorka pokrivena je mno-

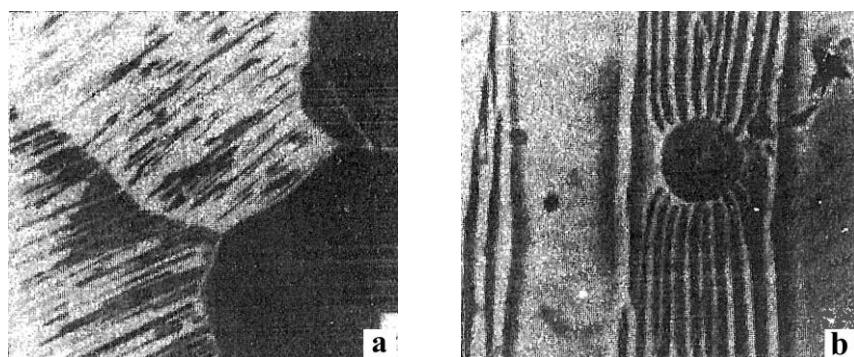
gobrojnim malim tečnim kapljicama, koje se postepeno slivaju obrazujući velike providne kapi, kako je prikazano na slici 9.



**Sl. 9.** Površina legure PtIr4 s obrazovanjem silikatnih kapljica nakon žarenja na 1.400°C:  
a) 4 h, uvećanje 500x; b) 300 h, uvećanje 100x

Granice i subgranice javljaju se istovremeno kao zona izdvajanja i dalje, odvođenja tečnosti. Izdvojena tečnost ote-

žava klizanje po ravni (111) unutar zrna, kako je prikazano na slici 10.



**Sl. 10.** Linije klizanja unutar zrna obrazovane na površini platine pri zagrevanju na vazduhu:  
a) do 1.300°C, uvećanje 200x; b) preko 1.300°C, uvećanje 500x

Ukoliko je brzina zagrevanja metala do 1.300°C prilično velika, stvaranje linija klizanja je malo verovatno. Samo u izuzetno nekontrolisanim slučajevima na površini platine, unutar zrna mogu se istovremeno opaziti mala količina linija klizanja i tečne faze, kako je prikazano na slici 10 b.

Odsustvo linija klizanja u prisustvu tečnosti (kapljica) na površini metala povezano je sa tim, da su sve kapi sjedinjene

u tanak film tečnosti koji sprečava stvaranje sloja adsorbovanog kiseonika, pa samim tim i stvaranje linija klizanja. Očvrsle kapi tečnosti nisu reagovale sa sonom i azotnom kiselinom, ali su se odlično rastvarale u fluorovodoničnoj kiselini. Mikro-analiza očvrslih kapi pokazala je prisustvo: 8%Si; 10%Al; 10%Ca; 0,1%Ni; 0,1%Fe; 0,1%Mn i 0,1%Mg. Pored nabrojanih elemenata prisutni su bili Pb i Na.

Spektralna analiza pokazala je da zagrevanjem platine, u trajanju od 800 h, dolazi do postepenog smanjenja sadržaja nečistoća poput Si, Fe, Ni, Ca i Mg. Obrazovanje tečne silikatne faze povezano je sa smanjenjem otpora puzanju platine i njenih legura, pri sadržaju nekih od navedenih primesa, budući da međusloj istopljenih silikata na ravnima granica zrna verovatno ubrzava klizanje.

## ZAKLJUČAK

Na osnovu dosadašnjih rezultata istraživanja, može se sledeće zaključiti:

U realnim uslovima u nastajanju ravnotežne segregacije može uzeti učešće desetak nečistoća i taj proces jako zavisi od njihovog međusobnog dejstva, dejstva s metalom - osnovom i legirnim elementima uz istovremenu zavisnost temperaturno - vremenskog faktora.

Ukoliko je viša temperatura metala pri hlađenju, utoliko je više i značajnije stvaranje para vakancija-intersticijski atom koji difunduje ka granicama zrna, pojačavajući neravnotežnu segregaciju nečistoća.

Uporedno sa ravnotežnom i neravnotežnom segregacijom nečistoća u platinskim legurama primećene su skupine nečistoća u obliku stranih uključaka. U tim uključcima nečistoće se nalaze, u obliku čvrstih jedinjenja, najčešće u obliku oksida. Čestice oksida dospevaju u leguru, u procesu topljenja u keramičkim loncima ili nastaju u vidu silikatnih uključaka u procesu zagrevanja. Veličina tih uključaka dostiže stotinu mikrometara.

Nečistoće poput Al, Mg, Si i Fe, prisutne u platinskim legurama, nakon zagrevanja na vazduhu ( $1.400^{\circ}\text{C}$ , 50 h), nalaze se u oksidnom obliku, dok se nakon žarenja u vuksu ( $1.400^{\circ}\text{C}$ , 2 h) registruju u elementarnom stanju.

Ispitivanjem legure sastava PtRh20Pd10Ir0,1Au0,1 pokazano je da strani uključci sadrže deseti deo procenta S, C, P i Pb i drugih štetnih nečistoća

Segregacija nečistoća u platinskim legurama uslovljena je prirodnom nečistoća, njihovom koncentracijom, raspodelom u zapremini metala, uzajamnim dejstvom sa osnovnim i legirnim komponentama, kao i temperaturno - vremenskim faktorom. Moguće je očekivati da kao rezultat uzajamnog dejstva štetnih nečistoća s platinским metalima koji ulaze u sastav legure, nastaju sniženja visokotemperaturne otpornosti legure i povećanje verovatnoće krtog preloma na visokim temperaturama

## LITERATURA

- [1] H. Gavin, Platinum Met. Rev. 54 (2010) 166.
- [2] E. Preston, Platinum Met. Rev. 4 (1960) 48.
- [3] D. F. Lupton, J. Merker, B. Fischer, R. Völkl, 24<sup>th</sup> International Precious Metals Conference, Williamsburg, Virginia, USA, 1–14 June 2000.
- [4] Y. Ning, Z. Yang, H. Zhao, Platinum Met. Rev. 4 (1996) 80.
- [5] N. Yuantao, Y. Zhengfen, Platinum Met. Rev. 43 (1999) 62.
- [6] B. Trumić, D. Stanković, V. Truić, J. Min. Metall., Sect. B 45 (1) B (2009) 79 – 87.
- [7] B. Wu, G. Liu, , Platinum Met. Rev. 41 (1997) 81.
- [8] M. Funabikia, T. Yamadaa, K. Kayanoa, Catal. Today 10 (1991) 33.
- [9] T. Biggs, S.S. Taylor, E. Van der Lingen, Platinum Met. Rev. 49 (2005) 2.
- [10] John C. Wright, Platinum Metals Rev., 2002, 46 (2), 66.
- [11] T. Biggs, M. B. Cortie, M. J. Witcomb, L. A. Cornish, Platinum Metals Rev., 2003, 47, (4), 142.
- [12] T. Biggs, M.J. Witcomb, L.A. Cornish, Materials Science and Engineering A273–275 (1999) 204.
- [13] F. Xiao, F. Zhao, D. Mei, Z. Mo, B. Zeng, Biosens. Bioelectron. 24 (2009) 3481.

- [14] K. T. Jacob, S. Priya, and Y. Waseda, Metall. Mater. Trans. A 29A (1998) 1545.
- [15] G. Dereli, T. Cagin, M. Uludogan, M. Tomak, Philos. Mag. Lett. 75 (4) (1997) 209.
- [16] P. Battaini, Platinum Met. Rev. 55 (2011) 74.
- [17] J. Luyten, J. De Keyzer, P. Wollants, C. Creemers, Calphad 33 (2009) 370.
- [18] B. Trumic, L. Gomidželović, S. Marjanović, V. Krstić, A. Ivanović, S. Dimitrijević, Pt-Materials Testing, 55 (2013) 38.
- [19] Ритвин, Е. И., Медовој, Л. А.: Влияние физико-химическој следи на жаропрочност мераллических материалов, Москва, Наука, 1974
- [20] Савицкиј, Е. М., Полјакова В. П., Горина, Н. Б., Рошан, Н. Р.: Металоведение платиновых металлов, Москва, Металургија, 1975.
- [21] Захаров, М. В., Захаров, А. М.: Жаропрочные сплавы, Москва, Металургија, 1983.
- [22] Ритвин, Е. И.,: Жаропрочност платиновых сплавоажв, Москва, Металургија, 1987.
- [23] B. Trumić, L. Gomidželović, M. Bugarin, Mining and Metallurgy Engineering Bor, 1/2015, str. 141-148.

Bore Jegdić\*, Maja Stevanović, Aleksandar Jegdić\*

## CHEMICAL AND ELECTROCHEMICAL DISSOLUTION OF CHROMIUM AT ROOM AND ELEVATED TEMPERATURES\*\*

### Abstract

The influence of temperature on electrochemical and chemical dissolution of chromium was studied in the acidic sulphuric solutions. The hydrogen evolution reaction, as well as the anodic dissolution and chemical dissolution of chromium from activated surfaces in sulphuric acid solutions pH 1 follow the Arrhenius law, with the apparent activation energies of  $35 \text{ kJ mol}^{-1}$ ,  $58 \text{ kJ mol}^{-1}$  and  $62 \text{ kJ mol}^{-1}$ , respectively. The higher activation energy of the chemical dissolution of chromium leads to the significantly noticeable chemical corrosion on elevated temperatures in comparison with the electrochemical corrosion.

**Keywords:** chromium chemical corrosion, electrochemical dissolution, activation energy

### INTRODUCTION

Simultaneously with the electrochemical dissolution of chromium occurs its chemical dissolution, which does not depend on potential and that, in certain circumstances, is dominant process of dissolution, especially at elevated temperatures [1-9]. Chemical dissolution is the cause of occurrence the hydrogen evolution, which is not subjected to the laws of electrochemical kinetics.

Determination the activation energy of chemical chromium dissolution, electrochemical chromium dissolution, cathodic hydrogen evolution and temperature dependence on electrochemical corrosion rate was determined and analyzed in this paper. Also, texture of chromium was determined using the OIM method (orientation imaging microscopy). Determination of chromium concentration in solution was carried out by the atomic absorption spectroscopy (AAS). The anodic and cathodic polarization curves

were recorded, and also, electrochemical corrosion rates were determined using the various electrochemical methods.

### EXPERIMENTAL PART

Before testing, the surface of chromium samples was mechanically polished gradually with abrasive paper to the grade 1000. The solution for testing was  $0.1 \text{ M Na}_2\text{SO}_4 + \text{H}_2\text{SO}_4$ , pH 1, which was purified conducting through testing solution of pure nitrogen.

A three-part glass electrochemical cell with water jackets for thermostating, with an auxiliary Pt electrode and a saturated calomel electrode (SCE) as the reference electrode were used for electrochemical tests.

The chromium electrode was cathodically activated at  $-0.900 \text{ V}$  for 120 s to the aim of removal the surface oxide layer before each test. Oxide layer is spontaneously cre-

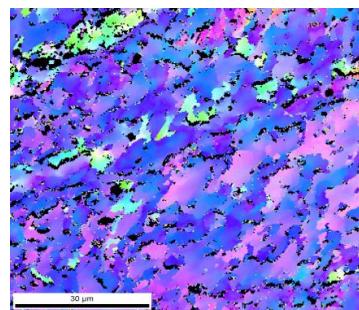
\* Institute for Chemistry, Technology and Metallurgy, IHTM, University of Belgrade, Njegoševa 12, Belgrade, Serbia, E-mail: borejegdic@yahoo.com

\*\* The work was funded by the Ministry of Education and Science and Technological Development of the Republic of Serbia, Project No. 34028.

ates on the chromium surface in contact with air. Electrochemical measurements were made using the potentiostat-galvanostat PAR 273.

## RESULTS AND DISCUSSION

Figure 1 shows the inverse polar image of chromium, obtained by the OIM method.

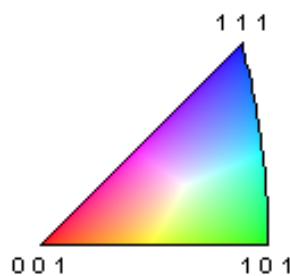


**Figure 1** Texture (111) of the chromium electrode is obtained by the OIM method. The approximate grain size can be estimated on the basis of the scale given in Figure

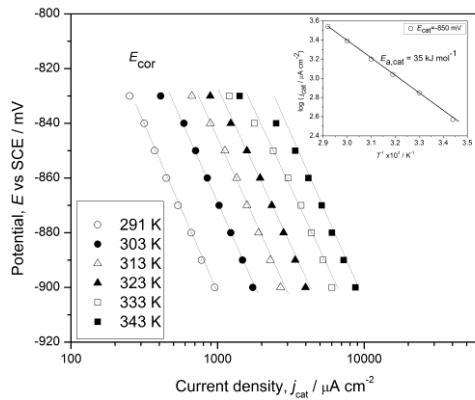
The temperature influence on chemical and electrochemical chromium dissolution in temperature the range from 291 to 353 K in aqueous sulphuric acid, pH 1 was carried out.

Cathodic polarization curves, recorded at different temperatures at 291 to 343 K in sulphuric acid pH 1, are shown in Figure 2. Figure 2 shows that with an increase in temperature, the rate of hydrogen evolution in

The grains with the orientation (111) are marked with blue colour and it can be seen that a large number of grains on the chromium surface has exactly this orientation. The size of chromium crystal grains was also determined, which have been the small dimensions, with a high degree of in orientations. In fact, these are separate grains with their own orientation.



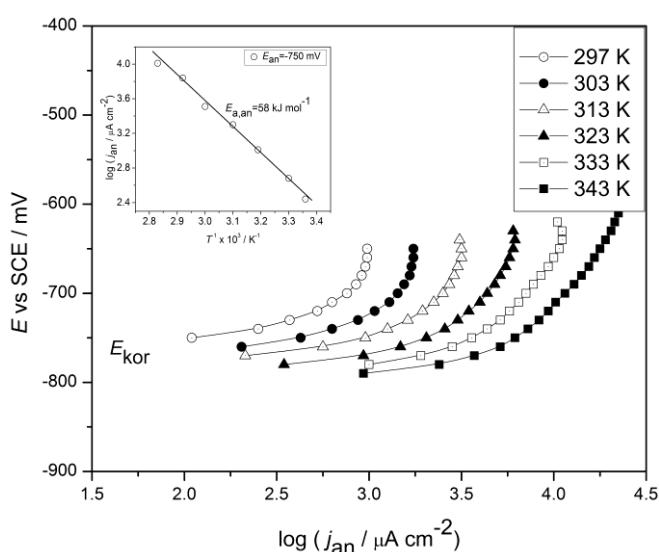
increases, while the Tafel slope variation with the temperature was at theoretically expected levels. An inset in Figure 2 shows the dependence of current density logarithm as a function of reciprocal temperature for determination the apparent activation energy for hydrogen evolution at -0.860 V. The apparent activation energy  $35 \text{ kJ mol}^{-1}$  is for cathodic reaction of hydrogen evolution.



**Figure 2** Chatodic polarization curves for chromium electrode in aqueous solution of  $0.1 \text{ M } \text{Na}_2\text{SO}_4 + \text{H}_2\text{SO}_4$ , pH 1 at various temperatures

The anodic polarization curves of chromium in the solution of sodium sulphate and sulphuric acid pH 1, recorded at different temperatures, were shown Figure 3. The shape of polarization curves is similar, except that the curves at higher temperatures are shifted towards higher current densities, as it might be expected. The Arrhenius dependence at -0.750 V is shown

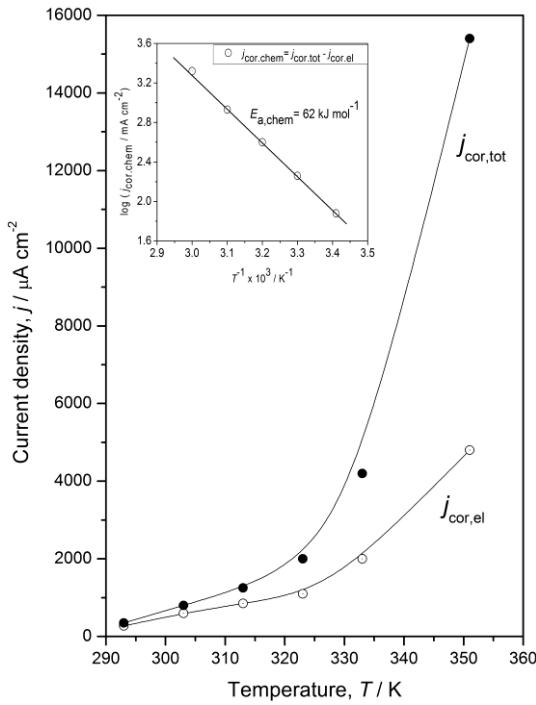
in inset in Figure 3. The apparent activation energy  $E_{a,an} = 58 \text{ kJ mol}^{-1}$  obtained for the reaction of the active anodic dissolution. This indicates that the anodic reaction is more dependent on temperature than the cathodic reaction. The corrosion potential change with temperature in a direction of more negative potentials also explains this.



**Figure 3** Anodic polarization curves of chromium electrode in sulphuric acid solution pH 1, at various temperatures

The electrochemical current density  $j_{cor,el}$  is determined by extrapolation the Tafel slope on corrosion potential and by the Stern-Gerry linear polarization method, while the total chromium dissolution rate  $j_{tot}$  was determined analyzing the solution with atomic absorption spectrophotometry, and they are shown in Figure 4. It can be seen from Figure 4 that the overall rate of dissolution or equivalent current density with temperature is higher than the electro-

chemical corrosion current density. A significant part of electrochemical corrosion is the chemical corrosion of chromium at all temperatures. That difference increases with temperature as it can be seen in Figure 4. At 353 K, the total dissolution rate is about four times higher than the electrochemical corrosion rate. It means that the chemical dissolution rate at this temperature is for approximately three times higher than the electrochemical dissolution rate.



**Figure 4** Total current density obtained analytically (●) and corrosion current density obtained electrochemically at different temperatures (○) for the chromium electrode

As it is shown in Figure 4, the overall corrosion rate  $j_{tot}$  at all temperatures that are used in this experiment are higher than the electrochemical corrosion rates  $j_{cor,el}$ . This is the result of chemical dissolution of chromium, which takes place directly by reaction of water molecules and atoms of chromium from the electrode surface and not dependent on potentials. Differences between the total chromium dissolution rate determined analytically  $j_{tot,anal}$  and electrochemical dissolution rate  $j_{cor,el}$  vs. the reciprocal temperature is plotted on the inset in Figure 4. The apparent activation energy was determined from the slope of this linear dependence and it is  $62 \text{ kJ mol}^{-1}$ . The high value of activation energy indicate that the influence of temperature on reaction of chemical dissolution is large and that contribution of chemical corrosion to the overall corrosion rate is

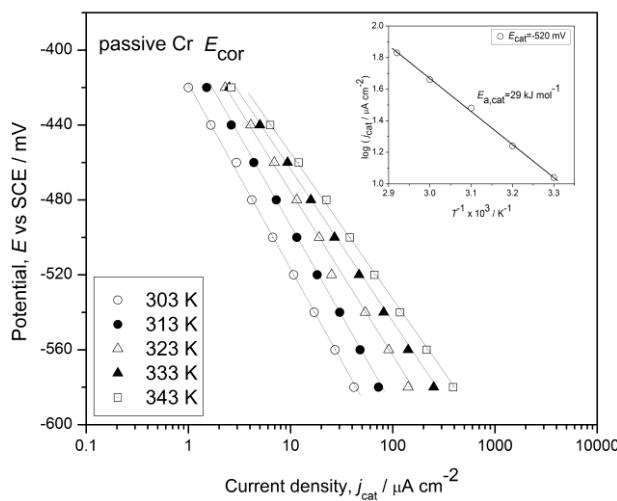
higher at the elevated than the lower temperatures. This should be kept in mind if using data for corrosion rate, obtained at room temperature, for predicting the corrosion behaviour at elevated temperatures. The similar differences in terms of temperature influence likely existing in case of corrosion of other metals that corrode electrochemically and chemically (i.e., Fe, Ni, Mn and other metals).

After immersion into testing solution, the chromium electrode is in a passive state with the characteristic corrosion potential  $E_{cor,1}$ . During the cathodic polarization at -0.900 V, for several tens of seconds, the passive films are dissolved, whereby the electrodes activated and the corrosion potential  $E_{cor,2}$  is then formed.

The chatodic curves recorded on passive chromium in form of the Tafel dia

grams for different temperatures are presented in Figure 5. It can be noted that cathodic Tafel slope is approximately  $-0.060$  V dec $^{-1}$  and that the current density increases with temperature. The inset in Figure 5 shows the Arrhenius dependence,

obtained at  $-0.520$  V. The apparent activation energy was determined, that is  $29$  kJ mol $^{-1}$ . Slightly lower value of activation energy is than obtained in the process of hydrogen evaluation on the activated chromium surface ( $35$  kJ mol $^{-1}$ ).



**Figure 5** The cathodic Tafel plots for passivated chromium electrode at different temperature

Accordingly, the corrosion of active metallic chromium in an aqueous solution of sulphuric acid pH 1 consists of two simultaneous processes corrosion, the electrochemical corrosion and chemical dissolution. With increase of temperate, significantly increases the anodic dissolution, chemical dissolution, and cathodic hydrogen evolution on the bare chromium surface, as well as on the surface coated with chromium oxide in  $0.1$  M  $\text{Na}_2\text{SO}_4 + \text{H}_2\text{SO}_4$  solution, pH 1.

Reaction of the hydrogen evolution, anodic dissolution and chemical dissolution on the activated chromium surface in sulphuric acid solution, pH 1 in temperature range of 293 to 353 K followed the Arrhenius dependence with an apparent activation energy of  $35$  kJ mol $^{-1}$ ,  $58$  kJ mol $^{-1}$  and  $62$  kJ mol $^{-1}$ , respectively. The apparent activation energy of the hydrogen evolution reaction on chro-

mium oxide covered surface has value of  $29$  kJ mol $^{-1}$ .

## CONCLUSION

Corrosion of the active metallic chromium in aqueous sulphuric acid pH 1 simultaneously flowed by electrochemical and chemical mechanism. The rate of chemical corrosion is obtained as difference of the total and electrochemical corrosion rate.

Reaction of the hydrogen evolution, anodic dissolution and chemical dissolution of Cr from chromium-activated surface in sulphuric acid solution, pH 1 at temperature from 291 to 353 K followed the Arrhenius law from the apparent activation energy of  $35$  kJ mol $^{-1}$ ,  $58$  kJ mol $^{-1}$  and  $62$  kJ mol $^{-1}$ , respectively. A high activation energy of chemical dissolution of chromium, at ele

vated temperatures causes to significantly higher chemical corrosion, compared to electrochemical corrosion. The apparent activation energy of hydrogen evolution on the chromium-covered oxide layer has a value of  $29 \text{ kJ mol}^{-1}$ .

As the result of simultaneous occurrence of reaction of hydrogen evolution on the oxide-covered chromium surface and reaction of anodic dissolution of chromium through the passive film, the stable corrosion potential  $E_{\text{cor},1}$  was formed. The other corrosion potential was formed as the results of cathodic hydrogen evolution and anodic dissolution on the bare chromium surfaces, when the chromium surface is depasivated (by cathodic activation, or mechanical action, etc.). In this case, the stable corrosion potential  $E_{\text{cor},2}$  establishes.

## REFERENCES

- [1] Wilde B. E., Hodge F. G., The Cathodic Discharge of Hydrogen on Active and Passive Chromium Surfaces in Dilute Sulphuric Acid Solutions, *Electrochim. Acta* 14 (7) (1969) pp. 619-627;
- [2] Kolotyrkin Ya. M., Florianovich G. M., Anomalnoe rastvorenje metallov. Eksperimentalnie fakti i ih teoreticheskoe tolkovanie, *Zashch. Metal.* 20 (1) (1984) pp. 14-24;
- [3] Dražić D. M., Popić J. P., Anomalous Dissolution of Metals and Chemical Corrosion (Review), *J. Serb. Chem. Soc.* 70 (3) (2005) pp. 489-513;
- [4] Dražić D. M., Popić J. P., Dissolution of Chromium in Sulfuric Acid, *J. Serb. Chem. Soc.* 67 (11) (2002) pp. 777-783;
- [5] Popić J. P., Dražić D. M., Electrochemistry of Active Chromium. Part III. Effect of Temperature, *J. Serb. Chem. Soc.* 68 (11) (2003) pp. 871-883;
- [6] Dražić D. M., Popić J. P., Electrochemistry of Active Chromium: Part I—Anomalous Corrosion and Products of Chromium Dissolution in Deaerated Sulfuric Acid, *Corrosion* 60 (3) (2004) pp. 297-304.
- [7] Popić J. P., Dražić D. M., Electrochemistry of Active Chromium: Part II. Three Hydrogen Evolution Reactions on Chromium in Sulfuric Acid, *Electrochim. Acta* 49 (27) (2004) pp. 4877-4891;
- [8] Dražić D. M., Popić J. P., Jegdić B., Vasiljević-Radović D., Electrochemistry of Active Chromium. Part IV. Dissolution of Chromium in Deaerated Sulfuric Acid, *J. Serb. Chem. Soc.* 69 (12) (2004) pp. 1099-1110;
- [9] Sukhotin A. M., Khoreva N. K., Passivnost khroma. Osobennosti katodnogo aktivirovaniya khroma, *Electrokhimiya* 18 (1) (1982) pp. 132-134;
- [10] Jegdić B., Dražić D. M., Popić J. P., Structural Effects of Metallic Chromium on its Electrochemical Behavior, *J. Serb. Chem. Soc.* 72 (6) (2007) pp. 563-578;
- [11] Jegdić B., Dražić D. M., Popić J. P., Influence of Chloride Ions on the Open Circuit Potentials of Chromium in Deaerated Sulfuric Acid Solutions, *J. Serb. Chem. Soc.* 71 (11) (2006) pp. 1187-1194;
- [12] Jegdić B., Dražić D. M., Popić J. P., Open Circuit Potentials of Metallic Chromium And Austenitic 304 Stainless Steel in Aqueous Sulphuric Acid Solution and the Influence of Chloride Ions on them, *Corr. Sci.* 50 (2008) pp. 1235-1244.

Bore Jegdić\*, Maja Stevanović, Aleksandar Jegdić\*

## HEMIJSKO I ELEKTROHEMIJSKO RASTVARANJE HROMA NA SOBNOJ I NA POVIŠENIM TEMPERATURAMA \*\*

### Izvod

*Ispitivan je uticaj temperature na elektrohemijsko i hemijsko rastvaranje hroma u kiselim rastvorima sulfata. Reakcije izdvajanja vodonika, anodnog rastvaranja i hemijskog rastvaranja hroma sa aktivirane površine hroma u rastvoru sumporne kiseline pH 1 slede Arenijusovu zavisnost sa prividnom energijom aktivacije 35 kJ mol<sup>-1</sup>, 58 kJ mol<sup>-1</sup> i 62 kJ mol<sup>-1</sup>, respektivno. Velika energija aktivacije hemijskog rastvaranja hroma dovodi na povišenim temperaturama do znatno izraženije hemijske korozije u odnosu na elektrohemiju koroziju.*

**Ključne reči:** hemijska korozija hroma, elektrohemijsko rastvaranje, prividna energija aktivacije

### UVOD

Paralelno sa elektrohemijskim rastvaranjem hroma odvija i njegovo hemijsko rastvaranje, koje ne zavisi od potencijala i koje je u nekim uslovima dominantan proces rastvaranja, naročito na povišenim temperaturama [1-9]. Hemijsko rastvaranje hroma je uzrok pojavi izdvajanja vodonika, koje ne podleže zakonitostima elektrohemijske kinetike.

U ovom radu vršeno je određivanje energije aktivacije procesa hemijskog rastvaranja hroma, elektrohemijskog rastvaranja hroma, katodnog izdvajanja vodonika i temperaturne zavisnosti brzine elektrohemijske korozije. Takođe, određena je teksture hroma primenom OIM metode (orientation imaging microscopy). Određivanje koncentracije hroma u rastvoru je vršeno primenom atomske apsorpcione spektroskopije (AAS). Vršeno je snimanje anodnih i katodnih polarizacionih krivih i određi-

vanje brzine elektrohemijske korozije primenom različitih elektrohemijskih metoda.

### EKSPERIMENTALNI DEO

Pre ispitivanja, površina uzorka hroma je mehanički polirana stupnjevito brusnim papirom do finoće 1000. Rastvor za ispitivanje je bio 0,1 M Na<sub>2</sub>SO<sub>4</sub> + H<sub>2</sub>SO<sub>4</sub>, pH 1, koji je deaerisan provođenjem prečićenog azota. Za izvođenje elektrohemijskih ispitivanja korišćena je trodelna staklena elektrohemijska celija sa vodenim plastirom za termostatiranje, sa Pt pomoćnom elektrodom i zasićenom kalomelovom elektrodom (ZKE) kao referentnom elektrodom.

Pre merenja, elektroda hroma je aktivirana katodnom polarizacijom na -0,900 V tokom 120 s radi uklanjanja površinskog oksida, koji se na hromu uvek spontano stvara u dodiru sa vazduhom. Elektro-

\* NU Institut za hemiju tehnologiju i metalurgiju, IHTM, Univerzitet u Beogradu, Njegoševa 12, Beograd, Srbija, e-mail: borejegdic@yahoo.com

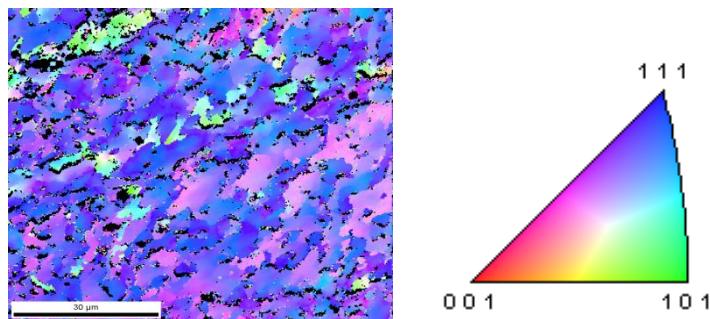
\*\* Ovaj rad je finansiran od strane Ministarstva prosvete, nauke i tehnološkog razvoja Republike Srbije, Projekat No. 34028.

hemijksa merenja su izvedena primenom potencijostata-galvanostata PAR 273.

## REZULTATI I DISKUSIJA

Na slici 1 je prikazana inverzna polarna slika uzorka hroma dobijena OIM metodom.

Plavom bojom je označena orijentacija zrna (111) i vidi se da veliki broj zrna na površini elektrode ima upravo tu orijentaciju. Takođe određena je veličina kristalnih zrna, koja su bila malih dimenzija sa velikim stepenom razorijentisanosti. Zapravo, to su zasebna zrna sa sopstvenom orijentacijom.

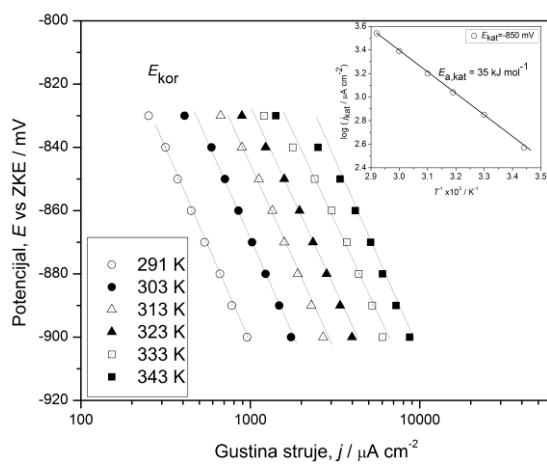


**Sl. 1.** Inverzna polarna slika, tekstura (111) elektrode hroma dobijena OIM metodom.  
Orijentaciona veličina zrna se može proceniti na osnovu razmere date na slici

Ispitivan je uticaj temperature na hemijsko i elektrohemski rastvaranje elektrode Cr u temperaturnom intervalu od 291 do 353 K u vodenom rastvoru sumporne kiseline, pH 1.

Katodne polarizacione krive snimljene na različitim temperaturama iz oblasti od 291 do 343 K u sumpornoj kiselini pH 1 su prikazane na slici 2. Sa slike se vidi da se sa povećanjem temperature povećava brzina

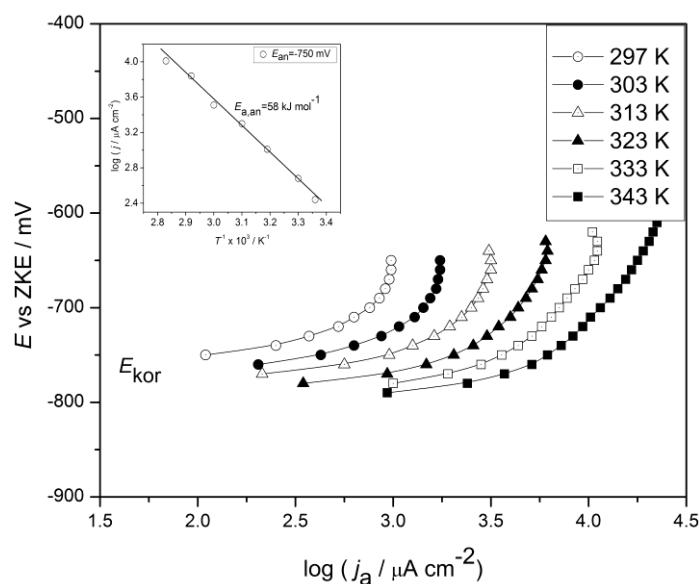
izdvajanja vodonika, pri čemu je varijacija Tafelovih nagiba sa temperaturom bila u teoretski očekivanim okvirima. Isečak na slici 2 prikazuje zavisnost logaritma gustine struje kao funkcije recipročne temperature, za određivanje prividne energije aktivacije, za reakciju izdvajanja vodonika na -0,860 V. Prividna energija aktivacije za reakciju katodnog izdvajanja vodonika je  $35 \text{ kJ mol}^{-1}$ .



**Sl. 2.** Katodne polarizacione krive za elektrodu hroma u vodenom rastvoru  $0,1 \text{ M } \text{Na}_2\text{SO}_4 + \text{H}_2\text{SO}_4$ , pH 1 na različitim temperaturama

Na slici 3 su prikazane krive anodne polarizacije hroma u rastvoru natrijum-sulfata i sumporne kiseline pH 1 snimljene na različitim temperaturama. Oblik polarizacionih krivih je sličan izuzev što su krive na većim temperaturama pomerene prema većim gustinama struje, kao što se moglo i očekivati. Arenijusova zavisnost za -0,750 V

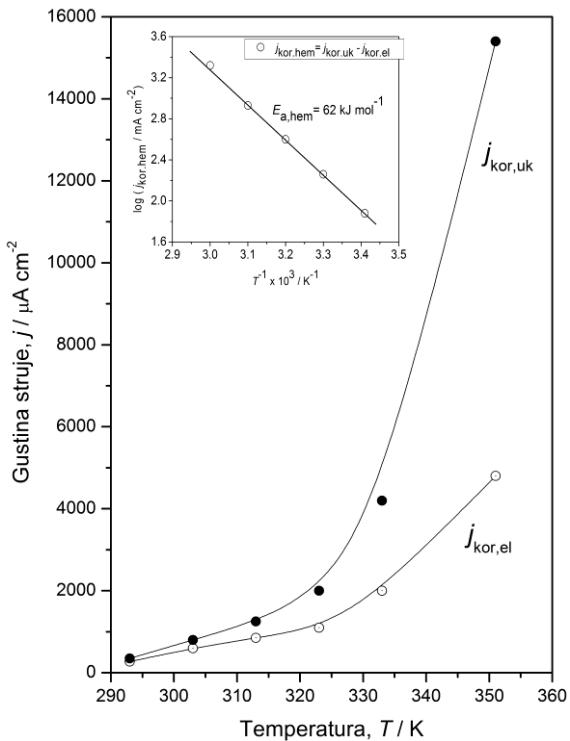
prikazana na isečku na slici 3 daje prividnu energiju aktivacije za reakciju aktivnog anodnog rastvaranja od  $E_{a,an} = 58 \text{ kJ mol}^{-1}$ . To ukazuje da anodna reakcija više zavisi od temperature nego katodna reakcija, što takođe objašnjava promenu korozionog potencijala sa temperaturom u smeru negativnijih potencijala.



**Sl. 3. Anodne polarizacione krive za elektrodu hroma u rastvoru sumporne kiseline pH 1 na različitim temperaturama**

Gustina struje elektrohemijske korozije  $j_{kor,el}$  je određivana ekstrapolacijom Tafelovih nagiba na korozioni potencijal i Stern-Gerievom metodom linearne polarizacije, dok je ukupna brzina rastvaranja određivana analizom rastvora primenom atomske apsorpcione spektrofotometrije  $j_{uk,an}$ , i prikazane su na slici 4. Sa slike 4 se može videti da je ukupna brzina rastvaranja, odnosno ekvivalentna gustina struje za sve temperature veća nego gustina struje elektrohemijskog rastvara-

nja tj. elektrohemijske korozije. To pokazuje da postoji pored elektrohemijskog značajno hemijsko rastvaranje hroma na svim temperaturama. Ta razlika se povećava sa povećanjem temperature kao što se može videti sa slike 4. Na 353 K ukupna brzina rastvaranja je približno četiri puta veća nego elektrohemijska brzina korozije. U isto vreme to znači da je brzina hemijskog rastvaranja na toj temperaturi približno tri puta veća nego brzina elektrohemijskog rastvaranja.



Sl. 4. Ukupna gustina struje dobijena analitički (●) i gustina korozione struje dobijena elektrohemiski na različitim temperaturama (○) za elektrodu hroma

Kao što je prikazano na slici 4, ukupne brzine korozije  $j_{\text{uk}}$  na svim temperaturama koje su korišćene pri ovim eksperimentima su veće nego elektrohemiske brzine korozije  $j_{\text{kor},\text{el}}$ . Ta razlika je posledica hemijskog rastvaranja hroma, koji se odvija direktnom reakcijom molekula vode i atoma hroma sa površine elektrode i koji ne zavisi od potencijala. Razlike između ukupne brzine rastvaranja određene analitički  $j_{\text{uk,anal}}$  i elektrohemiskih brzina korozije  $j_{\text{kor},\text{el}}$  su nacrtane u zavisnosti od recipročne vrednosti temperature na isečku na slici 4. Iz nagiba te pravolinijske zavisnosti se može odrediti prividna energija aktivacije i ona iznosi  $62 \text{ kJ mol}^{-1}$ . Visoka vrednost energije aktivacije ukazuje da je uticaj temperature na reakciju hemijskog rastvaranja prilično velik i da je doprinos ukupnoj brzini korozije veći u oblasti povišenih nego nižih

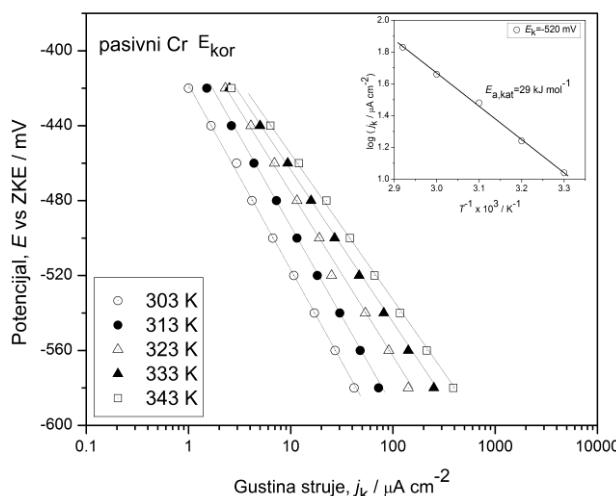
temperatura. To treba imati u vidu kada se koriste podaci o brzini korozije dobijeni na sobnoj temperaturi za predviđanje korozionog ponašanja na povišenim temperaturama. Vrlo je moguće da slične razlike u pogledu uticaja temperature postoje u slučaju korozije ostalih metala koji korodiraju i elektrohemiski i hemijski (tj. Fe, Ni, Mn i drugi).

Hrom se nalazi u pasivnom stanju posle uranjanja u rastvor za ispitivanje, sa karakterističnim korozionim potencijalom  $E_{\text{kor},1}$  koji odgovara pasivnom stanju hroma. Tek katodnom polarizacijom na -0,900 V u toku nekoliko desetina sekundi, pasivni films se rastvara, pri čemu se elektroda aktivira. Tada se formira korozioni potencijal  $E_{\text{kor},2}$  koji odgovara aktivnom hromu.

Katodne krive snimljene na pasiviranom hromu, prikazane u obliku Tafelovog dijagrama za različite temperature predstavljene

su na slici 5. Uočava se da je katodni Tafelov nagib približno jednak  $-0,060$  V dek $^{-1}$  i da se gustina struje povećava sa temperaturom. Isečak na slici 5 predstavlja Arenijusov dijagram dobijen na  $-0,520$  V sa koga

se može odrediti prividna energija aktivacije koja iznosi  $29$  kJ mol $^{-1}$ . To je nešto manja vrednost nego energija aktivacije za izdvajanje vodonika na aktiviranoj površini hroma ( $35$  kJ mol $^{-1}$ )



**Sl. 5.** Katodne Tafelove zavisnosti za pasiviranu elektrodu B sa slike 4.29. na različitim temperaturama

Prema tome korozija aktivnog metalnog hroma u vodenom rastvoru sumporne kiseline pH 1 se sastoji od dva simultana koroziona procesa, elektrohemijske korozije i hemijskog rastvaranja. Pokazano je da se na Cr elektrodi u rastvoru  $0,1$  M  $\text{Na}_2\text{SO}_4 + \text{H}_2\text{SO}_4$ , pH 1 sa povišenjem temperature značajno ubrzavaju reakcije anodnog rastvaranja hroma, hemijskog rastvaranja hroma, katodnog izdvajanja vodonika na čistoj metalnoj površini, kao i na površini hroma prevučenoj oksidom.

Reakcija izdvajanja vodonika, reakcija anodnog rastvaranja i reakcija hemijskog rastvaranja hroma sa aktivirane površine u rastvoru sumporne kiseline pH 1 u temperaturskom intervalu od 293 do 353 K slede Arenijusovu zavisnost sa prividnom energijom aktivacije  $35$  kJ mol $^{-1}$ ,  $58$  kJ mol $^{-1}$  i  $62$  kJ mol $^{-1}$ , respektivno. Prividna energija aktivi-vacije reakcije izdvajanja vodonika na

hromu prekrivenom oksidom ima vrednost  $29$  kJ mol $^{-1}$ .

## ZAKLJUČAK

Korozija aktivnog metalnog hroma u vodenom rastvoru sumporne kiseline pH 1 se odvija paralelno elektrohemijskim i hemijskim mehanizmom. Brzina hemijske korozije se dobija iz razlika ukupne i elektrohemijske brzine korozije.

Reakcija izdvajanja vodonika, reakcija anodnog rastvaranja i reakcija hemijskog rastvaranja Cr sa aktivirane površine u rastvoru sumporne kiseline pH 1 u temperaturnom intervalu od 291 do 353 K slede Arenijusovu zavisnost sa prividnom energijom aktivacije  $35$  kJ mol $^{-1}$ ,  $58$  kJ mol $^{-1}$  i  $62$  kJ mol $^{-1}$ , respektivno. Velika energija aktivacije hemijskog rastvaranja hroma dovodi na povišenim temperaturama do znatno izra-

ženje hemijske korozije u odnosu na elektrohemiju koroziju. Prividna energija aktivacije reakcije izdvajanja vodonika na hromu prekrivenom oksidnim filmom ima vrednost  $29 \text{ kJ mol}^{-1}$ .

Korozioni potencijal je posledica simultanog odvijanja reakcije izdvajanja vodonika bilo na oksidom prekrivenoj površini hroma sa reakcijom anodnog rastvaranja hroma kroz pasivni film obrazujući stabilni potencijal  $E_{\text{kor},1}$  ili katodnim izdvajanjem vodonika i anodnim rastvaranjem ogoljene površine kada se površina hroma depasivira na neki način (katodnom aktivacijom, mehaničkim delovanjem itd.). U tom slučaju uspostavlja se stabilni korozioni potencijal  $E_{\text{kor},2}$ .

## LITERATURA

- [1] Wilde B. E., Hodge F. G., The cathodic discharge of hydrogen on active and passive chromium surfaces in dilute sulphuric acid solutions, *Electrochim. Acta* 14 (7) (1969) pp. 619-627.
- [2] Kolotyrkin Ya. M., Florianovich G. M., Anomalnoe rastvorenje metallov. Eksperimentalnie fakti i ih teorecheskoe tolkovanie, *Zashch. Metal.* 20 (1) (1984) pp. 14-24.
- [3] Dražić D. M., Popić J. P., Anomalous dissolution of metals and chemical corrosion (Review), *J. Serb. Chem. Soc.* 70 (3) (2005) pp. 489-513.
- [4] Dražić D. M., Popić J. P., Dissolution of chromium in sulfuric acid, *J. Serb. Chem. Soc.* 67 (11) (2002) pp. 777-783.
- [5] Popić J. P., Dražić D. M., Electrochemistry of active chromium. Part III. Effect of temperature, *J. Serb. Chem. Soc.* 68 (11) (2003) pp. 871-883.
- [6] Dražić D. M., Popić J. P., Electrochemistry of Active Chromium: Part I-Anomalous Corrosion and Products of Chromium Dissolution in Deaerated Sulfuric Acid, *Corrosion* 60 (3) (2004) pp. 297-304.
- [7] Popić J. P., Dražić D. M., Electrochemistry of active chromium: Part II. Three hydrogen evolution reactions on chromium in sulfuric acid, *Electrochim. Acta* 49 (27) (2004) pp. 4877-4891.
- [8] Dražić D. M., Popić J. P., Jegdić B., Vasiljević-Radović D., Electrochemistry of active chromium. Part IV. Dissolution of chromium in deaerated sulfuric acid, *J. Serb. Chem. Soc.* 69 (12) (2004) pp. 1099-1110.
- [9] Sukhotin A. M., Khoreva N. K., Passivnost khroma. Osobennosti katodnogo aktivirovaniya khroma, *Electrokhimiya* 18 (1) (1982) pp. 132-134.
- [10] Jegdić B., Dražić D. M., Popić J. P., Structural effects of metallic chromium on its electrochemical behavior, *J. Serb. Chem. Soc.* 72 (6) (2007) pp. 563-578.
- [11] Jegdić B., Dražić D. M., Popić J. P., Influence of chloride ions on the open circuit potentials of chromium in deaerated sulfuric acid solutions, *J. Serb. Chem. Soc.* 71 (11) (2006) pp. 1187-1194.
- [12] Jegdić B., Dražić D.M., Popić J. P., Open circuit potentials of metallic chromium and austenitic 304 stainless steel in aqueous sulphuric acid solution and the influence of chloride ions on them, *Corr. Sci.* 50 (2008) pp. 1235-1244.

*Ljiljana Savić\**, *Vladimir Radovanović\*\**, *Ljubinko Savić\**

## BUSINESS SUCCESS MANAGEMENT

### **Abstract**

*This paper first discusses the essence and purpose of measuring the business success as well as the theoretical-methodological problems in defining model for measuring the overall business success. By expression and measurement of business success the efficiency and effectiveness the functioning of entire system of the company are quantitatively formalized and defined. Modern environment characterized by complexity, uncertainty, frequent and significant changes and the existence of strong competition requires companies to constantly improve the measurement systems for business success. In this paper, disputing the significance of financial performance measures for control and measurement of business success, the necessity to establish a new approach is highlighted where the financial indicators are combined with a large number of non-financial indicators. Experience in practical use of different models is a valuable knowledge showing managers in which direction to go in order to have more effective support in the management process.*

*Bearing this in mind, the mining companies should improve systems for control and measurement of business success, drawing on the experience of complex business practices or confirmation of all those measures which have acquired the attributes of an effective instrument of management.*

**Keywords:** effectiveness, efficiency, measurement of business success, business success model, financial indicators, Prism performance.

## INTRODUCTION

Expressing and measuring of business success is an integral element of the control system, of which adequacy, the effectiveness of the management process directly depends on.

The problem of measuring the overall business success is viewed in terms of purpose, essence and theoretical-methodological problems in defining the model for measuring the overall business success. This issue gains importance in contemporary environments which are characterized by complexity and uncertainty, and where the strong requirements are manifested for meeting the interests of different stakeholders. It is necessary that the mining enterprises take into account the interests of stakeholders in

making profit, paying the debts, reliable supply to consumers, adequate remuneration and care about the community.

In order to get knowledge on how to increase the effectiveness of the model for measuring business success, as a prerequisite for efficient management, the existing models are analyzed as a valuable contribution to economic theory and practice. This knowledge is useful for managers of mining companies.

## EFFECTIVENESS, EFFICIENCY AND BUSINESS SUCCESS

As concepts that contain and link company objectives, resources and trans

\* Faculty of Technical Science, K. Mitrovica , e-mail: ljsavic@open.telekom.rs

\*\* Faculty of Technical Science, Čačak, e-mail: mrvladimirradovanovic@yahoo.com

formation processes that form the basis for realization the objectives, efficiency and effectiveness are essential for every company. Recognizing many similar but different concepts for defining these essential and at the same time the key economic phenomena, it can be assumed that [1]:

- Effectiveness is the request to firstly make the selection of right goals and then, using available resources, to achieve the maximum realization of the selected goals.
- Efficiency is a requirement that the realization of a certain degree of selected targets is achieved with the least use of available resources, i.e. with the greatest rationality of their use.

Effectiveness is therefore focused on the choice of needs that will be met by the company, i.e. the selection of objectives and activities and efficiency is focused on the productive capacity and rational use of resources that a company has.

A similar interpretation is represented in the national literature by D. Grozdanović [2]. A differentiated concept of effectiveness and efficiency is based on the attempt of success differentiation in the work in relation to the market environment and in relation to the internal conditions in production. In doing so, however, the question of measuring or criteria is raised for design such determined success in the work. Effects in the domain of effectiveness depend on the effects in the area of production efficiency. And vice versa, the effects in the field of efficiency are dependent on effects on the basis of effectiveness.

Theoretical and methodological distinction between effectiveness and efficiency is not easy especially when it comes to their measurement. The product is the result of choice but also the result of more efficient or less efficient real production.

The effectiveness of the results is a measure of output tasks or achieving the goal. In the production organizational units that means to achieve planned production tasks qualitatively and quantitatively. Tasks

can be achieved, but with the loss of sources used in the transformation process. Therefore both processes must be regarded. The efficiency of the results measure the costs of the sources used for the goal realization, that is the outputs in relation to inputs used [3].

Starting from the essence of economic efficiency and its apparent manifestations of the economy in general the effectiveness and efficiency as economic phenomena at the level of enterprise economy can be defined [1].

- *Economic efficiency* is essentially a manufacturing efficiency, i.e. the ability of efficient organization of the transformation of inputs into outputs of enterprises.
- *Economic efficiency* is an expression of the efficiency of the exchange because the selection of targets that meet societal needs and resources that define the production potential of the company ultimately comes down to the sale and purchase of inputs and outputs, i.e. the overall marketing activities.
- *Allocative efficiency*, term for efficiency in organization of production and exchange, is an expression of the overall efficiency of the company, which includes the effects of the efficiency and effects of effectiveness.

Integration of the efficiency and effectiveness in the unique expression of the overall economic efficiency is a function of measuring the performance of the overall company effects. Through understanding the overall effect, it is possible to manage effectively the economy of enterprises.

The quality of enterprise economy can be accessed through consideration the relationship between a uniquely understood product as the result of production and uniquely conceived social work introduced in reproduction in order to achieve that result.

Quantitative expression the quality of the economy is expressed by business success **Pu**, which is contained in the relations between the results of reproduction (output) and investments (inputs) to reproduction.

$$P_u = R(O_u)/U(I_n)$$

The quality of enterprise economy as the expression of economic success in achieving objectives degree at the same time is the expression of effectiveness and efficiency of enterprise and business development. In accordance with the statement that the economic significance of efficiency and effectiveness, i.e. only economic efficiency, is just in the teconomy quality and it follows that business success is a quantitative expression of efficiency and effectiveness [2].

## MEASUREMENT OF BUSINESS SUCCESS

The problem of measuring the total business success can be seen in terms of purpose, essence and theoretical methodological problems of defining the model for measuring business success.

The purpose of measuring the total business success of the company is clear information on the actual economic efficiency of enterprises, as well as on real economic effects of the new investments in the particular company of interest to the business owners. Continual measurement of business success is a realistic assumption for effective economic management of the company.

In the joint-stock companies, in which the ownership is separated from management, the measurement of business performance allows the owners to control managers who are engaged to manage the company.

The measurement of business success provides, in addition to the management efficiency, more realistic distribution of profits in the so-called financial groups of companies, more realistic view of actual effects of external growth.

The measurement of business success encourages the functioning of stock market, because potential investors (shareholders) have relevant information about their investments.

Expression of business success is a legal requirement without which the company cannot exist. The reported results serve as a basis for calculation and payment of dividends to the shareholders.

The owners, managers and state are interested in measuring the business success. Measuring the business success at the end of business period or continuously if required, is a necessary condition of efficient management and adequate satisfaction of stakeholders' interest.<sup>1</sup>

Substantial interpretation suggests that the overall success of business of concrete enterprise is the expression of the overall economic efficiency. This means that it expresses its overall allocative ability as the ability for selection and procurement of inputs; efficient organization of production as a transformation process and selection and implementation of products and services as the output of enterprises. All economic effects that are manifested in the inputs and outputs to a specific company express the overall economic efficiency [1].

Business success becomes quantitatively determined when measured and estimated by corresponding economic methods formulated in certain indicators or models. The main economic criteria of efficiency are important starting point for expression, monitoring, controlling and directing the relationship between the results and investments. Production volume, total revenue, income and profit are measured on side of the results and workforce, total costs and capital employed on the side of investment.

$$P_u = R(Q; C; D; D_b) / U(L; T; S)$$

If within the enterprise primary goal, the sub goals are viewed such as the production, accumulative and reproductive ability, the mentioned measures on the side of results and investments are formed in the tradition-

---

<sup>1</sup> Strategic constituents in the company are its stockholders or owners, customers, creditors, suppliers and other groups without whose co-operation enterprise cannot survive

nally complex known indicators of productivity ( $P=Q/L$ ), economy ( $E=C/T$ ) and profitability of  $R=D(Db)/S$ . These partial indicators are determined by the elements of results and investments; they are conditioned by factors forming quality of economy and activities to achieve the efficiency in the use of resources [4].

Expressing the business success by partial indicators as the enterprise economy measures shows the efficiency in functioning the production-financial company's subsystems. This allows the control and guidance the quality of certain subsystems of the economy to a unique integrated goal to achieve the efficiency of the whole company system. However, in expressing and managing the dynamics of business success, divergence and disadvantages of partial indicators as well as the complexity of this issue are manifested. It is caused by different intensity and direction of movement the elements of results and investments under the influence of positive or negative effects within operating activities.

The contemporary theory and practice resolve the expression and measurement problem of business success accepting two attitudes [2]:

- the first is based on the use of a number of individual indicators, where the denominator term is given most often in the form of quantitative evaluation, which is generally not objectified on some basis
- the second is based on an attempt to, along with numerous difficulties and constraints faced by the modern theory and practice, formulate and uses the synthetic term of business success, in the form of more or less integrated, maximum possible objectified model, which, along with mandatory additional qualitative indicators, physical expresses the change of overall economic quality.

The scope and content of any set of indicators or integral model of business success, should, on the basis of the basic criteria of

economic efficiency, primarily meet the informational, management-control and motivational functions in business [5].

### **THEORETICAL AND METHODOLOGICAL PROBLEMS OF DEFINING A MODEL FOR MEASURING THE BUSINESS SUCCESS**

Moving from a large number of partial indicators on a single indicator of overall efficiency requires solving the problem of reduction to a common denominator for the inputs and outputs of enterprises, as well as developing a complex business and information systems in the company, developed from a concrete model for measuring the business success.

In the constitution of model for expressing the overall business success, a model *Econometer* deserves a special attention as the original creation made by S. Kukoleča [6] which in dynamics record and report all connections and all changes in the shape of results and investments, reduced to a single common measure – working equivalent. The high level of abstraction and perfection in design and development of business success models in general, and specifically to the factors of conditionality, imposed the impression that it is difficult or impossible to achieve its implementation. This is especially true for a period of sixties when there were no support information systems in our companies. Also, that information base, required for measurements according to this model, on a small scale is associated with the official accounting and financial system. This represented one of the main obstacles for the use in practice.

Diligent efforts are also done by domestic scholars (D. Grozdanović and N. Malenović) on constituting the model for overall performance measurement of business success which overcomes some limitations of the original model and its subsequent modification (also by the two above mentioned authors), especially regarding the use of financial reporting information as a basis for calculation of certain elements [7].

The existing theoretical and practical instruments for controlling and directing business development and growth of the company do not allow consideration of a realistic picture of actual efficiency of modern enterprises. Many theoretical models derived from different company theories could not be applied to solve the specific problems in practice of companies. Thus, mathematical methods and models have limited utility in the application and were used for solving hypothetical cases rather than specific problems in the economy of companies.

The problem of efficient business of enterprises in management theories is formulated as the problem of determining maximum usefulness of managers, but since managers do not have unlimited discretion and their goals can be achieved with the conditions set by the owners of shareholders, maximizing of the utility function occurs as the result of problem solutions caused by maximization. Except a dichotomy of interests of the owners on one side, and managers, on the other side, does not identify the other important interests. Access to the objectives of the company changed over the time and techniques and methods of achieving the goals improved, but the basic objectives and their economic content were marginalized.

Financial indicators as the basis of traditional systems for measurement and control of business success have a clear control role bounded by certain period. Therefrom derived sets of various indicators, indices and ratio numbers, just show what the result of business in companies is during the past period and it is not expressed through the overall business success, but according to the partial statements of certain conditions and effects.

With the development of theories that deal with the economy of enterprises, the preconditions are created for development of models to measure the business success for such control of company and management of its economy to emphasize the positive and to reduce negative consequences with satis-

faction of all essential interests which are manifested in connection with business, growth and development.

### **FINANCIAL INDICATORS AS THE BASIS OF TRADITIONAL SYSTEMS OF MEASUREMENT AND CONTROL THE BUSINESS SUCCESS**

Common to all traditional systems of financial control and measurement the business success is that they are all based on data that can be obtained on the basis of the accounting system. Giving priority to the use of quantitative accounting information is explained by the fact that accounting as a single integrated system for quantitative analysis of the company, characterized by integrity of business and financial activities of the company and the advantage of numerical expressions from which a value objectivism is derived. Also, the advantage of accounting information is manifested in their capacity to turn different conditions, trends and relationships into a universal, generally accepted unique numeric expression.

An integrated set of financial statements of most companies in the international practice is consisted of a balance sheet<sup>2</sup> (the statement of financial position), income statement (profit and loss). Although being more and more favored, cash flow statement is not accepted in all countries<sup>3</sup>. Regardless of establishment on the

<sup>2</sup> One of the key changes in the revised IAS1, published in 2007 refers to the replacement of balance sheet with statement of financial position of the company. As a reason for this terminological changes are functions of this basic financial statement.

<sup>3</sup> According to accepted accounting standards, in addition to balance sheet, small businesses companies in our country are obliged to submit income statement and statistical annex to the Business Registers Agency (APR), a medium-sized and large companies are obliged to submit cash flow statement and statement of changes in capital.

same business and financial transactions and financial universal quantification of these transactions, the financial statements set as an objective chronicler of company gives a variety of information on its activities for a certain period.

Basic information content of the balance sheet date is a book value of the company or the state of assets, liabilities and equity (net asset value) on a particular day.

Income statement is known as a profit and loss account. Basic information content of the income statement is profitability. Balance sheet presents the information on income, expenditure and net profit / loss for the certain period.

All revenues and expenses of a conventionally adopted accounting period, mutual confronted and presented in accordance with the relevant principles and in the appropriate reporting forms, allow determination of the results, profit as positive and loss as negative differences, which at the end of the accounting period are included in the balance sheet as an increase or decrease (the own) capital. This understanding of the income statement indicates the existence of a systematic and organic links between balance sheet and income statement, and this fact indicates that these financial statements in terms of evaluation the efficiency of operations are treated as complementary and interdependent accounting products [8].

Cash-flow statement shows turnover on cash account through cash inflows and outflows as well as free cash flow generated in the period. Cash Flow Statement shows the business, financial and investment inflows and outflows of cash flows of the company during the reporting period. Basic information for control in cash flow statement is liquidity. Also, the cash flow statement carries information about the possibilities of creating value if a discounted free cash flow is implemented.

Certain financial statement items, shown in absolute values, do not give enough information for management. Ratio numbers

are obtained by bringing particular positions from balance sheet, income statement and other statements in appropriate relations.

In the control process, the ratio numbers are compared to the past results or the competition results, that is, ratio numbers can be used to monitor the results of the company over time or to monitor the relative position of the company in relation to the competitors. In any case, these relative values provide much richer information than absolute values analyze (financial statement). All ratio numbers can be classified into four major groups: liquidity indicators, turnover (activities) indicators, indicators of solvency (financial structure) and indicators of profitability (profitability) [9].

The aforementioned indicators are actually operational performance measures, namely indicators of the success that measure results of operational decisions. It is obvious that the effects of operational decisions include effects of strategic and tactical decisions [10].

In addition to the simple ratio numbers there are complex ratio numbers that arise by combining the ratio numbers, following a substantial part business process or specific aspects of the business. DuPont formula leads to a synthetic expression of profitability which allows establishing the change as well as causes of changes in profitability, because the overall profitability, that is, the return on total assets is seen as a result of interactions, or interactions of partial indicators of profitability [11].

For the purposes of managers as the internal users of financial and accounting reports in the company, the additional reports on operations can be made which should contribute to making the rational management decisions and taking appropriate actions.

The importance of the financial statements, which reflect the financial business activities of the company as a whole, is reflected in the fact that the analytical interpretation of data contained therein enables identification and monitoring the key

financial performance measures of enterprise efficiency. In addition to the traditional criteria of MIA, indicators are used lately that have their stronghold in the concept of value-based management. One of the most important is the economic value added (EVA). The following indicators are lately often used by economic analysts: Earning Before Interest (EBIT) and Earning Before Interest, Taxes, Depreciation and Amortization (EBITDA)

### **RESULTS OF ECONOMIC THEORY AND PRACTICE IN DEFINING THE MODEL FOR MEASURING THE OVERALL BUSINESS SUCCESS**

Despite irreplaceable role of the financial criteria, it is necessary to emphasize its imperfections and incompleteness for the purposes of valid analysis and evaluation of effectiveness. The use of traditional financial measures has certain drawbacks and limitations that are primarily related to: presentation of events that occurred in the previous period, unreliability of comparison base for a longer period, not giving enough importance to the business environment by ignoring the perspective of consumers and competitors. A problem of traditional measures, based on financial indicators, is that they do not take into account the intangible value contained in the knowledge that can greatly increase market value of the company.

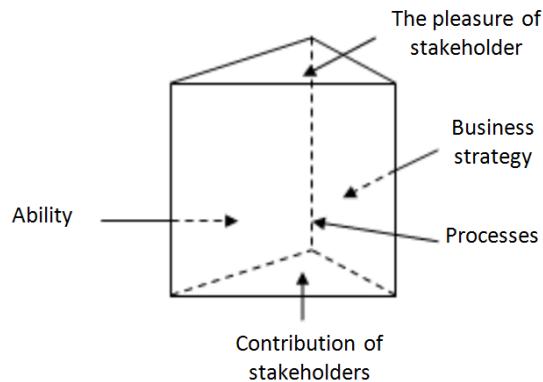
Changes in the environment, globalization of the world economy, strong competition and development of information technology leads to the changes in the traditional control apparatus. Industrial economy characterized by physically tangible assets is replaced by a new economy where the most valuable resource becomes intangible assets that include relationships with consumers, employee skills and their

knowledge, information and organizational culture favorable for innovation, problem solving and general improvement of organization [12].

In terms of developed market, the only sustainable way to create value for business owners at the same time is value creation for their stakeholders. Stakeholders therefore have legitimate interests in the company performance, as well as the specific requirements and needs that arise from the relationship in carrying out certain activities. In addition, the primary (active) stakeholders have a formal, official and contractual relationship with the company, while all the others can be considered as the secondary. Orientation to stakeholders implies that the model of business success include indicators of success in achieving the individual goals of all stakeholders as well as measurements of achieving these goals both expressed by appropriate indicators.

One of the most important roles of management is to find a balance between acceptable financial responsibilities towards the owners and strategic responsibilities to the other stakeholders. The higher the quality of the relationship of companies with stakeholders such as customers, employees, suppliers, communities and others, leads to better financial performance, and ultimately to a higher enterprise value, and shareholding wealth [13].

Model Prism performances – Based on said, and taking into account the causal processes among stakeholders, one of the modern model is formulated, so-called Performance Prism (A. Neely) which is considered to be an integral model because it combines the elements oriented on stakeholders and elements of process oriented models [5]. Prism performance model is shown in Figure 1.



**Figure 1** Prism performance as a model showing business success, according to [14]

Model Prism performance provides five different but related views, and thus reflects the business success of the company stated by set of indicators differentiated into five key groups, as well as answers to the questions [14]:

- The pleasure of stakeholder (top of the prism) - who are the key stakeholders and what they want or what they need;
- Business strategy (side of the prisms) - which strategy company needs to implement to satisfy the mentioned desires or needs
- Processes (side of the prisms) - what critical processes a company should apply to the set objective, favoring so-called processes that add value to the investment in reproduction
- Ability (side of the prisms) - what ability the key stakeholders should have (employees, customers, community and the owners of capital) in the exercise of applied processes and finally
- Contribution of stakeholders (bottom of the prisms) – what contribution the company can expect from stakeholders if the company's management supports and develops the skills of stakeholders

Management on the basis of these criteria involves defining the target perfor-

mance measures, comparing achievements with target-setting values, identifying deviations and causes (factors) of deviations, and finally identifying corrective management action. The model is considered valuable because it highlights the dimension of measures ability (resources). The main disadvantage is a big number of criteria that, considering the limited time and ability attention of managers, cannot be used operationally.

Numerous references prove that the application of multidimensional performance measurement system contributes to the effectiveness thereof (*Domanović, 2013*, according to: *Malina, M. A., & Selto, F. H. 2001*; *Ittner, C. D and others 2003*; *Davis, S., & Albright, T. 2004*; *Crabtree, A. D & De Busk, G.K 2008*; *Van der Stede, W.A. and others 2006*; *Tung, A. and others 2011*). Most of these studies examined the effectiveness of these systems from the perspective of contribution the same financial results [15].

The analyzed models of measurements as well as the other existing models that have proven their applicability in practice are of particular importance to improve the management process. Combining the existing models creates the new ones. The

improved measurement systems provide the real preconditions for efficient management, with appropriate support of information systems.

## CONCLUSION

In economic theory and business practice in companies, the issues of measuring overall business success is very live and still insufficiently rounded. From the management aspect the design of quality aggregate criteria requires previously solving extremely complex problem of reducing to a common denominator of different criteria for inputs and outputs of enterprises as well as development and use of appropriate information system for monitoring the budget and so the designed aggregate size of business success. Economic theory has offered a solution in the form of the optimal model Econometer. Model of total performance of business success tries to overcome some limitations of the original model and its subsequent modifications, especially regarding the use of financial reporting information as the basis for calculation the certain elements.

The financial measures have an irreplaceable role in the evaluation of enterprise business success; however, it is necessary to point to their imperfection and incompleteness with the need for a valid analysis of business success. In the modern period there is inability of financial indicators to include the intangible resources of the company (intellectual capital) and level of achievement of non-financial company goals (relationship with customers, employees) who are critical for business success in the modern period.

Effective measurement system is one that includes a set of financial and non-financial measures that will enable managers to successfully deal with a large number of business activities and focus on the key factors of business success. Model Prism performance is one such proposal (attempts). But there is no stopping here.

In the aim of real overview of the effectiveness and efficiency of the company, looking for solutions providing a new paradigm of enterprise and its appropriate model will continue.

The considered problem in this paper is useful for management of mining companies which will, through greater responsibility to their stakeholders, acquire the attributes of successful enterprise.

## REFERENCES

- [1] M. Nikolić, N. Malenović, D. Pokrajčić, B. Paunović, Enterprise Economics, Faculty of Economics, Kragujevac, 2003, pp. 122,136,475;
- [2] D. Grozdanović, Fundamentals of Enterprise Economics, Faculty of Economics, Kragujevac, 2003, pp. 23, 25,456;
- [3] M. Milisavljević, Contemporary Strategic Management, Megatrend University of Applied Sciences, Belgrade, 2005, p. 5;
- [4] Lj. Savić, The Tole of Management in Improving the Effectiveness and Efficiency of the Company, Doctoral Dissertation at Megatrend University, Faculty of Business Studies, Belgrade, 2010, p.100;
- [5] M. Ratković Abramović, Management of Dynamics of Business Success, the Copyright Issue, ŽELNID - Belgrade, 2005, pp. 67,79;
- [6] S. Kukoleča, Ekonometar, Consulting Center, Belgrade, 1994;
- [7] B. Krstić, Model of Measurement the Performance of the Overall Business Success of the Company, Faculty of Economics, Niš, 2007;
- [8] V. Domanović, J. Bogićević, The Possibilities of the Balanced Scorecard Concept Implementation in Serbia, NDE, Palić, 2011;
- [9] B.Pešalj, Company Performance Measurement, Faculty of Economics, Belgrade, 2006, p.63;

- [10] D. Djuričin, S. Janošević, Dj. Kaličanin, Management and Strategy, Faculty of Economics, Belgrade, 2013, p. 161;
- [11] D. Pokrajčić, Enterprise Economics, Copyright Issue, Čigoja štampa, Belgrade, 2002, p.356;
- [12] R. Kaplan and D. Norton, Having Trouble With Your Strategy? Then Mapit!, Harvard Business Review, September-October, 2000, p. 4;
- [13] Dj. Kaličanin, The Formulation and Implementation of Strategies of Value Creation, Doctoral Dissertation, Faculty of Economics, Belgrade, 2005, p.15;
- [14] A. Neely, Business Performance Measurement, Cambridge University Press, 2003, p. 153;
- [15] V. Domanović, The Effectiveness of the Performance Measurement in Terms of Contemporary Business Environment, Ekonomski horizonti, Faculty of Economics, Kragujevac, April 2013.

*Ljiljana Savić\**, *Vladimir Radovanović\*\**, *Ljubinko Savić\**

## UPRAVLJANJE POSLOVNIM USPEHOM

### *Izvod*

*U ovom radu se prvo ukazuje na suštinu i svrhu merenja poslovnog uspeha kao i na teorijsko-metodološke probleme u definisanju modela za merenje ukupnog poslovnog uspeha. Izražavanjem i merenjem ukupnog poslovnog uspeha kvantitativno se formalizuje i definiše efikasnost i efektivnost funkcionisanja celokupnog sistema preduzeća. Savremeno okruženje koje odlukuje složenost, neizvesnost, česte i značajne promene i postojanje izražene konkurenčije zahteva od preduzeća da stalno unapređuju sisteme merenja poslovnog uspeha. U radu se, ne sporeći značaj finansijskih merila za kontrolu i merenje poslovnog uspeha, ističe neophodnost uspostavljanja novih pristupa gde su finansijski pokazatelji kombinovani sa velikim brojem nefinansijskih pokazatelja. Iskustva u praktičnoj primeni pojedinih modela su vredna saznanja u kom pravcu treba dalje ići da bi menadžeri imali efikasniju podršku u upravljačkom procesu.*

*Imajući ovo u vidu rudarska preduzeća treba da unapređuju sisteme za kontrolu i merenje poslovnog uspeha, crpeći iskustva iz kompleksne poslovne prakse odnosno utvrđivanju svih onih merila koja su stekla atribute efikasnog upravljačkog instrumenta.*

**Ključne reči:** efektivnost, efikasnost, merenje poslovnog uspeha, model poslovnog uspeha, finansijski pokazateli, prizma performansi

## UVOD

Izražavanje i merenje ukupnog poslovnog uspeha sastavni je element upravljačkog sistema, od čije adekvatnosti neposredno zavisi i efikasnost samog upravljačkog procesa.

Problematika merenja ukupnog poslovnog uspeha sagledava se sa aspekta svrhe, suštine i teorijsko-metodoloških problema u definisanju modela za merenje ukupnog poslovnog uspeha. Ova problematika dobija na značaju u uslovima savremenog okruženja koje karakteriše složenost i neizvesnost i gde se ispoljavaju snažni zahtevi za zadovoljavanjem interesa različitih stekholdera. Rudarska preduzeća takođe moraju uvažavati interes neposrednih stekholdera u sticanju profita, isplati dugova, pouzda-

nom snabdevanju kupaca, adekvatnom nagrađivanju, vođenjem računa o doslednosti i dr.

U cilju sticanja saznanja o tome kako povećati efektivnost modela za merenje poslovnog uspeha danas, kao prepostavke za efikasnije upravljanje analiziraju se postojeći modeli kao vredni doprinosi ekonomskе teorije i prakse. Ova su znanja korisna za menadžersku strukturu rudarskih preduzeća.

## EFEKТИВНОСТ, ЕФИКАСНОСТ И POSLOVNI USPEH

Kao koncepti koji u sebi sadrže i povezuju ciljeve preduzeća, resurse i transfor-

\* Fakultet tehničkih nauka u Kosovskoj Mitrovici, e-mail: ljsavic@open.telekom.rs

\*\* Fakultet tehničkih nauka u Čačku, e-mail: mrvladimirradovanovic@yahoo.com

macione procese koji predstavljaju osnovu za realizaciju ciljeva, efikasnost i efektivnost su od suštinskog značaja za svako preduzeće. Uvažavajući brojne slične, pa i različite koncepte za definisanje ovih suštinskih i istovremeno ključnih ekonomskih fenomena može se poći od toga da [1]:

- *Efektivnost* podrazumeva zahtev da se prvo izvrši izbor pravih ciljeva a potom korišćenjem raspoloživih resursa ostvari maksimalna realizacija izabranih ciljeva.
- *Efikasnost* predstavlja zahtev da se realizacija određenog stepena izabranih ciljeva ostvari uz najmanje korišćenje raspoloživih resursa, odnosno uz najveću racionalnost njihove upotrebe.

Efektivnost je prema tome orijentisana na izbor potreba koje će preduzeće zadovoljavati, odnosno izbor ciljeva i delatnosti kojima će to obezbediti, a efikasnost na proizvodnu sposobnost i racionalnost upotrebe resursa kojima preduzeće raspolaže.

Slično tumačenje zastupa u domaćoj literaturi D. Grozdanović [2]. Diferencirani koncept efektivnosti i efikasnosti bazira na pokušaju diferenciranja uspeha u radu u odnosu na tržišno okruženje i u odnosu na interne uslove u proizvodnji. Pri tome se, međutim, otvara pitanje merenja odnosno kriterijuma za projektovanje tako određene uspešnosti u radu. Efekti u domenu efektivnosti zavise od efekata u domenu proizvodne efikasnosti. Važi i obratno, efekti u domenu efikasnosti su uslovljeni efektima po osnovu efektivnosti.

Teorijsko-metodološko razgraničenje efektivnosti i efikasnosti nije nimalo jednostavno, a pogotovo kada se radi o njihovom merenju. Proizvod je rezultat izbora ali i rezultat efikasnije ili manje efikasne ostvarene proizvodnje.

Efektivnost rezultata je merilo zadataka outputa ili ostvarenja cilja. U proizvodnim organizacionim jedinicama to znači ostvariti planirane proizvodne zadatke kvalitativno i kvantitativno. Zadaci se mogu ostvariti, ali uz gubitak izvora korišćenih u transforma-

cionom procesu. Zbog toga se moraju posmatrati oba procesa. Efikasnost rezultata meri troškove korišćenih izvora za ostvarenje cilja, tj. outputa u odnosu na korišćene inpute [3].

Polazeći od suštine ekonomske efikasnosti i njenih pojavnih manifestacija u ekonomiji uopšte efektivnost i efikasnost kao ekonomski fenomeni na nivou ekonomije preduzeća mogu se definisati [1]:

- *Ekonomska efikasnost* u suštini predstavlja proizvodnu efikasnost odnosno sposobnost efikasnog organizovanja transformacije inputa u outpute preduzeća.
- *Ekonomska efektivnost* predstavlja izraz efikasnosti razmene jer se izbor ciljeva kojima se definišu proizvodni potencijali preduzeća u krajnjoj liniji svodi na prodaju outputa i nabavku inputa, odnosno na sveukupne marketing aktivnosti.
- *Alokativna efikasnost* kao izraz efikasnosti organizovanja proizvodnje i razmene predstavlja izraz ukupne efikasnosti preduzeća koja u sebe uključuje i efekte efikasnosti i efekte efektivnosti.

Integracija efikasnosti i efektivnosti u jedinstveni izraz ukupne ekonomske efikasnosti je u funkciji merenja ukupnih efekata uspešnosti preduzeća. Kroz sagledavanje ukupnog efekta se omogućava efikasnije upravljanje ekonomijom preduzeća. Kvalitet ekonomije preduzeća, može da se oceni kroz sagledavanje odnosa između jedinstveno shvaćenog proizvoda, kao rezultata proizvodnje i jedinstveno shvaćenog društvenog rada unesenog u reprodukciju u cilju ostvarivanja tog rezultata.

Kvantitativni izraz kvaliteta ekonomije izražen je poslovним uspehom  $P_u$ , koji je sadržan u odnosima između rezultata reprodukcije (outputa) i ulaganja (inputa) u reprodukciju

$$P_u = R(O_u) / U(I_n)$$

Kvalitet ekonomije preduzeća, kao izraz stepena ekonomske uspešnosti u ostvariva-

nju ciljeva, istovremeno je i izraz uspešnosti u efektivnosti i efikasnosti preduzeća u poslovanju i razvoju. Saglasno sa konstatacijom da je ekonomsko značenje efektivnosti i efikasnosti, odnosno samo ekonomiske efikasnosti upravo u kvalitetu ekonomije sledi istovremeno zaključak da je i poslovni uspeh kvantitativni izraz efikasnosti i efektivnosti [2].

## MERENJE UKUPNOG POSLOVNOG USPEHA

Problematika merenja ukupnog poslovnog uspeha može se sagledati sa aspekta svrhe, suštine i teorijsko-metodoloških problema definisanja modela za merenje poslovnog uspeha.

Svrha merenja ukupnog poslovnog uspeha preduzeća su jasne informacije o stvarnoj ekonomskoj efikasnosti preduzeća kao i o realnim ekonomskim efektima novih investicija u konkretno preduzeće za koje su zainteresovani vlasnici preduzeća. Kontinuelno merenje poslovnog uspeha je realna pretpostavka za efikasnije upravljanje ekonomijom preduzeća.

U akcionarskim preduzećima u kojima je vlasništvo odvojeno od upravljanja merenje poslovnog uspeha omogućuje vlasnicima kontrolu menadžera koje su angažovali da upravljaju preduzećem.

Merenje ukupnog poslovnog uspeha obezbeđuje pored efikasnosti upravljanja i realniju raspodelu profita tzv. finansijskim grupacijama preduzeća, realnije sagledavanje stvarnih efekata eksternog rasta.

Merenje ukupnog poslovnog uspeha podstiče funkcionisanje berze, jer potencijalni investitori (akcionari) imaju relevantne informacije za svoje investicije.

Izražavanje poslovnog uspeha je i zakonski uslov bez koga preduzeće ne može da postoji. Iskazani rezultati poslužiće kao osnova za obračun i isplatu dividendi akcionarima.

Za merenje poslovnog uspeha, zainteresovani su vlasnici, država i menadžeri. Merenje poslovnog uspeha na kraju poslovnog perioda ili kontinuelno po potrebi je

neophodan uslov efikasnijeg menadžmenta, kao i adekvatnije zadovoljavanje interesa različitih stejkholdera.<sup>1</sup>

Suštinsko tumačenje ukazuje na to da je ukupni poslovni uspeh konkretnog preduzeća izraz ukupne ekonomске efikasnosti. To znači da izražava njegovu ukupnu alokativnu sposobnost kako kroz sposobnosti: za izbor i nabavku inputa, efikasno organizovanje proizvodnje kao transformacionog procesa tako i izbor i realizaciju proizvoda i usluga kao outputa preduzeća. Svi ekonomski efekti koji se pojавno manifestuju na inputima i na outputima konkretnog preduzeća izražavaju njegovu ukupnu ekonomsku efikasnost [1].

Poslovni uspeh postaje kvantitativno određen kada je izmeren i ocenjen odgovarajućim ekonomskim metodama uobičajenim u određene indikatore ili modele. Osnovni ekonomski kriterijum efikasnosti je značajno polazište izražavanja, praćenja, kontrole i usmeravanja odnosa između pojavnih oblika rezultata i ulaganja. Na strani rezultata mere se: obim proizvodnje, ukupan prihod, dohodak i dobitak, a utrošena radna snaga, ukupni troškovi i angažovani kapital na strani ulaganja.

$$P_u = R(Q; C; D; D_b) / U(L; T; S)$$

Ako se u okviru osnovnog cilja preduzeća posmatraju podciljevi kao: proizvodna, akumulativna i reproduktivna sposobnost navedena merila na strani rezultata i na strani ulaganja uobičavaju se u tradicionalno poznate indikatore kompleksa produktivnosti ( $P = Q / L$ ), ekonomičnosti ( $E = C / T$ ) i rentabilnosti ( $R = D(D_b) / S$ ) [4].

Izražavajući poslovni uspeh parcijalnim indikatorima kao merilima stanja ekonomije preduzeća iskazuje se efikasnost funkcionisanja proizvodno-finansijskog podsistema

<sup>1</sup> Strategijski konstituenti preduzeća su njegovi stejkholderi, odnosno vlasnici, kupci, kreditori, dobavljači i ostale grupe bez čije saradnje ne može da opstane.

preduzeća. Na taj način omoguće se kontrola i usmeravanje kvaliteta pojedinih podistema ekonomije ka jedinstvenom integralnom cilju ostvarivanja efikasnosti celog sistema preduzeća. Međutim pri iskazivanju i upravljanju dinamikom ukupnog poslovnog uspeha ispoljavaju se divergentnost i nedostaci parcijalnih indikatora i kompleksnost ove problematike. To je uslovljeno različitim intenzitetom i smerom kretanja samih elemenata rezultata i ulaganja pod uticajem pozitivnih ili negativnih dejstava u sklopu poslovnih aktivnosti.

Problem svodnog izražavanja i merenja ukupnog poslovnog uspeha savremena teorija i praksa rešava prihvatanjem dva stava [2]:

- prvi se bazira na korišćenju brojnih pojedinačnih indikatora, pri čemu je svodni izraz dat najčešće u vidu kvalitativne ocene, koja po pravilu nije objektivizirana po nekom osnovu,
- drugi zasnovan na pokušaju da se, uz brojne teškoće i ograničenja na koje nailazi savremena teorija i praksa, formuliše i koristi sintetički izraz poslovnog uspeha, u vidu, manje ili više integralnog, maksimalno moguće objektiviziranog modela koji, uz obavezne dopunske kvalitativne pokazatelje, agregatno iskazuje promenu ukupnog ekonomskog kvaliteta preduzeća.

Obuhvat i sadržaj, bilo seta indikatora, bilo integralnog modela ukupnog poslovnog uspeha, treba da, na osnovu bazičnog kriterijuma ekonomske efikasnosti, prvenstveno zadovolji informacionu, upravljačko-kontrolnu i motivacionu funkciju u poslovanju preduzeća [5].

### **TEORIJSKO-METODOLOŠKI PROBLEMI DEFINISANJA MODELAA ZA MERENJE POSLOVNOG USPEHA**

Prelazak sa velikog broja parcijalnih pokazatelja na jedan jedinstven pokazatelj ukupne efikasnosti zahteva rešavanje problema svođenja na zajednički imenitelj

za inpute i outpute preduzeća, kao i razvijanje kompleksnog poslovno-informacionog sistema u preduzeću razvijenog iz konkretnog modela za merenje poslovnog uspeha.

U konstituisanju modela za izražavanje ukupnog poslovnog uspeha posebnu pažnju zavređuje model *Ekonometar* kao originalna tvorevina S. Kukoleće [6], kojim se u dinamici evidentiraju i iskazuju sve veze i sve promene oblika rezultata i ulaganja, svedenih na jedinstvenu zajedničku meru – radni ekvivalent. Visok nivo apstrakcije i perfektnosti u koncipiranju i razradi modela poslovnog uspeha u globalu, te posebno prema faktorima uslovljenosti, nametnuli su utisak da je teško ili nemoguće ostvariti njegovu primenu. To važi naročito za period šesdesetih godina kada nije postojala podrška informacionih sistema u našim preduzećima. Takođe ta informaciona osnova, potrebna za merenje prema ovom modelu u maloj meri je povezana sa zvaničnim računovodstveno-finansijskim sistemom. Ovo je predstavljalo jednu od bitnih prepreka za značajniju primenu u praksi.

Vredni su naporci takođe domaćih teoričara (D. Grozdanović i N. Malenović) na konstituisanju modela *Merenje ukupne performanse poslovne uspešnosti* kojim se prevazilaze određena ograničenja izvornog modela i njegovih kasnijih modifikacija (takođe od strane pomenutih autora) posebno u pogledu korišćenja sistema finansijskog izveštavanja kao informacione osnove za proračun pojedinih elemenata [7].

Postojeći teorijski i praktični instrumenti kontrole i usmeravanja poslovanja, rasta i razvoja preduzeća ne omogućavaju sagledavanje realne slike stvarne efikasnosti savremenih preduzeća. Mnogi teorijski modeli, proizašli iz različitih teorija preduzeća, nisu mogli biti primenjeni za rešavanje konkretnih problema u praksi preduzeća. Tako su matematički metodi i modeli imali ograničene domete u primeni, služili su za rešavanje hipotetičkih slučajeva, a ne konkretnih problema u ekonomiji preduzeća.

Problem efikasnog poslovanja preduzeća se u menadžerskim teorijama formuliše kao problem određivanja maksimalne korisnosti menadžera, ali s obzirom da menadžeri ne poseduju neograničenu diskreciju i da svoje ciljeve mogu da ostvare uz uslove koje postavljaju vlasnici – akcionari, maksimiziranje funkcije korisnosti se javlja kao rezultat rešenja problema uslovljene maksimizacije. Sem dihotomije interesa vlasnika s jedne i menadžera s druge strane ne identifikuju se drugi značajni interesi. Pristup ciljevima preduzeća se tokom vremena menjao gde su usavršavane tehnike i metode ostvarivanja ciljeva ali su bazični ciljevi i njihova ekonomska sadržina marginalizovani.

Finansijski pokazatelji kao osnova tradicionalnih sistema merenja i kontrole poslovnog uspeha imaju svoje jasne kontrolne uloge omeđene određenim vremenskim periodima. Iz njih izvedeni setovi raznih indikatora, indeksa i racio brojeva, samo pokazuju kakav je rezultat poslovanja preduzeća u proteklom periodu i to ne izraženo kroz ukupan poslovni uspeh već prema parcijalnim iskazima pojedinih stanja i efekata.

Razvojem teorija koje se bave ekonomijom preduzeća stvaraju se prepostavke za usavršavanje modela za merenje poslovnog uspeha, za takvu kontrolu preduzeća i upravljanje njegovom ekonomijom da se pozitivne konsekvene potenciraju, a negativne smanje na najmanju meru uz zadovoljenje svih bitnih interesa koji se ispoljavaju u vezi sa njegovim poslovanjem, rastom i razvojem.

### **FINANSIJSKI POKAZATELJI KAO OSNOVA TRADICIONALNIH SISTEMA MERENJA I KONTROLE POSLOVNOG USPEHA**

Zajedničko za sve tradicionalne sisteme finansijske kontrole i merenja poslovnog uspeha je da se u celini zasivaju na podacima koji se mogu dobiti na osnovu računovodstvenog sistema. Davanje pred-

nosti korišćenju kvantitativnih računovodstvenih informacija obrazlaže se činjenicom da računovodstvo kao jedini integralni sistem kvantitativne analize preduzeća karakterišu integralnost obuhvata poslovno-finansijskih aktivnosti preduzeća, prednost numeričkog izraza i iz toga proizilazi vrednosni objektivizam. Takođe, prednost računovodstvenih informacija se manifestuje u njihovom svojstvu da različita stanja, tokove i relacije pretvoriti u jedan univerzalni, opšte prihvaćeni jedinstveni brojčani izraz.

Inače, integralni set finansijskih izveštaja većine preduzeća u međunarodnoj praksi čine bilans stanja<sup>2</sup> (izveštaj o finansijskom položaju) i bilans uspeha (račun dobitka i gubitka). Mada je vremenom sve više favorizovan, izveštaj o tokovima gotovine nije prihvaćen u svim zemljama.<sup>3</sup> I pored njihove baziranosti na istim poslovno-finansijskim transakcijama i univerzalnog finansijskog kvantifikovanja ovih transakcija, set finansijskih izveštaja kao objektivni hroničar preduzeća emituje različite informacije o njegovim aktivnostima za određeni period.

Osnovni informacioni sadržaj bilansa stanja (engl. Balance sheet) je knjigovodstvena vrednost preduzeća odnosno stanje aktive, obaveza i kapitala (neto vrednost aktive) na određeni dan.

Bilans uspeha (engl. Income statement) je poznat kao račun dobitka i gubitka (engl. P&L – Profit and Loss Account). Osnovni informacioni sadržaj bilansa uspeha je profitabilnost. Bilans uspeha prikazuje

<sup>2</sup> Jedna od ključnih izmena u revidiranom IAS1, objavljenom 2007. godine, odnosi se na zamenu naziva bilans stanja (Balance sheet) u izveštaj o finansijskom položaju preduzeća (Statement of financial position). Kao razlog ove terminološke promene navodi se isticanje funkcije ovog osnovnog finansijskog izveštaja.

<sup>3</sup> Prema prihvaćenim računovodstvenim standardima mala preduzeća u našoj zemlji su u obavezi da dostavljaju Agenciji za privredne registre (APR) osim bilansa stanja i bilansa uspeha i statistički aneks, a srednja i velika preduzeća izveštaj o tokovima gotovine i izveštaj o promenama na kapitalu.

informacije o prihodima, rashodima i neto dobitku/gubitku za određeni period. Međusobno konfrontirani svi prihodi i rashodi jednog konvencionalno usvojenog obračunskog perioda raščlanjeni i prikazani u skladu sa odgovarajućim principima i u odgovarajućoj izveštajnoj formi omogućavaju utvrđivanje rezultata dobitka kao pozitivne i gubitka kao negativne razlike, koja se na kraju obračunskog perioda obuhvataju u bilansu stanja kao povećanje i smanjenje (sopstvenog) kapitala. Ovakvo shvatnje bilansa uspeha ukazuje na postojanje sistematske i organske veze između bilansa stanja i bilansa uspeha, a ova činjenica ukazuje na to da se ovi finansijski izveštaji sa aspekta ocene efikasnosti poslovanja tretiraju kao komplementarni i međuzavisni proizvodi računovodstva [8].

Izveštaj o tokovima gotovina (engl. Statement of Cash Flows) pokazuje promet na računu gotovine preko priliva i odliva gotovine kao i generisan slobodan gotovinski tok u periodu. Izveštaj o tokovima gotovine pokazuje poslovne, finansijske i investicione prilive i odlive novčanih tokova preduzeća u toku izveštajnog perioda. Osnovna informacija za kontrolu koju izveštaj o tokovima gotovine nosi je likvidnost. Takođe, izveštaj o tokovima gotovine nosi informacije o mogućnostima stvaranja vrednosti ukoliko se izvrši diskontovanje slobodnog novčanog toka.

Pojedine pozicije finansijskih izveštaja, prikazane u apsolutnim vrednostima ne daju dovoljno informacija za upravljanje. Dovodenjem pojedinih pozicija bilansa stanja i bilansa uspeha i drugih izveštaja u odgovarajuće odnose dobijaju se racio brojevi. U procesu kontrole racio brojevi se porede sa prošlim rezultatima ili rezultatima konkurenčije. Dakle, racio brojevi se mogu koristiti za praćenje rezultata preduzeća tokom vremena ili za praćenje relativne pozicije preduzeća u odnosu na konkurente. U svakom slučaju ove relativne vrednosti

pružaju mnogo bogatije informacije u odnosu na analizu apsolutnih veličina (pozicije finansijskih izveštaja). Sve racio brojeve možemo klasifikovati u četiri velike grupe: pokazatelje likvidnosti, pokazatelje obrta (aktivnosti), pokazatelje solventnosti (finansijske strukture) i pokazatelje rentabilnosti (profitabilnosti) [9].

Pomenuti pokazatelji predstavljaju, zapravo, operativna merila performansi, tj. pokazatelje uspeha koji mere rezultate operativnih odluka. Očigledno je da su u efektima operativnih odluka sadržani i efekti strategijskih i taktičkih odluka [10].

Pored jednostavnih racio brojeva postoje i složeni racio brojevi koji nastaju kombinovanjem osnovnih racio brojeva, praćenjem bitnog dela poslovnog procesa ili specifičnih aspekata poslovanja. Po osnovu *DuPont* formule dolazi se do sintetičkog izraza rentabilnosti koji omogućava da se ustanovi promena kao i uzroci promene rentabilnosti, jer se ukupna rentabilnost, tj. prinos na ukupna sredstva posmatra kao rezultat uzajamnog delovanja, ili interakcije parcijalnih pokazatelja rentabilnosti [11].

Značaj finansijskih izveštaja, koji odražavaju poslovno-finansijske aktivnosti preduzeća kao celine, ogleda se u tome što analitička interpretacija podataka sadržanih u njima omogućava identifikovanje i praćenje ključnih finansijskih merila efikasnosti preduzeća. Pored ovih tradicionalnih merila u poslednje vreme se koriste i pokazatelji koji imaju svoje uporište u konceptu upravljanja zasnovanog na vrednosti. Jedan od najznačajnijih je dodata ekonomска vrednost (Economic Value Added – EVA). Danas se često koriste od strane ekonomskih analitičara i pokazatelji profit pre kamate i poreza (Earning Before Interest and Taxes – EBIT) i profit pre kamate, poreza, amortizacije i otpisa (Earning Before Interest, Taxes, Depreciation and Amortization – EBITDA).

## **REZULTATI SAVREMENE EKONOMSKE TEORIJE I PRAKSE U DEFINISANJU MODELA ZA MERENJE UKUPNOG POSLOVNOG USPEHA**

I pored nezamenljive uloge finansijskih merila potrebno je ukazati na njihovu nesavršenost i nepotpunost za potrebe validne analize i ocene efikasnosti. Primena tradicionalnih finansijskih merila pokazuje izvesne nedostatke i ograničenja koja se pre svega odnose na: prikazivanje događaja koji su se desili u prethodnom periodu, nepouzdanost baze poređenja za duži vremenski period, ne pridaju dovoljno važnosti poslovnom okruženju zanemarujući perspektivu potrošača i konkurenata. Problem tradicionalnih merila koja se baziraju na finansijskim indikatorima je da ona ne uzimaju u obzir neopipljivu vrednost sadržanu u znanju koja u velikoj meri može da uveća tržišnu vrednost preduzeća.

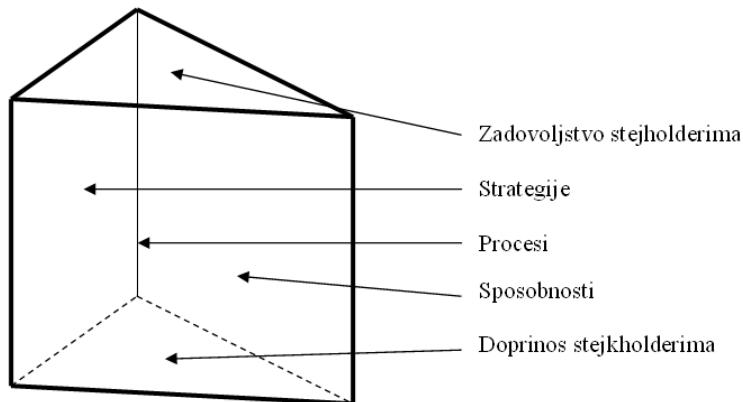
Promene u okruženju, globalizacija svetske privrede, izražena konkurenca, razvoj informacione tehnologije dovodi do promena u tradicionalnoj upravljačkoj aparaturi. Industrijsku ekonomiju koju karakteriše fizički opipljiva aktiva zamjenjuje nova ekonomija u kojoj najvredniji resurs postaje neopipljiva aktiva koja obuhvata odnose sa potrošačima, veštine zaposlenih i njihovo znanje, informacionu tehnologiju i organizacionu kulturu plodnu za inovacije, rešavanje problema i opšte unapređenje organizacije [12].

U uslovima razvijenog tržišta jedini održivi način za stvaranje vrednosti za vlasnike preduzeća je istovremeno ostvarivanje vrednosti i za njegove stejkholderere. Stejkholderi, dakle, imaju legitimne interese u obavljanju aktivnosti preduzeća, kao i određene zahteve i potrebe koje proizilaze

iz povezanosti u obavljanju određene aktivnosti. Pri tome, primarni (aktivni) stejkholderi imaju formalne, zvanične i ugovorne odnose sa preduzećem, dok se svi ostali mogu tretirati sekundarnim (pasivnim). Orientacija na stejkholdere podrazumeva da se u model poslovnog uspeha uključuju i pokazatelji uspešnosti u ostvarivanju pojedinačnih ciljeva svih stejkholdera kao i merenja ostvarivanja tih ciljeva, i jedno i drugo se izražavaju odgovarajućim indikatorima.

Jedna od najvažnijih uloga menadžmenta je da pronađe prihvatljiv balans između finansijske odgovornosti prema vlasnicima i strategijske odgovornosti prema ostalim stejkholderima. Menadžeri moraju poći od činjenice da je finansijska odgovornost preduslov za kasnije ispunjenje strategijske odgovornosti. Međutim, ovaj odnos nije jednosmeran. Viši kvalitet odnosa preduzeća sa stejkholderima kao što su potrošači, zaposleni, dobavljači, zajednica i dr. vodi boljim finansijskim performansama, a na kraju većoj vrednosti preduzeća i akcionarskog bogatstva [13].

Na prethodno navedenoj osnovi, a uvažavajući uzročno-posledične procese između samih stejkholdera formuliše se jedan od savremenih modela, tzv. **Model Prizma performansi (A. Neely)**, koji se smatra integralnim modelom, zato što objedinjuje elemente modela orijentisanih na stejkholdere i elemente procesno orijentisanih modela [5]. Model prizma performansi je prikazan na *slici 1*.



**Sl. 1. Prizma performansi kao model iskazivanja poslovnog uspeha (prema [14])**

Model Prizma performansi pruža pet različitih, ali povezanih pogleda, a time i izraza poslovnog uspeha preduzeće iskaznog setom indikatora diferenciranih u pet ključnih grupa kao odgovora na pitanja [14]:

- zadovoljstvo stejholderima (vrh prizme) – ko su ključni stejholderi i šta oni žele, ili šta im treba;
- strategije poslovanja (strana prizme) – koju strategiju preduzeće treba da primeni da bi zadovoljilo navedene želje ili potrebe;
- procesi (strana prizme) – koje kritične proceze preduzeće treba da primeni ka zadatom cilju, favorizujući tzv. procese koji dodaju vrednost na ulaganja i reprodukciju;
- sposobnost (strana prizme) – koje sposobnosti treba da imaju ključni stejholderi (zaposleni, kupci, društvena zajednica i vlasnici kapitala) u ostvarivanju primenjenih procesa, i konačno
- doprinos stejkhodera (dno prizme) – koje doprinose preduzeće može očekivati od stejkhodera, ako menadžment preduzeće podržava i razvija sposobnosti stejkhodera.

Upravljanje na bazi ovih merila podrazumeva definisanje ciljnih merila perfor-

mansi, upoređivanje ostvarenja sa ciljnim vrednostima, identifikovanje odstupanja i uzroka (faktora) odstupanja, i na kraju identifikovanje korektivnih upravljačkih akcija. Model se smatra vrednim zato što ističe i dimenziju merila sposobnosti (resursa). Glavni nedostatak je preveliki broj merila, koja se s obzirom na ograničeno vreme i mogućnosti pažnje menadžera ne mogu operativno koristiti.

Brojna literatura dokazuje da primena višedimenzionalnih sistema merenja performansi doprinosi efektivnosti istih (Domonović, 2013. prema: Malina, M. A. & Selto, F. H. 2001; Ittner, C.D. i dr. 2003; Davis, S. & Albright, T. 2004; Crabtree, A. D. & De Busk, G. K 2008; Van der Stede, W. A. i dr. 2006; Tung, A. i dr. 2011). Većina ovih studija ispitivala je efektivnost ovih sistema iz perspektiva doprinosa istih finansijskim rezultatima [15].

Analizirani modeli merenja poslovnog uspeha i drugi postojeći modeli koji su dokazali svoju primenljivost u praksi, od posebne su važnosti za unapređenje upravljačkog procesa. Kombinovanjem postojećih modela stvaraju se novi. Unapređeni sistemi merenja pružaju realne pretpostavke za efikasnije upravljanje uz odgovarajuću podršku informacionih sistema.

## ZAKLJUČAK

U ekonomskoj teoriji i poslovnoj praksi preduzeća vrlo je aktuelna i još uvek nedovoljno zaokružena problematika merenja ukupnog poslovnog uspeha. Sa upravljačkog aspekta dizajniranje kvalitetnog agregatnog merila zahteva prethodno rešavanje izuzetno kompleksnog problema svedenja na zajednički imenitelj različitih merila za inpute i outpute preduzeća kao i razvijanje i korišćenje odgovarajućeg informacionog sistema za proračun i praćenje tako projektovane agregatne veličine poslovnog uspeha. Ekonomска teorija u domaćoj literaturi je ponudila rešenje u vidu originalnog modela *Ekonometar*. Modelom *Ukupne performanse* poslovne uspešnosti nastoje se prevazići određena ograničenja izvornog modela i njegovih kasnijih modifikacija posebno u pogledu korišćenja sistema finansijskog izveštavanja kao informacione osnove za proračun pojedinih elemenata.

Finansijska merila imaju nezamenljivu ulogu u oceni poslovnog uspeha preduzeća, međutim, neophodno je ukazati na njihovu nesavršenost i nepotpunost za potrebe validne analize poslovnog uspeha. U savremenom periodu dolazi do izražaja nemogućnost finansijskih pokazatelja da obuhvate nematerijalne resurse preduzeća (intelektualni kapital) i stepen ostvarenja nefinansijskih ciljeva preduzeća (odnos sa kupcima, zaposlenima) koji su u savremenom periodu kritični za poslovni uspeh preduzeća.

Efektivan sistem merenja je onaj koji uključuje set finansijskih i nefinansijskih merila koja će omogućiti menadžerima da se uspešno suoče sa velikim brojem poslovnih aktivnosti i fokusiraju na ključne faktore poslovnog uspeha. Model *Prizma performansi* je jedan od takvih predloga.

U cilju realnog sagledavanja efektivnosti i efikasnosti preduzeća i dalje će se tragati za rešenjima na koja će odgovor moći da pruži nova paradigma preduzeća i njoj primereni modeli.

Razmatrana problematika u radu je korisna za upravljanje rudarskim preduzećima koja će putem veće odgovornosti i prema svojim stejkholderima stići atributе uspešnog preduzeća.

## LITERATURA

- [1] M. Nikolić, N. Malenović, D. Pokrajčić, B. Paunović, *Ekonomika preduzeća*, Ekonomski fakultet, Beograd, 2005, str. 122, 136, 475.
- [2] D. Grozdanović, *Osnovi ekonomike preduzeća*, Ekonomski fakultet, Kragujevac, 2003, str. 23, 25, 456.
- [3] M. Milisavljević, *Savremeni strategijski menadžment*, Megatrend Univerzitet primenjenih nauka, Beograd, 2005, str. 5.
- [4] Lj. Savić, *Uloga menadžmenta u unapređenju efektivnosti i efikasnosti preduzeća*, Doktorska disertacija, Megatrend univerzitet, Fakultet za poslovne studije, Beograd, 2010, str. 100.
- [5] M. Ratković Abramović, *Upravljanje dinamikom poslovnog uspeha*, Autorско izdanje, Beograd, 2005, str. 67,79.
- [6] S. Kukoleča, *Ekonometar*, Konsalting centar, 1994, Beograd.
- [7] B. Krstić, *Model merenja performansi ukupne poslovne uspešnosti preduzeća*, Ekonomski fakultet, Niš, 2007.
- [8] V. Domanović, J. Bogićević, *Mogućnosti primene Balanced Scorecard koncepta u Srbiji*, Naučno društvo ekonomista Srbije, Naučni skup Novi metodi menadžmenta i marketinga u podizanju konkurentnosti srpske privrede, Palić, 2011.
- [9] B. Pešalj, *Merenje performansi preduzeća*, Ekonomski fakultet, Beograd, 2006, str. 63.

- [10] D. Đuričin, S. Janošević, Đ. Kaličanin, Menadžment i strategija, Ekonomski fakultet, Beograd, 2013, str. 161.
- [11] D. Pokrajčić, Ekonomika preduzeća, Autorsko izdanje-Čigoja štampa, Beograd, 2002, str. 356.
- [12] R. Kaplan and D. Norton, Having Trouble With Your Strategy? Then Mapit!, Harvard Business Review, September-October, 2000, p. 4.
- [13] Đ. Kaličanin, Formulisanje i primena strategija stvaranja vrednosti, Doktorska disertacija, Ekonomski fakultet, Beograd, 2005, str. 15.
- [14] A. Neely, Business Performance Measurement, Cambridge University Press, 2003, p. 153.
- [15] V. Domanović, Efektivnost sistema merenja performansi u uslovima savremenog okruženja, Ekonomski horizonti, Ekonomski fakultet, Kragujevac, 2013.

*Slavica Miletic<sup>\*</sup>, Dejan Bogdanovic<sup>\*\*</sup>, Jane Paunkovic<sup>\*\*\*</sup>*

## **SELECTION OF THE OPTIMAL MODEL OF INTEGRATED SUSTAINABLE MANAGEMENT SYSTEM IN THE MINING COMPANIES<sup>\*\*\*\*</sup>**

### **Abstract**

*The multi-criteria analysis for the selection of the optimal model of integrated management system was conducted in this paper in order to improve the performance of mining companies. Integrated management system is the process of integrating of different management systems in a contemporary business as a requirement for each company in order to survive in the market. Modern companies that have implemented integrated management system work better, have arranged processes, improve its structure and culture for the management practice, and have continual improvements of all processes.*

*Mining companies are in a very difficult position in Serbia. Their business is specific because it is characterized by a high complexity, obsolete and complex organizational structure, inadequate management practices, everyday functioning and many other problems. In that context, authors are proposing four models of integrated management systems that could be applicable in mining companies in order to improve their performance. Also, the appropriate criteria for the selection of the optimal model are defined. AHP method is applied for the selection and ranking of the models of integrated management system. The obtained results give an optimal model of integrated management system that is applicable with the best results in terms of performance improvement and sustainability of mining companies in Serbia.*

**Keywords:** Integrated system management, Mining, AHP method

## **1 INTRODUCTION**

Implementation of the integrated management system (IMS), composed of different management systems, has received a lot of attention in recent years. The integrated management system is defined as a comprehensive management tool that links all elements of the business system in a unique and comprehensive system of processes management in the organization, in order to meet

the demands of stakeholders [1]. Today, there are more models of implementation of the IMS, and they were created based on the specific requirements of stakeholders and the companies themselves. Companies that have implemented the optimal model of IMS, have significant benefit such as: continuous improvement of processes, obtaining a unique quality of products and services,

---

<sup>\*</sup> *Mining and Metallurgy Institute Bor*

<sup>\*\*</sup> *University of Belgrade, Technical Faculty in Bor*

<sup>\*\*\*</sup> *Megatrend University, Faculty for Management Zajecar*

<sup>\*\*\*\*</sup> *This work in the results of the Project TR 34023 "Development the Technological Processes of Treatment the Non-standard Copper Concentrates to the Aim of Optimization the Emission of Polluting Materials and TR 37001 "The Effect of Mine Waste from RTB Bor and Pollution the Waterflows with a Proposal of Measures and Procedures for Reductid the Harmful Effect on the Environment", funded by the Ministry of Education, Science and Technological Development of the Republic of Serbia*

improving the organizational culture, the greater degree of satisfaction of stakeholders and others. The additional value of integrated management systems is that they are in accordance with a concept of sustainable development that institutes a balance between technological development necessary for economic prosperity and survival of the environment and society as a whole [2]. The key issue for the management of the mining companies is to align management system with different standards, and consequently how to make internal alignment of partial management systems in the company. Additionally, it is often difficult to take the advantage of already implemented system, and to choose the optimal model of IMS. Because of its specificity, the mining companies must first identify the requirements of stakeholders and subsequently select an optimal model of implementation of the IMS. Since all elements of standardized management systems are mutually compatible, it enables all partial management systems to form a single integrated management system (IMS) in which there are strong interconnections between the individual elements of the system [3]. Accordingly, the integrated management system is established through the commitment of the organization's management to implement the requirements of standards, raising awareness about the importance of planning processes and continuous improvement of business processes, thus creating the conditions for success.

The commercial success of mining companies precedes proper selection of the optimal model of IMS that will bring significant improvements in time, such as higher level of satisfaction of all stakeholders from the owner, manager, and to the end user of products and services, i.e. consumer or customer.

## 2 MODELS OF INTEGRATED MANAGEMENT SYSTEMS

There are a numerous models of IMS that have been successfully applied in commercial companies. Basic models of IMS

originally were the quality management system (ISO 9001) and the system of environmental management (ISO 14001), which later became integrated into the system management of health and safety (OHSAS 18001). Further development led to the creation of the new models of IMS that take into account the type of activity of certain companies, as well as all interested parties and stakeholders. The system that in itself integrates the requirements of several standards primarily aims to satisfy the demands of many stakeholders, because it is often the case that different stakeholders require different management systems, i.e. management systems compliant only with certain standards or [4].

This paper explores the practices of sustainable mining companies implementation the optimal model of IMS, analyzed by Analytical Hierarchy Process (AHP method). AHP is one of the multi-criteria decision-making methods for the selection of the best solution among several alternatives [5]. The advantage of this method is that it can simultaneously consider both financial and non-financial factors in the process of selecting the optimal model of IMS [6]. There are four alternatives that are discussed here (four models of IMS) which have been successfully applied in developed countries. These models are based on the fundamental principles and the process approach in the development of the integration process of management.

### 2.1 Wilkinson – Dale's model (alternative A1)

The integrated systems in Wilkinson – Dale's model consists of: the system of quality management (QMS), the system of environmental management (EMS) and the system of occupational health and safety (OHSAS) [7] – Figure 1. Differentiation and specificity of this model is that it includes an integrated culture and elements of TQM

model (Total Quality Management). Wilkinson – Dale's model of integration depends on the requirements and policies of any organization or interested party. Stakeholders may be managers (a successful business), employees themselves (wages, working conditions), suppliers (long term collaboration), customers (quality and price of a product), community (environment), owners (profits) and others.

This model can be implemented by any organization that takes the quality system, environmental protection system and the system of protection of health and safety at work as a priority in their business. Also, this model can be implemented by organizations that are involved in the activities of TQM works of continuous improvement.

Wilkinson and Dale model puts a great importance to sustainability culture in organizations that could lead to the creation of organizational culture which enhances the implementation of the integration system.

It is very important for the mining company that implements the IMS to select a model that takes into consideration a national culture, because it can improve the successful realization of this process. The importance of incorporation of national culture model is explained in a work of Geert Hofstede's [8]. Geert Hofstede is the most cited social science author - 123707 citations in Google Scholar [9]. Authors of this paper have considerable experience in research of organizational and national culture relations in Serbia [10, 11]).

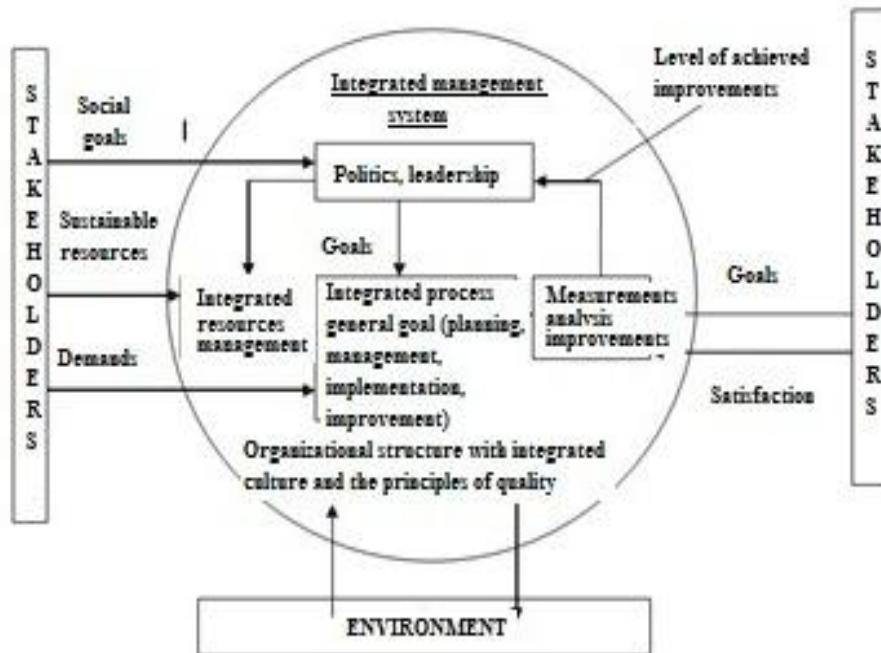
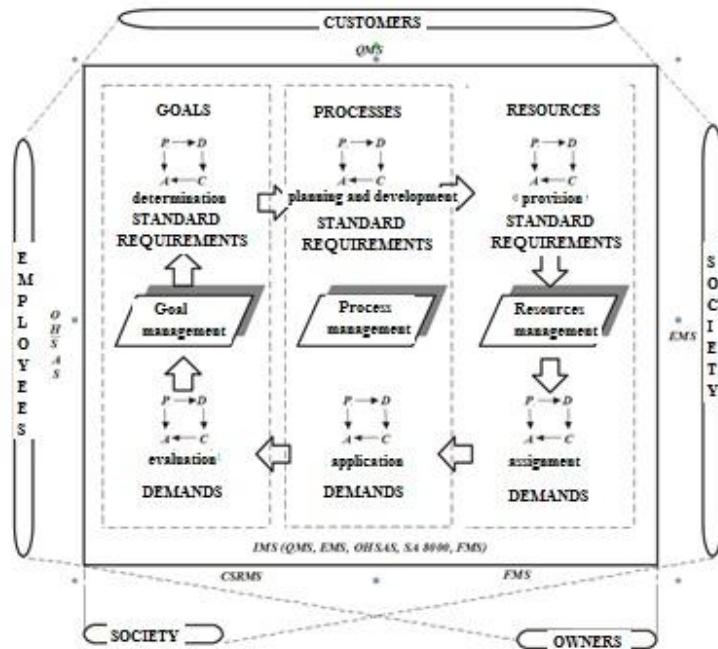


Figure 1 The extended Wilkinson – Dale's model of IMS [7]



**Figure 2** Karapetrovic's model [13]

## 2.2 Karapetrovic's model (alternative A2)

This model includes integration of five systems - QMS, EMS, OHSAS, the corporate social responsibility management system (CSRMS) and the financial management system (FMS). This means that the model includes the requirements of the standards and requirements of stakeholders. The model is based on a systematic approach and the PDCA cycle - plan, do, check and act - improve.

The focus of Karapetrovic's model, except for customers, is directed to the satisfaction of stakeholders of the community (environment), staff reductions (injury), management (reducing business risk), as well as other stakeholders [12, 13]. The implementation of management systems is done through management to objectives, process management and resource management -

Figure 2. Karapetrovic's model is compatible with the PDCA management system, because it considers all processes with a goal to their continual improvement and enhancements. These processes are: goals, planning and development processes, resourcing, scheduling, resource management, application in management processes and evaluation of management objectives.

This model is applicable to all industrial companies - manufacturing and service industries.

Characteristics of the company (type of activity, their specifics, size and demands of stakeholders) instigated development of the new standardized management system (MSS - Management Systems Standards) in order to meet their specific requirements and easier implementation of the IMS.

### 2.3 The process model (alternative A3)

In this model, each process, sub-process and activity has inputs – the demands of stakeholders, and outputs - satisfaction of stakeholders - Figure 3. During production the measurements, analysis and improvements are carried out by management supervision.

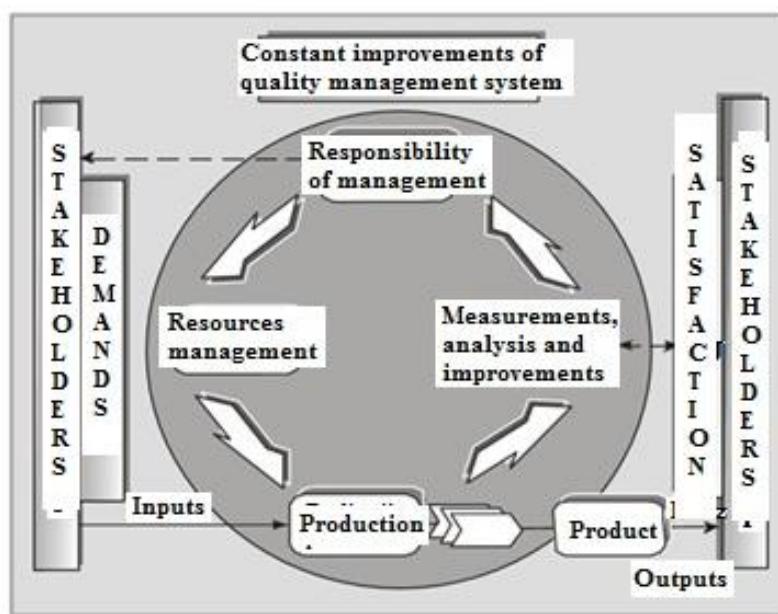
The management systems that are based on essentially procedural approach of ISO 9000 can be identified through integration strategy [14].

Specifics of the process model are reflected through the application of process approach, and it integrates the N systems: QMS, EMS, OHSAS and Food Safety Management System (HACCP). These standards have similarities within their structure, so the integration of the standards can be made on the basis of identical and specific requirements that must be resolved in the management process. That is why the process approach represents a new management approach. The essence of the standards for

management systems (ISO 9001, ISO 14001, OHSAS 18001 and ISO 22000) is precisely in the processes management.

The process model during its implementation requires knowledge about the organization, the requirements of stakeholders, defining management methodology, determining the necessary resources and the implementation of all procedures with continuous improvement and enhancement. During the implementation of the process model, person in charge, owner or manager of the process is responsible for the documentation, implementation requirements (products or services) and measurement of satisfaction of stakeholders. Also, employees and all participants in the process are responsible for the realization of the implementation of this process.

This model is highly represented in Serbia (in approximately 96 % of all companies).



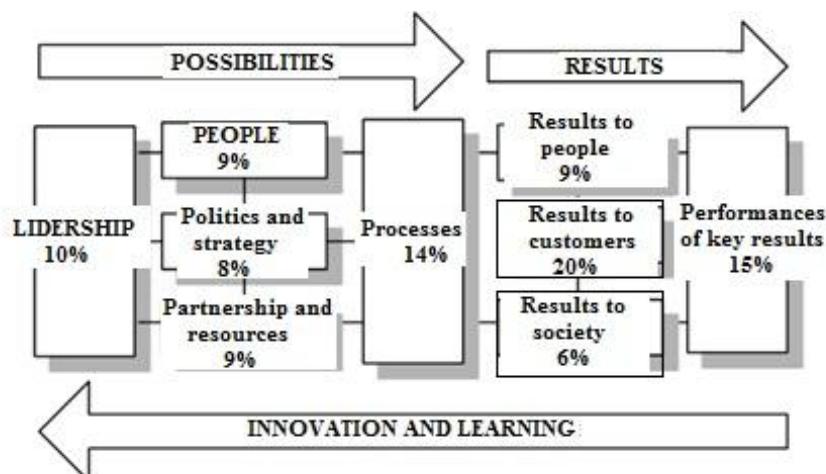
**Figure 3** Model of quality management system based on processes [14]

## 2.4 EFQM excellence model (alternative A4)

EFQM excellence model was created by the European Foundation for Quality Management in 1992 and promoted in 1999. The model is the basis for the European Quality Award for the following:

- large companies and
- small and medium companies

Unlike the others, this model is based on philosophy of Total Quality Management (TQM) and on two systems-integration (interoperability), such as quality management system and environmental management system (EFQM, 1998, EFQM, 2002) – Figure 4.



**Figure 4** EFQM excellence model [15]

This model has nine criteria where five are related to opportunities that show what the company does, while others refer to results. The results show the extent to which the organization uses opportunities.

The EFQM excellence model is applicable in companies whose requirements are such that they can develop their own approaches to achieving excellence. Within this model, there are a few basic concepts that are required for its implementation, namely:

- orientation to results, where results show excellence that are satisfaction of stakeholders;

- focus on customers, where the excellence is creating a stable customer;
- leadership and consistency determination, where is the excellence in leadership with a persistent feature;
- process and facts management, where is the excellence management company on the basis of processes and facts;
- inclusion of employees and their development, where is the excellence in employees motivation to increase contributions;
- improvement, innovation and continuous education, where the excellence is in innovation to create the

- possibility for more sophisticated operations;
- development of partnership, where excellence is manifested through the development and maintenance of partnerships with the increasing value;
- social responsibility, where excellence is reflected in overcoming some minimum obligations in the company and where the company aims to more responsible understanding of the demands of society.

The criteria for achieving the business excellence are: leadership, people, policy and strategy, partnership and resources, processes, results to customers and society, and finally results that make the satisfaction of all stakeholders.

Common features of the EFQM model, the process model, Karapetrovic's model and Wilkinson - Dale's model are: systemic approach, continuous improvement, satisfying demands of all stakeholders, reducing the extensive documentation and that they are applicable in the all types of organizations including mining companies.

### **3 DEFINING THE CRITERIA FOR SELECTION OF THE OPTIMAL MODEL OF IMS**

The criteria include the most important characteristics for the selection of the optimal model of implementation of the IMS in mining companies, namely:

**The cost of implementation of the IMS (criterion C1)** is a very important factor for the choice of an optimal model of IMS. The cost of implementation is determined for each proposed model of IMS in mining companies and influence is proportional to the obtained results.

**The expected effects of the IMS (criterion C2)** is a very important factor that has a major influence in selecting process of the optimal model of implementation of IMS. By implementation of optimal model of IMS, mining companies should make signi-

ficant improvements, such as building a model of organizational culture aligned with national culture, better implementation of its policies and strategies, greater employee satisfaction, injuries reduction at work, constant improvement of resources (material, financial and human), continuous improvement of business processes, improvements of corporate governance, satisfied external and internal customers, a better relationship to society, improving environmental protection, operations according to all the rules and regulations, the ability of business to the global market, the advantage in participating in the tender, cost reduction, etc.

**The time required for implementation of the IMS (criterion C3)** is also a very important factor that significantly influences the choice of optimal method of IMS. For example, if the implementation takes longer period than expected, some of the interested party will not met the requirements, which implies that their dissatisfaction reflects on the others, so that all can led to bad reputation of mining company within the community. Some of these models of IMS demand a shorter implementation period which can be very important for mining companies.

**The applicability of the model (criterion C4)** is a criterion that indicates the degree of implementation possibilities of a particular model of IMS in mining companies. Some models are easier to implement and others more difficult. The aim is that mining companies choose the model that is not difficult to implement and that it will bring many long-term benefits to them. In addition, mining companies must take into account many factors, such as their own specificities, equipment condition, the structure of labor, management of the companies and others.

### **4 AHP METHOD**

AHP is a quantitative technique that allows the structuring of complex decision problems with multiple criteria and provides

an objective methodology for a wide range of decisions.

AHP is based on decomposition the complex decision problems in multi-dimensional hierarchical structure of objectives, criteria and alternatives. After that, impact assessment of criteria is done. Then comparison of the alternatives in relation to each criterion is made, and final ranking of alternatives is obtained.

Assessment of the relative impact of each criterion and comparison of alternatives in relation to the criteria is performed by matrix of comparison. These include: the formation of matrix of comparisons at each level of the hierarchy, starting from the second level down; calculation of weight coefficients for each element of the hierarchy and the assessment of the degree of consistency in order to check the consistency of the entire process.

According to that, a set of alternatives {A1, A2, ..., An} is defined, as well as a set of criteria weight coefficients {w1, w2, ..., wn}.

Comparison of criteria and alternatives is made on the basis of the scale with scores from 1 to 9 – Table 1.

**Table 1** Scale of comparison of decision elements

Dominance	
description	Value
Equal	1
Weak dominance	3
Strong dominance	5
Very strong dominance	7
Absolutely dominance	9
2, 4, 6, 8 are intermediate values	

The result of the comparison of criteria is the matrix that has the following form:

$$W = \begin{bmatrix} w_i \\ \diagdown w_j \end{bmatrix} = \begin{bmatrix} w_i / w_1 & w_i / w_2 & \dots & w_i / w_n \\ w_2 / w_1 & w_2 / w_2 & \dots & w_2 / w_n \\ \dots & \dots & \dots & \dots \\ w_n / w_1 & w_n / w_2 & \dots & w_n / w_n \end{bmatrix}$$

After that, the comparison of pairs of alternative is performed in respect to each criterion, to give the matrix A in which a comparison element  $a_{ij}$  represents the ratio of the weight of the coefficient  $A_i$  alternative compared to the alternative of  $A_j$ .

$$A = \begin{bmatrix} a_{11} & a_{12} & \dots & a_{1n} \\ a_{21} & a_{22} & \dots & a_{2n} \\ \dots & \dots & \dots & \dots \\ a_{n1} & a_{n2} & \dots & a_{nn} \end{bmatrix}$$

The elements  $A_{ij}$  represent the relationship between the weight coefficients  $w_i / w_j$  where  $w$  is the weight vector of each alternative.

The matrix has a reciprocal properties, in which the  $a_{ji} = 1/a_{ij}$ .

After the comparison, weight coefficients are calculated and vector of coefficients is obtained  $w = [w_1, w_2, \dots, w_n]$  which is calculated on the basis of Saati procedure in two steps.

First, the matrix of pairs comparison  $A = [a_{ij}]_{n \times n}$  is normalized, then weights are calculated.

The normalization is performed by the following equation:

$$a_{ij}^* = a_{ij} / \sum_{j=1}^n a_{ij} \quad (1)$$

for all  $j = 1, 2, \dots, n$ .

Weight coefficients are calculated by the following equation:

$$w_i = \sum_{j=1}^n a_{ij}^* / n \quad (2)$$

for all  $j = 1, 2, \dots, n$ .

After the comparison, the Consistency Ratio is checked. Consistency Ratio should have a value lower than 0.1. Otherwise, they must reconsider the values that are entered into a matrix of comparison.

Consistency Ratio is calculated as follows:

$$CI = \frac{\lambda_{\max} - n}{n - 1} \quad (3)$$

where  $\lambda_{\max}$  is an important parameter of the AHP method and it is used as a reference index for displaying information when calculating the Consistency Ratio (CR). CR is calculated as follows:

$$CR = CI/RI \quad (4)$$

where  $RI$  represents the random consistency index obtained randomly from comparison matrices.

The final ranking of alternatives is made by synthesis of results from all levels.

## 5 RESULTS OF THE SELECTION OF THE OPTIMAL MODEL OF IMS

After defining the criteria and models of IMS (alternatives) it is performed their evaluation and ranking by AHP method. Criterium DecisionPlus software was used for calculation.

The first step is defining the multi-dimensional hierarchical structure of objectives, criteria and alternatives - Figure 5.

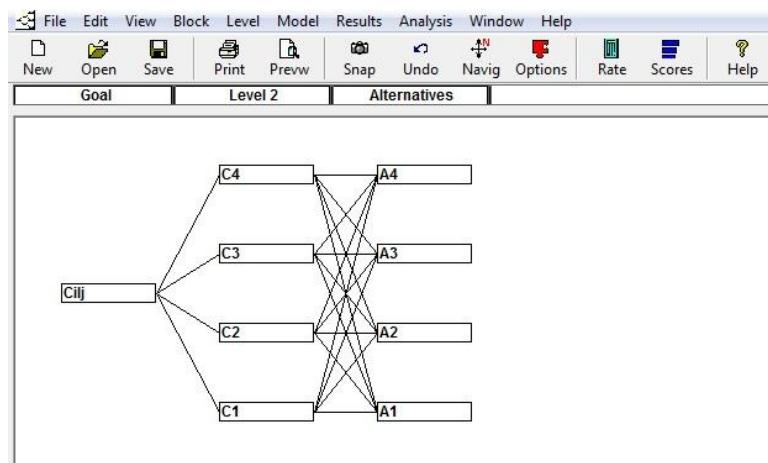
Thereafter, the weight coefficient of criteria is calculated according to the scale of comparison given in Table 1. The comparison results are shown in Table 2 and Table 3.

**Table 2** Definition of weight coefficient of criteria

Criteria	C1	C2	C3	C4
C1	1	1/5	5	2
C2		1	8	5
C3			1	1/5
C4				1

**Table 3** Results of weight coefficients criteria

Criteria	C1	C2	C3	C4
Weight coefficients	0.193	0.624	0.045	0.138
Consistency Ratio	0.084<0.1			



**Figure 5** Decision-making hierarchy (Criterium DecisionPlus software)

In the next step, a comparison of models of IMS (alternatives) is done with regard to all four criteria defined - Table 4-7.

**Table 4** Comparison of alternatives with regard to a criterion C1

Alternatives	A1	A2	A3	A4
A1	1	2	1	1
A2		1	2	1/2
A3			1	1/3
A4				1
Consistency Ratio	0.077<0.1			

**Table 5** Comparison of alternatives with regard to a criterion C2

Alternatives	A1	A2	A3	A4
A1	1	1/3	1/5	1
A2		1	1/3	3
A3			1	7
A4				1
Consistency Ratio	0.012<0.1			

**Table 6** Comparison of alternatives with regard to a criterion C3

Alternatives	A1	A2	A3	A4
A1	1	3	5	1
A2		1	3	1/3
A3			1	1/5
A4				1
Consistency Ratio	0.016<0.1			

**Table 7** Comparison of alternatives with regard to a criterion C4

Alternatives	A1	A2	A3	A4
A1	1	1/3	1/3	1
A2		1	1	3
A3			1	3
A4				1
Consistency Ratio	0.00<0.1			

Finally, after the all calculations, the results of ranking are obtained - Table 8. The best solution is alternative A3 (The process model of IMS). In the second place is an

alternative A2 (Karapetrovic's model), in the third place is an alternative A4 (EFQM excellence model) and on the last place is an alternative A1 (Wilkinson-Dale's model).

**Table 8** The final rank of models of IMS

No.	Model of IMS	Result
1.	A3 (The process model of IMS)	0.449
2.	A2 (Karapetrovic's model)	0.246
3.	A4 (EFQM excellence model)	0.157
4.	A1 (Wilkinson-Dale's model)	0.148

## 6 THE ANALYSIS OF RESULTS

Analysis includes criteria and their impact on the ranking of the models of IMS, as well as the models of IMS itself.

When analyzing the criteria, the most important are their weights, because that is their measure of influence on the result of ranking of alternatives or models of IMS. Table 3. shows that the criterion C2 (the expected effects of the IMS) has the greatest impact on the result of the ranking because its weight coefficient is 0.624. This means that it affects with 62.4% for a decision with regard to other criteria. Also, this shows that in the selection of the optimal model of IMS, the most important is what will the mining companies get after its implementation, i.e. which the positive effects companies will achieve.

In the second place is the criterion C1 (the cost of implementation of the IMS), which affects 19.3% on the result of ranking. This shows that the costs of implementation of the optimal model of IMS is very important for mining companies, considering that they are in a difficult financial situation.

In the third place is criterion C4 (the applicability of the model), which affects with 13.8% on the process. This shows that it is very important to the mining companies the suitable level of a particular model of IMS for use in conditions in which they operate. Implementation of the IMS requires forming a team for implementation, the acquisition of new knowledge, application of new methods, management and procedures, overcoming resistance, implementation and control of the obtained results.

Finally, the least influential is the criterion C3 (the time required for implementation of the IMS) with weight ratio of 0.045. This shows that the time required for the implementation of IMS, although important, are in the background compared to other effects that are expected from this system.

The analysis of the final ranking of alternatives (model IMS) starts from the optimal (best) alternative. It is the alternative A3 (the process model of IMS) which has the highest value of the results of 0.449. The reason

is that this model focuses precisely on that what is the strongest feature of mining companies – the existence and continuous performing of very complex and many processes during the work. Processes are the place where most can be done, which is the goal of this model. On the other hand, this model of IMS integrates various systems such as QMS, EMS, OHSAS, and all employees of the companies. All this enables significantly improvements of performances of mining companies in most or all areas of their functioning.

The second highest ranking of alternative is A2 (Karapetrovic's model). It discusses the integration of five systems - QMS, EMS, OHSAS, corporate social responsibility management system (CSRMS) and financial management system (FMS) and it is turned towards the continuous improvement process. Unlike the previous model, it is more complex, more demanding and less suitable for mining companies in our country.

In third place is the alternative A4 (EFQM excellence model), while in the last place is alternative A1 (Wilkinson –Dale's model). The difference in the results between these models is small. Their disadvantage compared to the previous two models of IM is that they to a lesser extent consider the processes, then they are less adapted to mining companies and therefore, they can provide the lower results. The good side of these models is that they integrate into their structures the environmental management system, which is very important for mining companies.

## CONCLUSION

Authors have conducted the multiple criteria decision-making method in order to select the optimal model of Integrated Management System (IMS) in mining companies in Serbia. Selection of the optimal model of IMS is one of the most important strategic decisions of mining companies. Four models of IMS are analyzed: Wilkinson Dale's model (alternative A1), Karapetro-

vic's model (alternative A2), the process model (alternative A3) and the EFQM excellence model (alternative A4). Four criteria for the ranking are also considered : the cost of implementation of the IMS (criterion C1), the expected effects of the IMS (criterion C2), the time required for implementation of the IMS (criterion C3) and the applicability of the model (criterion 4).

Ranking of models of IMS was performed by the AHP method for multiple criteria decision making. In this method, weight coefficient of criteria for ranking is calculated first, then the proposed models of IMS are assessed and their full ranking is done.

The applied method for multiple criteria analysis –AHP, can be of great help to decision-makers because it allows easy and high quality analysis of influential factors and parameters. The best model of IMS for mining companies in Serbia chosen based on the results of AHP method was the process model (alternative A3). The most influential criteria for a complete ranking of alternatives (IMS models) are the expected effects of the IMS (criterion C2) and the cost of implementation of the IMS (criterion C1).

## REFERENCES

- [1] Djekic, V. et al., Importance of Interoperability Information and Information Systems in the Implementation of the Model IMS. International Scientific Conference Managament, Mladenovac, Serbia (2012) 171-175;
- [2] Heleta M., Quality Management, Singidunum University, Belgrade, Serbia (2008) 5;
- [3] Brzakovic M., Interoperability and Information Security in Organizations of Strategic Importance in Emergency Situations-Doctoral Dissertation, Faculty of Security, Belgrade, Serbia (2009);
- [4] Volanovic S., The Development of a General Model for the Implementation of the Integrated Management System Based on Risk Assessment Processes in Organizations, Doctoral Dissertation, Faculty of Technical Sciences, Novi Sad, Serbia (2014);
- [5] Saaty T.L., The Analytical Hierarchy Process, New York: McGraw-Hill (1980);
- [6] Bogdanovic D. et al., Selection the Optimum Method of Rehabilitation the Degraded Ore as around the Bor River Downstream from the Flotation Tailing Dump Bor. Journal of Mining and Metallurgy Engineering Bor, 4 (2014) 137-146;
- [7] Wilkinson G., Dale B., Integrated Management Systems: a Model Based on Total Quality Approach, Managing Service Quality, 11(5) (2001) 318-330;
- [8] Hofstede G. H., Culture's Consequences: Comparing Values, Behaviors, Institutions and Organizations Across nations. Ed. Geert Hofstede. Sage (2001);
- [9] <https://scholar.google.com/citations?user=Q2V0P6oAAAAJ&hl=en&oi=ao> (accessed 13.05.2015)
- [10] Paunkovic J., Educational Programs for Sustainable Societies Using Cross-Cultural Management Method, Global Sustainable Communities Handbook: Green Design Technologies and Economics (2014): 387- Butterworth Heinemann imprint of Elsevier, Elsevier Copyright © 2014;
- [11] Paunkovic J., Zikic S., Cvetkovic A., Sustainable Utilization of Health Care Technologies is Influenced by Organizational and Cultural Factors – A Case Study. Advances in Biomedicine and Health Science, (2013) 57;
- [12] Karapetrovic S., Measuring of Integrated Management Systems, Measuring Business Excellence, 7(1) (2003) 4-13;
- [13] Karapetrovic S., Jonker J., Integration of Standardized Management Systems: Searching for a Recipe and Ingredients, Total Quality Management, 14(04) (2003) 451-459;
- [14] Petrovic M., The Process Approach to Integrated Management, 33. National Conference on Quality: Quality Festival, AQS and Quality Centre, Kragujevac, Serbia (2008);
- [15] European Foundation for Quality Management (EFQM), EFQM Model for Business.

*Slavica Miletić\*, Dejan Bogdanović\*\*, Jane Paunković\*\*\**

## **IZBOR OPTIMALNOG MODELA INTEGRISANOG ODRŽIVOG SISTEMA MENADŽMENTA U RUDARSKIM KOMPANIJAMA \*\*\***

### ***Izvod***

*U radu je primenjena multikriterijumska analiza za izbor optimalnog modela integrisanog sistema menadžmenta u cilju poboljšanja performansi rudarskih kompanija. Integrисani sistem menadžmenta koji predstavlja proces integracije različitih sistema menadžmenta u savremenom poslovanju su postala obaveza svake kompanije radi opstanka na tržištu. Savremene kompanije koje su implementirale integrisani sistem menadžmenta bolje funkcionišu, imaju uređene procese, poboljšavaju svoju strukturu i kulturu radi izvršenja aktivnosti upravljanja i stalnog unapređenjasnih procesa.*

*Rudarske kompanije u našoj zemlji se nalaze u vrlo teškoj situaciji. Njihovo poslovanje je vrlo specifično, jer se one karakterišu velikom složenošću, zastarem i kompleksnim organizacionim strukturama, neodgovarajućim načinom upravljanja, rada, funkcionisanja i dr. Polazeći od toga, u ovom radu su predložena četiri modela integrisanog sistema menadžmenta koji su primenljivi u rudarskim kompanijama, a u cilju poboljšanja njihovih performansi. Takođe, definisani su odgovarajući kriterijumi za izbor optimalnog modela. Za izbor i rangiranje modela integrisanog sistema menadžmenta je primenjena AHP metoda. Dobijeni rezultat daje optimalni model integrisanog sistema menadžmenta koji je primenljiv i koji može da ostvari najbolje rezultate u cilju poboljšanja performansi rudarskih kompanija u našoj zemlji.*

***Ključne reči:*** integrisani sistem menadžmenta, rudarstvo, AHP metoda

### **1. UVOD**

U zadnje vreme se velika pažnja poklanja implementiranju Integrisanog sistema menadžmenta (ISM) koji je sastavljen od različitih sistema menadžmenta. Integrисani sistem menadžmenta se definiše kao sveobuhvatni alat menadžmenta koji povezuje sve elemente poslovnog sistema u jedinstven i celovit sistem upravljanja procesima u organizaciji a radi zadovoljavanja zahteva

zainteresovanih strana [1]. Danas postoji više modela implementacije ISM-a koji su nastali na osnovu specifičnih zahteva stejkholdera i samih kompanija. Kompanije koje su implementirale za njih optimalni model ISM-a imaju značajne koristi od toga, kao što su: stalno poboljšanje procesa, dobijanje jedinstvenog kvaliteta proizvoda i usluga, poboljšanje organizacione kulture,

\* Institut za rudarstvo i metalurgiju Bor

\*\* Univerzitet u Beogradu-Tehnički Fakultet u Boru

\*\*\* Megatrend Univerzitet-Fakultet za menadžment Zaječar

\*\*\*\* Ovaj rad je proistekao kao rezultat projekta TR34023 "Razvoj tehnoloških procesa prerade nestandardnih koncentrata bakra u cilju optimizacije emisije zagadjujućih materija" finansiranog od strane Ministarstva prosvete, nauke i tehnološkog razvoja Republike Srbije

veći stepen zadovoljstva zainteresovanih strana i dr. Kvalitet predstavlja koncept za održivi razvoj koji uspostavlja bilans između tehnološkog razvoja neophodnog za ekonomski prosperitet i opstanka životne sredine i društva u celini [2]. Ključna pitanja za menadžment rudarskih kompanijas su kako uskladiti sistem menadžmenta sa različitim standardima, zatim kako izvršiti međusobno interno uskladištanje parcijalnih sistema menadžmenta kompanije, kako iskoristiti već implementirani sistem i nakraju, kako izabrati optimalni model ISM-a. Rudarske kompanije zbog svoje specifičnosti moraju prvo da identifikuju zahteve zainteresovanih strana, a onda, na osnovu toga da dođu do optimalnog modela implementacije ISM-a. Pošto su svi elementi standardizovanih sistema menadžmenta međusobno kompatibilni, to omogućuje da svi parcijalni sistemi menadžmenta čine jedinstveni integrisani menadžment sistem (ISM) u kom postoje jake međusobne veze između pojedinih elemenata sistema [3]. Shodno tome, sistem integrisanog menadžmenta se uspostavlja kroz opredeljenost menadžmenta organizacije za implementaciju zahteva standarda, širenje svesti o značaju uređenja procesa i stalnog poboljšanja poslovnih procesa čime se stvaraju uslovi za uspeh.

Poslovnom uspehu rudarskih kompanija prethodi pravilan izbor optimalnog modela ISM-a koji će tokom vremena doneti značajna poboljšanja, kao što su veći stepen zadovoljstva svih zainteresovanih strana od vlasnika, menadžera, pa do krajnjeg korisnika proizvoda i usluga, odnosno potrošača ili kupca.

## 2. MODELI INTEGRISANOG SISTEMA MENADŽMENTA

Danas postoji veliki broj modela ISM-a koji su uspešno primenjeni u poslovnim kompanijama. Osnovni modeli ISM-a su

prvobitno bili sistem menadžmenta kvaliteta (standard ISO 9001) i sistem upravljanja zaštitom životne sredine (standard ISO 14001), da bi kasnije došlo do integracije i sistema upravljanja zdravljem i bezbednošću na radu (standard OHSAS 18001). Daljim razvojem se došlo do stvaranja novih modela ISM-a koji uzimaju u obzir vrstu delatnosti određene kompanije, kao i sve zainteresovane strane ili stejkholdere. Sistem koji u sebe integrira zahteve više standarda prvenstveno obezbeđuje zadovoljenje zahteva više zainteresovanih strana zato što je čest slučaj da različite zainteresovane strane zahtevaju različite sisteme upravljanja, tj. sisteme upravljanja usaglašene samo sa određenim standardom ili standardima [4].

U ovom radu se direktno obrađuje održive rudarske kompanije sa aspekta implementacije optimalnog modela ISM-a pomoću Analitičko Higerarhijskog Procesa (AHP metoda). AHP je jedna od metoda višekriterijskog odlučivanja za donošenje odluka pri izboru najpovoljnijeg rešenja između više alternativa [5]. Prednost ove metode je u tome što ona može istovremeno da razmatra i finansijske i nefinansijske faktoare pri postupku izbora optimalnog modela ISM-a [6]. Kao alternative su ovde razmatrana četiri modela IMS-a koji su uspešno primenjeni u razvijenim zemljama. Ovi modeli su zasnovani na osnovnim postavkama i procesnom pristupu tako da se iz tog razvija proces integracije menadžmenta.

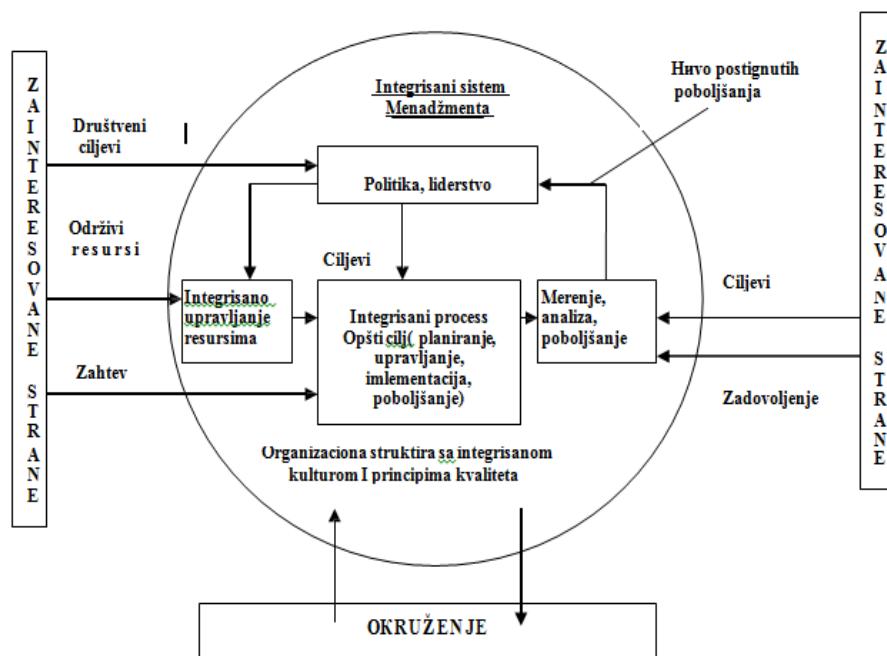
### 2.1. Wilkinson-Dale-ov model (Alternativa A1)

Sistemi integracija kod Wilkinson – Dale-ovog modela su: sistem menadžmenta za kvalitet (QMS), sistem menadžmenta zaštite životne sredine (EMS) i sistem menadžmenta zaštitom zdravlja i bezbednosti na radu (OHSAS) [7] - slika 1. Diferencijacija i specifičnost ovog modela je u tome što on

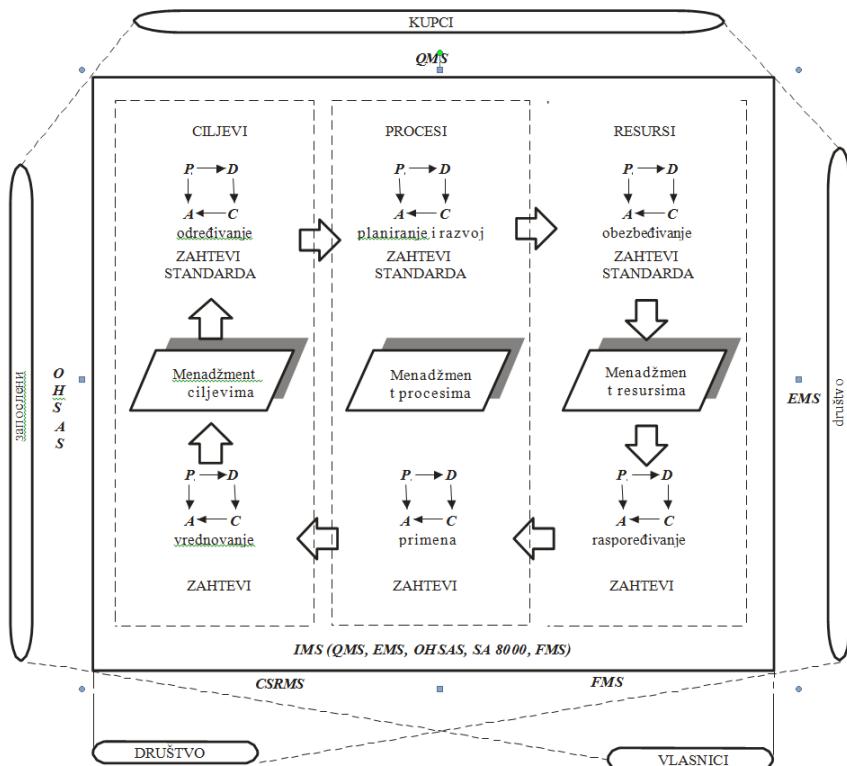
uključuje integriranu kulturu i elemente modela TQM-a (Total Quality Management). Wilkinson – Dale-ov model integracije zavisi od zahteva i politike svake organizacije, odnosno od zainteresovanih strana. Zainteresovane strane mogu biti menadžeri (uspešno poslovanje), sami zaposleni (zarađe, uslovi rada), dobavljači (dugoročna saradnja), kupci (kvalitet i cena proizvoda), društvena zajednica (životna sredina), vlasnici (profit) i dr. Ovaj model može da implementira svaka organizacija koja uzima sistem kvaliteta, sistem zaštite životne sredine i sistem zaštite zdravlja i bezbednost na radu kao prioritet u svom poslovanju. Takođe, ovaj model može da implementiraju i organizacije koje su uključene u aktivnosti TQM-a radi kontinualnih poboljšavanja.

Wilkinson i Dale u ovom modelu daju veliki značaj održivoj kulturi za integraciju kako bi moglo doći do stvaranja kulturnih organizacija što pomaže brzom implementiraju samog sistema integracije.

Za rudarsku kompaniju koja implementira ISM je jako bitno da ima ugrađen model "nacionalne kulture", jer to može dovesti do uspešne realizacije ovog procesa. Koliko je značajan i relevantan odnos organizacione i nacionalne kulture govori podatak o citiranosti Hofstedovih radova [8]. On je najcitaniji autor iz oblasti društvenih nauka (123707 citata - Google Scholar [9]). Autori ovog rada su objavili rezultate svojih istraživanja o povezanosti organizacione i nacionalne kulture u Srbiji u više oblasti [10, 11].



Sl. 1. Prošireni Wilkinson – Dale model ISM-a [13]



Sl. 2. Model IMS – a Karapetrovića

## 2.2. Model Karapetrovića (Alternativa A2)

Kod ovog modela su uključena pet sistema integracije – QMS, EMS, OHSAS, korporacijski menadžment sistem socijalne odgovornosti (CSRMS) i finansijski sistem menadžmenta (FMS). To znači da su uključeni zahtevi standarda i zahtevi zainteresovanih strana. Model se zasniva na sistematskom pristupu i ciklusu PDCA – planiraj, uradi, proveri i deluj – unapredi.

Kod modela Karapetrovića, osim kupaca, fokus je usmeren i na zadovoljenje interesne grupe društvene zajednice (zaštitu životne sredine), zaposlenih (smanjenje povreda na radu), menadžmenta (smanjenje rizika poslovanja), kao i drugih zaintereso-

vanih strana [9, 10]. Realizacija menadžment sistema se vrši kroz upravljanje prema ciljevima, upravljanje procesima i upravljanje resursima – slika 2. Model Karapetrovića je kompatabilan sa PDCA pristupom sistema menadžmenta, jer on razmatra sve procese sa ciljem njihovog stalnog unapređenja i poboljšanja. Ti procesi su: određivanje ciljeva, planiranje i razvoj procesa, obezbeđivanje resursa, raspoređivanje menadžment resursa, primena u menadžment procesima i vrednovanje menadžment ciljeva.

Ovaj model je primenljiv za sve industrijske kompanije – proizvodne i uslužne delatnosti.

Karakteristike kompanija (vrste delatnosti kompanija, njihove specifičnosti, veličine i zahteva interesnih grupa) su uslovile razvoj novih standardizovanih menadžment sistema (MSS – Management Systems Standards) za zadovoljenje njihovih specifičnih zahteva i lakšeg implementiranja ISM-a.

### 2.3. Procesni model (Alternativa A3)

Kod procesnog modela svaki od procesa, podprocesa i aktivnosti imaju ulaze, a to su zahtevi stejkholdera i izlaze – zadovoljstvo stejkholdera –slika 3. U toku realizacije proizvoda vrše se merenja, analize i poboljšanja uz odgovornost rukovodstva sa odgovarajućim resursima, stalnim poboljšanjem sistema menadžmenta i dr.

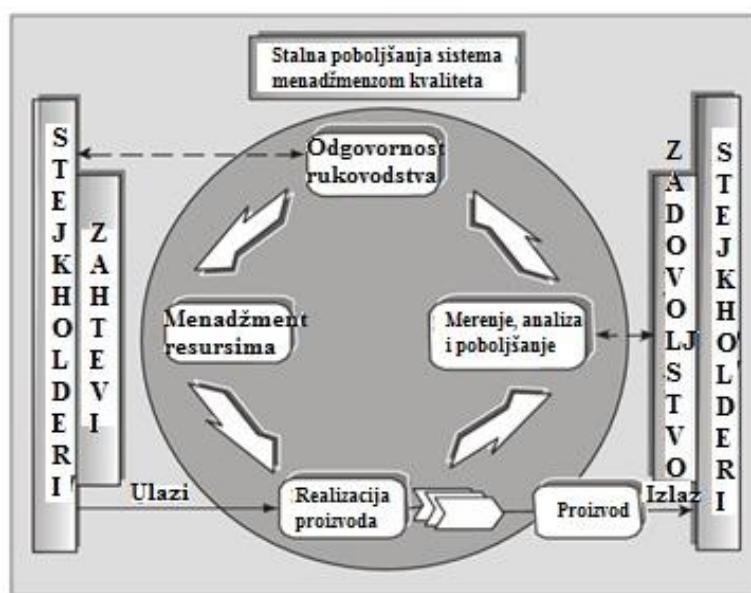
Prema [11] sisteme menadžmenta koji se baziraju na suštini procesnog pristupa iz ISO 9000 je moguće identifikovati kroz strategiju integracije.

Specifičnosti kod procesnog modela se ogledaju kroz primenu procesnog pristupa, a integriše se N sistema i to: QMS, EMS,

OHSAS i sistem menadžmenta bezbednosti hrane (HACCP). Ovi standardi imaju sličnosti u okviru njihove strukture tako da je integraciju standarda moguće izvesti na osnovu identičnih i specifičnih zahteva na koje se mora odgovoriti pri upravljanju procesa. To je razlog što procesni pristup predstavlja novi pristup menadžmentu. Suština standarda za sisteme menadžmenta (ISO 9001, ISO 14001, OHSAS 18001 i ISO 22000) upravo je u upravljanju procesima.

Procesni model prilikom implementiranja zahteva poznavanje procesa organizacije, zahteve interesne grupe, definisanje metodologije upravljanja, određivanje neophodnih resursa i sprovođenje svih procedura uz stalno unapređivanje i poboljšanje. Pri implementiranju procesnog modela ISM-a za dokumentaciju, realizaciju zahteva (proizvoda ili usluga) i merenja zadovoljstva stejkholdera odgovorni su osoba koja je zadužena, vlasnik procesa ili menadžer, a za realizaciju zaposleni i svi učesnici procesa.

U našoj zemlji je najviše zastupljen ovaj model ISM-a i to u 96,23% preduzeća.



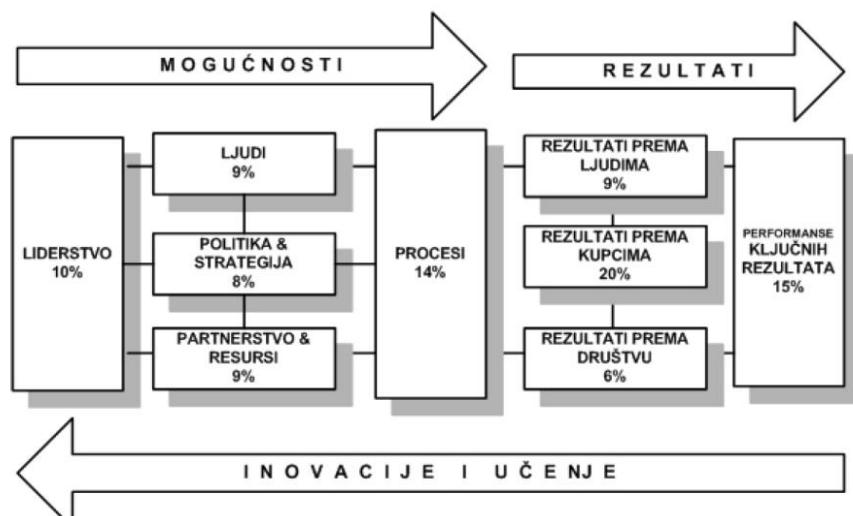
Sl. 3. Model sistema menadžmenta kvalitetom zasnovan na procesima [14]

## 2.4. EFQM model izvrsnosti (Alternativa A4)

EFQM model izvrsnosti je izgradila Evropska fondacija za menadžment kvaliteta 1992. godine i unapređen je 1999. godine. Model služi kao osnova za dodelu evropske nagrade za kvalitet i to za:

- velike kompanije i
- mala i srednja preduzeća.

Za razliku od drugih, ovaj model ima za bazu filozofiju menadžmenta totalnim kvalitetom (TQM) i zasniva se na integraciji dva sistema (interoperabilnost) i to sistema menadžmenta kvalitetom i sistema menadžmenta životnom sredinom (EFQM, 1998., EFQM, 2002.) – slika 4.



Sl. 4. EFQM model izvrsnosti [15]

Ovaj model ima devet kriterijuma pri čemu se pet odnose na mogućnosti koji pokazuju šta kompanija radi, dok se ostali odnose na rezultate. Rezultati pokazuju u kojoj meri organizacija koristi mogućnost.

Model EFQM je primenljiv kod onih kompanija čiji su zahtevi takvi da mogu da izgrade sopstvene pristupe u postizanju izvrsnosti. Unutar ovog modela ima nekoliko baznih koncepta koji su obavezni za njegovu primenu, a to su:

- orientisanost na rezultate, gde rezultati pokazuju izvrsnost koji su zadovoljstvo stejkohldera;

- fokusiranost na kupce, gde je izvrsnost kreiranje postojanog kupca;
- liderstvo i postojanost odlučnosti, gde je izvrsnost u liderstvu sa postojanim odlikama;
- menadžment procesima i činjenicama, gde je izvrsnost upravljanje kompanijom na osnovu procesa i činjenica;
- uključivanje zaposlenih i njihov razvoj, gde je izrsnost u motivisanju zaposlenih radi povećanja doprinosa;
- poboljšanje, inovacije i stalno edukacija, gde do izvrsnosti dovodi kreiranje

- inovacija i mogućnost za savremenije poslovanje;
- razvoj partnerstva, gde se izvrsnost manifestuje kroz razvoj i održavanje partnerstva uz povećavanje vrednosti;
  - društvena odgovornost, gde se izvrsnost ogleda u prevazilaženju nekih minimalnih obaveza u društvu i gde kompanija teži odgovornijem razumevanju zahteva društva.

Kriterijumi za ostvarenje poslovne izvrsnosti su: liderstvo, ljudi, politika i strategija, partnerstvo i resursi, procesi, rezultati prema kupcima i društvu i na kraju rezultati koji su zadovoljstvo svih zainteresovanih strana.

Zajedničke karakteristike modela EFQM, procesnog modela, modela Karapetrovića i modela Wilkinson - Dale su: sistemski pristup, stalna poboljšanja, zadovoljenje zahteva svih zainteresovanih strana, smanjenje obimne dokumentacije i to što oni nemaju ograničenja u pogledu vrste organizacije uključujući i rudarske kompanije.

### **3. DEFINISANJE KRITERIJUMA ZA IZBOR OPTIMALNOG MODELIA ISM-A**

Kriterijumi sadrže najvažnije karakteristike za izbor optimalnog modela implementacije ISM-a u rudarskim kompanijama, a to su:

**Troškovi uvođenja ISM-a (kriterijum C1)** je vrlo važan faktor za donošenje odluke pri izboru optimalnog modela ISM-a. Troškovi uvođenja se određuju za svaki predloženi model ISM-a u rudarskim kompanijama i njihov uticaj je srazmeran dobijenim rezultatima.

**Očekivani efekti ISM-a (kriterijum C2)** je takođe bitan faktor koji ima veliki uticaj pri donošenju odluke pri izboru optimalnog modela implementiranja ISM-a. Rudarske kompanije implementacijom optimalnog modela ISM-a treba da ostvare značajna poboljšanja, kao što su: izgradnja modela „nacionalne kulture“, bolja realizacija svoje politike i strategije, veće zadovoljstvo zapo-

slenih, smanjenje povreda na radu, stalna poboljšanja resursa (materijalnih, finansijskih i ljudskih), kontinualno poboljšanje procesa poslovanja, poboljšanje upravljanja kompanijom, zadovoljniji eksterni i interni kupci, bolji odnos prema društvu, poboljšanje zaštite životne okoline, poslovanje po svim propisima i pravilima, mogućnost poslovanja na globalnom tržištu, prednost prilikom učešća na tenderu, smanjenje troškova i dr.

**Vreme implementacije ISM-a (kriterijum C3)** je takođe, veoma važan faktor koji značajno utiče na izbor optimalne metode ISM-a. Na primer, ako se izabrani model implementira duži vremenski period od predviđenog, nekim od zainteresovana strana neće biti ispunjeni zahtevi, što povlači da se njihovo nezadovoljstvo odražava na ostale, tako da sve to dovodi do loše reputacije rudarske kompanije u okviru društvene zajednice. Neki od ovih modela ISM-a imaju kraći period implementiranja što može da bude veoma značajno za rudarske kompanije.

**Primenljivost modela (kriterijum C4)** je kriterijum koji ukazuje na stepen mogućnosti implementacije određenog modela ISM-a u rudarskim kompanijama. Neke modele je lakše implementirati, a druge teže. Cilj je da rudarska kompanija izabere onaj model koji nije težak za implementaciju i koji će joj dugoročno doneti mnogobrojne koristi. Pri tome, rudarska kompanija mora da uzme u obzir mnogobrojne faktore, kao što su određene njene specifičnosti, nivo opremljenosti, struktura radne snage, menadžment kompanije i dr.

### **4. AHP METOD**

AHP je kvantitativna tehnika koja omogućava strukturiranje kompleksnog problema odlučivanja sa više kriterijuma i pruža objektivnu metodologiju koja se primenjuje na širok spektar odluka.

AHP polazi od dekompozicije složenog problema odlučivanja u višedimenzionalnu hierarhijsku strukturu ciljeva, kriterijuma i

alternativa. Nakon toga, vrši se procena uticaja kriterijuma, onda se upoređuju alternative u odnosu na svaki kriterijum i vrši se konačno rangiranje alternativa.

Procena relativnog uticaja svakog kriterijuma i poređenje alternativa u odnosu na kriterijume se vrši preko matrice poređenja. To uključuje: formiranje matrice poređenja na svakom nivou hijerarhije, počev od drugog nivoa nadole; proračun težinskih koeficijenata za svaki element hijerarhije i procena stepena konzistentnosti u cilju provere konzistentnosti celokupnog procesa.

U tom cilju, definiše se skup alternativa  $\{A_1, A_2, \dots, A_n\}$  i skup težinskih koeficijenata kriterijuma  $\{w_1, w_2, \dots, w_n\}$ .

Upoređenje kriterijuma i alternativa vrši se na bazi skale sa ocenama od 1 do 9 – tabela 1.

**Tabela 1.** Skala poređenja elemenata odlučivanja

Dominantnosti	
Opis	Ocena
Jednako	1
Slaba dominacija	3
Jaka dominacija	5
Vrlo jaka dominacija	7
Apsolutna dominacija	9
2, 4, 6, 8 su međuvrednosti	

Rezultat upoređenja kriterijuma predstavlja matrica koja ima sledeći oblik:

$$W = \begin{bmatrix} w_i \\ \diagdown w_j \end{bmatrix} = \begin{bmatrix} w_1/w_1 & w_1/w_2 & \dots & w_1/w_n \\ w_2/w_1 & w_2/w_2 & \dots & w_2/w_n \\ \dots & \dots & \dots & \dots \\ w_n/w_1 & w_n/w_2 & \dots & w_n/w_n \end{bmatrix}$$

Nakon toga, vrši se upoređenje parova alternativa u odnosu na svaki kriterijum, pri čemu se dobija matrica poređenja  $A$  u kojoj element  $a_{ij}$  predstavlja odnos težinskog koeficijenta alternative  $A_i$  u odnosu na alternativu  $A_j$ .

$$A = \begin{bmatrix} a_{ij} \end{bmatrix} = \begin{bmatrix} 1 & a_{12} & \dots & a_{1n} \\ 1/a_{12} & 1 & \dots & a_{2n} \\ \dots & \dots & \dots & \dots \\ 1/a_{1n} & 1/a_{2n} & \dots & 1 \end{bmatrix}$$

Elementi  $A_{ij}$  predstavljaju odnos između težinskih koeficijenata  $w_i / w_j$  gde je  $w$  vektor težine svake alternative.

Matrica ima recipročna svojstva, kod koje su  $a_{ji} = 1/a_{ij}$ .

Posle izvršenog upoređenja računaju se težinski koeficijenti i dobija se vektor koeficijenata  $w = [w_1, w_2, \dots, w_n]$  koji se računa na bazi Satijeve procedure u dva koraka.

Prvo, matrica upoređenja parova  $A = [a_{ij}]_{n \times n}$  se normalizuje, a zatim se izračunavaju težine.

Normalizacija se vrši pomoću sledećeg obrasca:

$$a_{ij}^* = a_{ij} / \sum_1^n a_{ij} \quad (1)$$

za sve  $j = 1, 2, \dots, n$ .

Za izračunavanje težinskih koeficijenata koristi se sledeći obrazac:

$$w_i = \sum_1^n a_{ij}^* / n \quad (2)$$

za sve  $j = 1, 2, \dots, n$ .

Nakon upoređenja, vrši se provera stepena konzistentnosti. Stepen konzistentnosti treba da ima vrednost manju od 0,1. U suprotnom, moraju se ponovo razmatrati vrednosti koje su unete u matricu poređenja.

Stepen konzistentnosti se računa na sledeći način

$$CI = \lambda_{\max} - n / (n - 1) \quad (3)$$

gde  $\lambda_{\max}$  predstavlja značajan parametar kod AHP metode i on se koristi kao referentni

## 5. REZULTATI IZBORA OPTIMALNOG MODELA ISM-A

indeks za prikazivanje informacija kod proračuna stepena konzistentnosti ( $CR$ ).  $CR$  se računa na sledeći način:

$$CR = CI/RI \quad (4)$$

gde  $RI$  predstavlja slučajni indeks konzistentnosti dođen nasumice iz matrice upoređenja.

Određivanje konačnog ranga alternativa vrši se sintezom rezultata koji su dođeni na svim nivoima.

Nakon definisanja kriterijuma i modela ISM-a (alternativa) vrši se njihova ocena i rangiranje primenom AHP metode. Pri tome, za proračun je korišćen softver Criterium DecisionPlus.

Prvi korak je definisanje višedimenzijske hijerarhijske strukture ciljeva, kriterijuma i alternativa – slika 5.

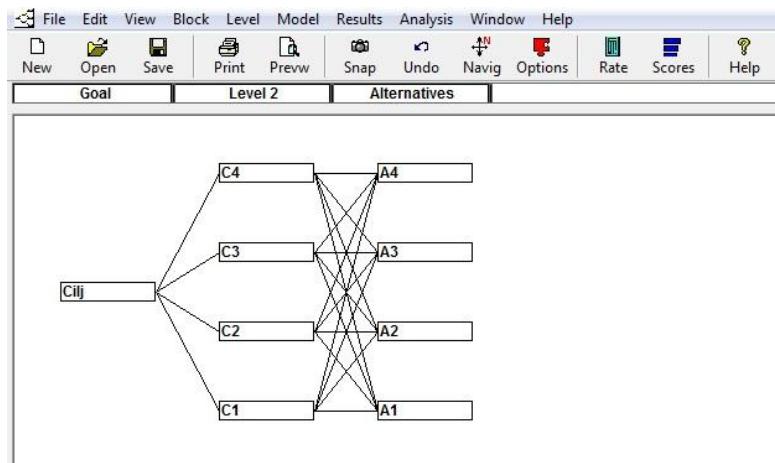
Nakon toga vrši se određivanje težinskih koeficijenata kriterijuma uz pomoć skale poređenja koja je data u tabeli 1. Rezultati poređenja su prikazani u tabelama 2 i 3.

**Tabela 2.** Definisanje težinskih koeficijenata kriterijuma

Kriterijumi	C1	C2	C3	C4
C1	1	1/5	5	2
C2		1	8	5
C3			1	1/5
C4				1

**Tabela 3.** Rezultati težinskih koeficijenata kriterijuma

Kriterijumi	C1	C2	C3	C4
Težinski koeficijenti	0.193	0.624	0.045	0.138
Stepen konzistentnosti	0.084<0.1			



**Sl. 5.** Higerarhija odlučivanja (Criterium Decision Plus softver))

U sledećem koraku se vrši upoređivanje modela ISM-a (alternativa) u odnosu na sva četiri definisana kriterijuma – tabele 4 - 7.

**Tabela 4.** Upoređenje alternativa u odnosu na kriterijum C1

Alternative	A1	A2	A3	A4
A1	1	2	1	1
A2		1	2	1/2
A3			1	1/3
A4				1
Stepen konzist.		0.077<0.1		

**Tabela 5.** Upoređenje alternativa u odnosu na kriterijum C2

Alternative	A1	A2	A3	A4
A1	1	1/3	1/5	1
A2		1	1/3	3
A3			1	7
A4				1
Stepen konzist.		0.012<0.1		

**Tabela 6.** Upoređenje alternativa u odnosu na kriterijum C3

Alternative	A1	A2	A3	A4
A1	1	3	5	1
A2		1	3	1/3
A3			1	1/5
A4				1
Stepen konzist.		0.016<0.1		

**Tabela 7.** Upoređenje alternativa u odnosu na kriterijum C4

Alternative	A1	A2	A3	A4
A1	1	1/3	1/3	1
A2		1	1	3
A3			1	3
A4				1
Stepen konzist.		0.00<0.1		

Na kraju, nakon izvršenih proračuna dobijeni su rezultati rangiranja – tabela 8. Rezultati pokazuju da je najbolje rešenje alternativa A3 (procesni model ISM-a).

Na drugom mestu je alternativa A2 (model Karapetrovića), na trećem mestu je alternativa A4 (EFQM model izvrsnosti) i na poslednjem mestu je alternativa A1 (Wilkinson - Dale-ov model).

**Tabela 8.** Konačni rang modela ISM-a

Red. br.	Model ISM-a	Rezultat
1.	A3 (Procesni model ISM-a)	0.449
2.	A2 (model Karapetrovića)	0.246
3.	A4 (EFQM model izvrsnosti)	0.157
4.	A1 (Wilkinson-Dale-ov model)	0.148

## 6. ANALIZA DOBIJENIH REZULTATA

Analiza obuhvata kriterijume i njihov uticaj na rangiranje modela ISM-a i same modele ISM-a.

Kada se analiziraju kriterijumi, najvažniji su njihovi težinski koeficijenti, jer je to njihova mera uticaja na rezultat rangiranja alternativa, odnosno modela ISM-a. Iz tabele 3. se vidi da kriterijum C2 (očekivani efekti ISM-a) ima najveći uticaj na rezultat rangiranja jer njegov težinski koeficijent iznosi 0,624. To znači da on utiče sa 62,4% na doношење odluke u odnosu na ostale kriterijume. To pokazuje da je kod izbora optimalnog modela ISM-a najvažnije šta će rudarske kompanije dobiti nakon njegove implementacije, odnosno koje će sve pozitivne efekte one ostvariti, što je i cilj ovog procesa.

Na drugom mestu po uticaju je kriterijum C1 (troškovi uvođenja ISM-a), koji utiče sa 19,3% na rezultat rangiranja. To pokazuje da su troškovi implementacije optimalnog modela ISM-a vrlo važni za rudarske kompanije, s obzirom da se one nalaze u teškoj finansijskoj situaciji.

Na trećem mestu po značaju se nalazi kriterijum C4 (primenljivost modela), koji utiče sa 13,8% na ovaj proces. To pokazuje da je za rudarske kompanije vrlo važno koliko je određeni model ISM-a pogodan za primenu u uslovima u kojima one funkcionišu. Implementacija ISM-a zahteva formiranje tima za uvođenje, sticanje novih znanja, primena novih metoda rada, upravljanja i procedura, savladavanje otpora, samo uvođenje i kontrolu dobijenih rezultata.

Na kraju, najmanje uticajem kriterijum je C3 (vreme implementacije ISM-a) koji ima težinski koeficijent od 0,045. To pokazuje da je vreme koje je potrebno za uvođenje ISM-a, iako važno, u drugom planu u odnosu na ostale efekte koje se očekuju od ovog sistema.

Kod analize konačnog ranga alternativa (modela ISM-a) polazi se od optimalne (najbolje) alternative. To je alternativa A3 (procesni model ISM-a) koji ima najveći vrednost rezultata od 0,449. Razlog je u tome što se ovaj model fokusira upravo na ono što je najjača karakteristika rudarskih

kompanija, a to je postojanje i neprekidno odvijanje vrlo kompleksnih i mnogobrojnih procesa u toku rada. Procesi su mesta gde se najviše može uraditi, što je i cilj ovog modela. Sa druge strane, ovaj model ISM-a integriše razne sisteme kao što su QMS, EMS, OHSAS, ali i sve zaposlene u kompanijama. Sve to omogućava značajno poboljšanje performansi rudarskih kompanija u najvećem broju ili u svim oblastima njihovog funkcionisanja.

Na drugom mestu po rangiranju se nalazi alternativa A2 (model Karapetrovića). On razmatra integraciju pet sistema – QMS, EMS, OHSAS, korporacijski menadžment sistem socijalne odgovornosti (CSRMS) i finansijski sistem menadžmenta (FMS) i okrenut je ka stalnim poboljšanjima procesa. Za razliku od prethodnog modela, on je složeniji, zahtevniji i manje pogodan za rudarske kompanije kod nas.

Na trećem mestu je alternativa A4 (EFQM model izvravnosti), dok je na poslednjem mestu alternativa A1 (Wilkinson-Dale-ov model). Razlika u rezultatu između ovih modela je mala. Njihov nedostatak u odnosu na prethodna dva modela ISM-a je u tome što se oni u manjoj meri bave procesima, zatim manje su prilagođeni rudarskim kompanijama i time, manji su rezultati koji oni mogu da pruže. Dobra strana ovih modela je u tome što oni integrišu u svoj model sistem menadžmenta životnom sredinom, što je vrlo važno kod rudarskih kompanija.

## ZAKLJUČAK

U ovom radu je primenjena višekriterijumska metoda donošenja odluke u cilju izbora optimalnog modela Integriranog sistema menadžmenta (ISM) u rudarskim kompanijama u našoj zemlji. Izbor optimalnog modela ISM-a je jedna od najznačajnijih strateških odluka rudarskih kompanija. Analizirana su četiri modela ISM-a – Wilkinson-Dale-ov model (alternativa A1), model Karapetrovića (alternativa A2), procesni model (alternativa A3) i EFQM model

izvrsnosti (alternativa A4). Takođe, razmatrana su četiri kriterijuma za rangiranje – troškovi uvođenja ISM-a (kriterijum C1), očekivani efekti ISM-a (kriterijum C2), vreme implementacije ISM-a (kriterijum C3) i primenljivost modela ISM-a (kriterijum C4).

Rangiranje modela ISM-a je izvršeno pomoću AHP metode za višekriterijumsko odlučivanje. Kod ove metode, prvo se vrši određivanje težinskih koeficijenata kriterijuma za rangiranje, a onda ocenjivanje predloženih modela ISM-a i njihovo kompletno rangiranje.

Primenjena metoda za višekriterijumsku analizu može biti od velike pomoći donosiocima odluka, jer omogućava laku i kvalitetnu analizu uticajnih faktora i parametara. Na osnovu dobijenih rezultata AHP metodom, izabran je najbolji model ISM-a za rudarske kompanije u našoj zemlji, a to je procesni model (alternativa A3). Najuticajniji kriterijumiza kompletno rangiranje alternativa (modela ISM-a) su očekivani efekti ISM-a (kriterijum C2) i troškovi uvođenja ISM-a (kriterijum C1).

## LITERATURA

- [1] Đekić, V. et al., Importance of interoperability information and information systems in the implementation of the model IMS. Internacional Scientific Conference Managament, Mladenovac, Serbia (2012) 171-175.
- [2] Heleta M., Menadžment kvaliteta, Univerzitet Singidunum, Beograd, Srbija (2008) 5.
- [3] Brzaković M., Interoperabilnost i bezbednost informacija u organizacijama od strateškog značaja u vanrednim situacijama – Doktorska disertacija, Fakultet bezbednosti, Beograd, Srbija (2009).
- [4] Volanović, S. Razvoj opštег modela za implementaciju Integrisanog sistema menadžmenta na osnovu procene rizika u procesima organizacija, Doktorska disertacija, Fakultet Tehničkih Nauka, Novi Sad, Srbija (2014).
- [5] Saaty T. L., The Analytical Hierarchy Process, New York: McGraw-Hill (1980).
- [6] Bogdanović D., Obradović Lj., Miletić S.: Izbor optimalne metode sanacije degradiranih površina oko borske reke nizvodno od flotacijskog jalovišta Bor, Mining and Metallurgy Engineering Bor, 4(2014) 147-156.
- [7] Wilkinson G., Dale B., Integrated management systems: a model based on total quality approach, Managing Service Quality, 11(5) (2001) 318-330.
- [8] Jenkić R., Kulture i organizacije - Organizacijske kulture Geerta Hofstede-a, Zbornik radova Pravnog fakulteta u Splitu, 1 (2011) 103-123.
- [9] <https://scholar.google.com/citations?user=Q2V0P6oAAAAJ&hl=en&oi=ao> (accessed 13.05.2015)
- [10] Paunkovic J., Educational Programs for Sustainable Societies Using Cross-Cultural Management Method. Global Sustainable Communities Handbook: Green Design Technologies and Economics (2014): 387- Butterworth Heinemann imprint of Elsevier, Elsevier Copyright © 2014.
- [11] Paunkovic J., Zikic S., Cvetkovic A., Sustainable Utilization of Health Care Technologies is Influenced by Organizational and Cultural Factors – A Case Study. Advances in Biomedicine and Health Science, (2013) 57.
- [12] Karapetrović S., Measuring of integrated management systems, Measuring Business Excellence, 7(1) (2003) 4-13.
- [13] Karapetrovic S., Jonker J., Integration of standardized management systems: searching for a recipe and ingredients, Total Quality Management, 14(04) (2003) 451-459.
- [14] Petrović M., Procesni pristup integrisanim menadžmentu, 33. Nacionalna konferencija o kvalitetu: Festival kvaliteta, AQS i Centar za kvalitet, Kragujevac, Srbija (2008).
- [15] European Foundation for Quality Management (EFQM), EFQM Model for Business.

## INSTRUCTIONS FOR THE AUTHORS

Journal **MINING AND METALLURGY ENGINEERING BOR** is published four times per a year and publishes the scientific, technical and review paper works. Only original works, not previously published and not simultaneously submitted for publication elsewhere, are accepted for publication in the journal. The papers should be submitted in both, Serbian and English language. The papers are anonymously reviewed by the reviewers after that the editors decided to publish. The submitted work for publication should be prepared according to the instructions below as to be included in the procedure of reviewing. Inadequate prepared manuscripts will be returned to the author for finishing.

**Volume and Font size.** The work needs to be written on A4 paper (210x297 mm), margins (left, right, upper and bottom) with each 25 mm, in the Microsoft Word later version, font Times New Roman, size 12, with 1.5 line spacing, justified to the left and right margins. It is recommended that the entire manuscript cannot be less than 5 pages and not exceed 10 pages.

**Title of Work** should be written in capital letters, bold, in Serbian and English. Under the title, the names of authors and institutions where they work are written under the title. The author of work, responsible for correspondence with the editorial staff, must provide his/her e-mail address for contact in a footnote.

**Abstract** is at the beginning of work and should be up to 200 words, include the aim of the work, the applied methods, the main results and conclusions. The font size is 10, italic.

**Key words** are listed below abstract. They should be minimum 3 and maximum of 6. The font size is 10, italic.

**Basic text.** The papers should be written concisely, in understandable style and logical order that, as a rule, including the introductory section with a definition of the aim or problem, a description of the methodology, presentation of the results as well as a discussion of the results with conclusions and implications.

**Main titles** should be done with the font size 12, bold, all capital letters and aligned with the left margin.

**Subtitles** are written with the font size 12, bold, aligned to the left margin, large and small letters.

**Figure and Tables.** Each figure and table must be understandable without reading the text, i.e., must have a serial number, title and legend (explanation of marks, codes, abbreviations, etc.). The text is stated below the figure and above the table. Serial numbers of figures and tables are given in Arabic numbers.

**References in the text** are referred to in angle brackets, exp. [1, 3]. References are enclosed at the end in the following way:

- [1] Willis B. A., Mineral Procesing Technology, Oxford, Pergamon Press, 1979, pg. 35. (for the chapter in a book)
- [2] Ernst H., Research Policy, 30 (2001) 143–157. (for the article in a journal)
- [3] www: <http://www.vanguard.edu/psychology/apa.pdf> (for web document)

Specifying the unpublished works is not desirable and, if it is necessary, as much as possible data on the source should be listed.

**Acknowledgement** is given where appropriate, at the end of the work and should include the name of institution that funded the given results in the work, with the name and number of project, or if the work is derived from the master theses or doctoral dissertation, it should give the name of thesis / dissertation, place, year and faculty where it was defended. Font size is 10, italic.

The paper works are primarily sent by e-mail or in other electronic form.

Editorial address : Journal MINING AND METALLURGY ENGINEERING BOR

Mining and Metallurgy Institute  
35 Zeleni bulevar, 19210 Bor  
E-mail: [nti@irmbor.co.rs](mailto:nti@irmbor.co.rs); [milenko.ljubojev@irmbor.co.rs](mailto:milenko.ljubojev@irmbor.co.rs)  
Telephone: +381 (0) 30/435-164; +381 (0) 30/454-110

*We are thankful for all authors on cooperation*

## UPUTSTVO AUTORIMA

**Časopis MINING AND METALLURGY ENGINEERING BOR** izlazi četiri puta godišnje i objavljuje naučne, stručne i pregledne radove. Za objavljivanje u časopisu prihvataju se isključivo originalni radovi koji nisu prethodno objavljivani i nisu istovremeno podneti za objavljivanje negde drugde. Radovi se dostavljaju i na srpskom i na engleskom jeziku. Radovi se anonimno recenziraju od strane recenzenta posle čega uredništvo donosi odluku o objavljinju. Rad priložen za objavljinje treba da bude pripremljen prema dole navedenom uputstvu da bi bio uključen u proceduru recenziranja. Neodgovarajuće pripremljeni rukopisi biće vraćeni autoru na doradu.

**Obim i font.** Rad treba da je napisan na papiru A4 formata (210x297 mm), margine (leva, desna, gornja i donja) sa po 25 mm, u Microsoft Wordu novije verzije, fontom Times New Roman, veličine 12, sa razmakom 1,5 reda, obostrano poravnat prema levoj i desnoj margini. Preporučuje se da celokupni rukopis ne bude manji od 5 strana i ne veći od 10 strana.

**Naslov rada** treba da je isписан velikim slovima, bold. Ispod naslova rada pišu se imena autora i institucija u kojoj rade. Autor rada zadužen za korespondenciju sa uredništvom mora da navede svoju e-mail adresu za kontakt u fusuotni.

**Izvod** se nalazi na početku rada i treba biti dužine do 200 reči, da sadrži cilj rada, primenjene metode, glavne rezultate i zaključke. Veličina fonta je 10, italic.

**Ključne reči** se navode ispod izvoda. Treba da ih bude minimalno 3, a maksimalno 6. Veličina fonta je 10, italic.

**Osnovni tekst.** Radove treba pisati jezgrovito, razumljivim stilom i logičkim redom koji, po pravilu, uključuje uvodni deo s određenjem cilja ili problema rada, opis metodologije, prikaz dobijenih rezultata, kao i diskusiju rezultata sa zaključcima i implikacijama.

**Glavni naslovi** trebaju biti urađeni sa veličinom fonta 12, bold, sve velika slova i poravnati sa levom marginom.

**Podnaslovi** se pišu sa veličinom fonta 12, bold, poravnato prema levoj margini, velikim i malim slovima.

**Slike i tabele.** Svaka ilustracija i tabela moraju biti razumljive i bez čitanja teksta, odnosno, moraju imati redni broj, naslov i legendu (objašnjenje oznaka, šifara, skraćenica i sl.). Tekst se navodi ispod slike, a iznad tabele. Redni brojevi slike i tabela se daju arapskim brojevima.

**Reference u tekstu** se navode u uglačastim zagradama, na pr. [1,3]. Reference se prilaže na kraju rada na sledeći način:

[1] B.A. Willis, Mineral Procesing Technology, Oxford, Pergamon Press, 1979, str. 35. (za poglavje u knjizi)

[2] H. Ernst, *Research Policy*, 30 (2001) 143–157. (za članak u časopisu)

[3] www: <http://www.vanguard.edu/psychology/apa.pdf> (za web dokument)

Navođenje neobjavljenih radova nije poželjno, a ukoliko je neophodno treba nvesti što potpunije podatke o izvoru.

**Zahvalnost** se daje po potrebi, na kraju rada, a treba da sadrži ime institucije koja je finansirala rezultate koji se daju u radu, sa nazivom i brojem projekta; ili ukoliko rad potiče iz magistarske teze ili doktorske disertacije, treba dati naziv teze/disertacije, mesto, godinu i fakultet na kojem je odbranjena. Veličina fonta 10, italic.

Radovi se šalju prevashodno elektronskom poštom ili u drugom elektronskom obliku.

Adresa uredništva je: Časopis MINING AND METALLURGY ENGINEERING BOR

Institut za rудarstvo i metalurgiju

Zeleni bulvar 35, 19210 Bor

E-mail: [nti@irmbor.co.rs](mailto:nti@irmbor.co.rs) ; [milenko.ljubojev@irmbor.co.rs](mailto:milenko.ljubojev@irmbor.co.rs)

Telefon: 030/435-164; 030/454-110

*Svim autorima se zahvaljujemo na saradnji.*

CIP - Каталогизација у публикацији  
Народна библиотека Србије, Београд

622

MINING and Metallurgy Engineering Bor /  
editor-in-chief Milenko Ljubojev. - 2013, no.  
2- . . - Bor : Mining and Metallurgy  
Institute Bor, 2013- (Bor : Grafomedtrade). -  
24 cm

Tromesečno. - Je nastavak: Rudarski radovi =  
ISSN 1451-0162  
ISSN 2334-8836 = Mining and Metallurgy  
Engineering Bor  
COBISS.SR-ID 201387788